# Open Economy Macroeconomics, Aalto University SB, Spring 2017 2019 Sticky Prices: The Dornbusch Model

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Jouko Vilmunen (BoF) Open Economy Macroeconomics, Aalto Unive

- The simple monetary model is incapable of explaining basic facts on international prices
  - PPP is the critical assumption
- Observed exchange rate volatility far greater than the simple model implies
- The Mundell-Fleming model, by assuming fixed or sticky prices, is relevant for the very shortest horizons
- Dornbusch's model, introduced in 1976, is a hybrid
  - $\bullet\,$  short-run price stickiness  $\rightarrow\,$  Keynesian features
  - long-run characteristics like in the monetary model
- Key idea: differential adjustment speed in goods and financial markets
  - goods markets: slow
  - financial markets: fast

### The overshooting model

- Implication: the burden of short-run adjustment falls on financial markets which overreact to different shocks, monetary shocks in particular
  - financial markets overshoot relative to long-run equilibrium
- Why? Price level initially fixed, a change in the *nominal* money stock is a change in the *real* money stock
  - an instantaneous change in the money demand has to result
  - only possible, if the interest rate changes appropriately, if, in particular, output is assumed fixed
- In the short-run, monetary policy changes have what is nowadays known as the *liquidity effect*
- Change in interest rates only temporary and the price level will start its delayed response
  - real money stock will starts to revert itself back to the original level driving interest rates, aggregate demand and the real exchange rate back to their original level

- Hence, over the long-run all real variables have reverted back to their original values
  - a flavour from the monetary model!
- Change in the nominal exchange rate in the long-run equilibrium reflects the proportionate change in the nominal money supply
- We will next outline the overshooting model, with two conventions

  - comparative statics: we will start from an initial equilibrium position and consider what happens to the *level* of the exchange rate once we change the *level* of the money supply

## The overshooting model: assumptions

- We need the following assumptions
- Aggregate demand is determined by the standard IS-LM mechanism/model
- Financial markets adjust instantaneously. In particular, investors are risk neutral, so that UIRP holds at all times
  - Hence, perfect capital mobility ensures that expected depreciation/appreciation is just enough to offset any interest rate differential between the domestic and foreign economy

$$r - r^f = \Delta s^e$$

- But: how are expectations actually determined?
  - suppose there is a long-run equilibrium real exchange rate  $\overline{Q}$  (and nominal exchange rate  $\overline{S}$ ), which determined by the domestic money stock, national income and interest rates relative to those of the rest of the world (ROW), ie. by the monetary model

### The overshooting model: assumptions

- $\bullet\,$  Dornbusch model: Q in equilibrium only in the long-run, deviations in the short-run
- Dornbusch assumes that the expected rate of depreciation of the domestic currency  $\frac{S^e-S}{S}$  is proportional to the percentage deviation of the actual exchange rate from its long-run equilibrium value  $\overline{S}$ ,  $\frac{\overline{S}-S}{\overline{S}}$
- We can formalize this idea by saying that there is a positive parameter Θ such that

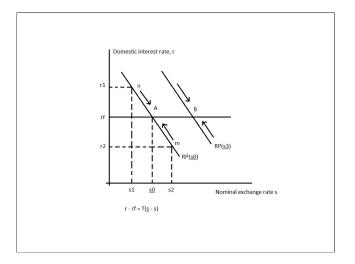
$$\frac{S^e-S}{S} = \Theta\left(\frac{\overline{S}-S}{S}\right)$$

• Since  $\frac{X-Y}{Y}\approx \ln(1+\frac{X-Y}{Y})=\ln(X)-\ln(Y)=x-y,$  we can rewrite the above as

$$\Delta s^{e} = \Theta\left(\overline{s} - s\right)$$

 We can represent this relationship graphically in the next figure (slope −Θ)

### The force of the UIP



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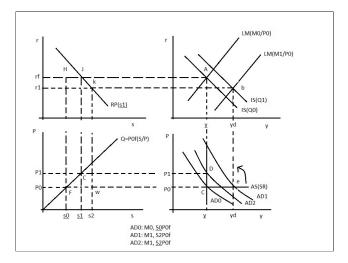
# Overshooting: adjustment

- Initially the economy is in point A with an exchange rate of <u>s0</u> and nominal interest rate at *rf*
- If the domestic interest rate falls to *r*2, continuous validity of the UIRP implies that the domestic currency is expected to appreciate
- Given Dornbusch's model for exchange rate expectations, this means that the value of the domestic currency (euro) is currently below its equilibrium value, ie.  $S > \overline{S}$ , so as to generate the expectation of a future euro appreciation
- Euro will appreciate towards its long run value as long as it is currently below the equilibrium value
- The arrows in the figure indicate the direction of adjustment that the exchange rate takes once off its long-run equilibrium
- The same analysis holds for any long-run equilibrium value of the domestic currency, eg. point **B**
- Note that the UIRP holds at any point along the **RP** line in the figure!

## Goods market

- Deviations from the equilibrium exchange rate result from the following assumption
- 3. The price level is sticky. That is aggregate supply curve is flat in the immediate impact phase, increasingly steep in the adjustment phase and, ultimately, vertical in the long-run equilibrium
  - In the long-run the exchange rate is at its equilibrium level, ie. the market clearing real value, given the domestic and foreign price levels
  - In the short-run, the price level is fixed, so shocks move the nominal exchange rate and, hence, the real exchange rate
    - current account surpluses and deficits will follow
  - With the passage of time and without any further shocks, the economy moves back to its long-run real exchange rate as a result of movements in both the nominal exchange rate and the price level
  - Let us look at the next figure to see what the Dornbusch model implies

# Overshooting in graphics



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- In the figure:
  - top rhs figure is the IS-LM diagram, showing the determination of aggregate demand
  - top lhs figure is the RP diagram (initial *S* at <u>s0</u>, the corresponding UIRP line not drawn)
  - bottom rhs figure AD-AS curves, AS for both long-run and short-run (AS(SR))
  - bottom lhs figure shows the PPP line and deviations from the PPP level

#### • Long-run equilibrium:

- aggregate demand is equal to aggregate supply: no upward or downward pressure on the price level
- domestic and foreign interest rates are equal: static exchange rate, no expected change
- the real exchange rate is at its long-run level: no imbalances in the current account
- satisfied at points A, C, F, H in the figure

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### Monetary expansion

- Suppose ECB decides to increase the domestic money supply from *M*0 to *M*1
- Long-run effects as in the monetary model: vertical long-run AS curve means that the price level has to increase as much as the money supply leaving the real money stock unchanged
  - for fixed government expenditure, the IS-curve will not shift if the real exchange rate returns back to its original level
- Short-run effects:
  - LM curves shifts down and to the right giving rise, at fixed real income, to an excess supply of domestic money
  - domestic interest would have to fall (to *r*1) to bring about the absorption of the temporarily higher real money stock (*liquidity effect*)
  - lower domestic interest rate, ie. negative interest rate differential induce expectations of a stronger domestic currency
    - domestic currecy depreciates immediately to generate these expectations
    - S immediately jumps to s2

- domestic and foreign price level fixed in the short-run, hence the real exchange rate weakens to Q1, boosting net exports and domestic demand → IS curve shifts up and to the right (point b)
- this increase in demand represents, given the flat short-run AS curve, also an increase in output produced
- with a given interest rate at *r*1 the temporary equilibrium is at point *k* in the top lhs figure
- subsequent adjustment takes place along the RP curve
- But note that the short-run exchange rate S at s2 is above the long-run equilibrium level of  $\underline{s1}$ 
  - this is the essence of the Dornbusch model: after the monetary expansion, the domestic currency weakens more than its new long-run equilibrium value, ie. it overshoots its long-run equilibrium level

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#### What is important?

- The extent of the overshoot depends on two factors:
  - interest rate elasticity of money demand; our formalism is

$$\frac{M}{P} = ky - lr$$
$$\frac{dr}{dy} = \frac{k}{l}$$

so that a fall in the interest elasticity of money demand, *I*, will make the LM curve steeper and the greater will the fall in the interest rate have to be from any given increase in the real money stock

- *the slope of the RP curve*; the flatter it is the more the exchange rate must overshoot its long-run equilibrium, for any given change in the interes rate
  - $\bullet\,$  the slope of the RP line is determined by the expectations parameter  $\Theta\,$

$$r - r^{f} = \Theta(\overline{s} - s)$$
$$\frac{\partial r}{\partial s} = -\Theta$$

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so lower  $\Theta$  implies larger overshooting

## What is important?

- The intuition for the last result is that when ⊕ is small, a larger gap between the current exchange rate and the corresponding long-run level is required to generate any given interest rate differential
- If ⊕ falls to zero no interest rate differential would be possible, because no matter how large the gap between current and long-run equilibrium exchange rate, no expected currency appreciation would be generated by the gap
- Note that along the adjustment path to the long-run equilibrium in the Dornbusch model, rising interest rates coincides with an appreciating domestic currency, an implication often observed in actual data
- However, it should be noted that it is wrong to conclude from this that the rising domestic interest rate *causes* the domestic exchange rate to appreciate; rather, both phenomena result from the same cause, namely expansionary domestic monetary policy and the concomitant, albeit temporary, undervaluation of the domestic

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• Dornbusch's overshooting model can be represented formally as follows

$$\begin{aligned} r - r^{f} &= \Delta s^{e} \quad (\text{UIRP}) \\ \Delta s^{e} &= \Theta \left( \overline{s} - s \right) \quad (\text{S expectations}) \\ m - p &= k \overline{y} - lr \quad (\text{MM equilibrium}) \\ y^{d} &= h(s - p) = h(q), \quad q = s - p \quad (\text{AD}) \\ \dot{p} &= \pi \left( y^{d} - \overline{y} \right) \quad (\text{Inflation adjustment}) \end{aligned}$$

#### Formal model

• where  $\overline{y}$  is constant and

$$\dot{p} = rac{d \ln p}{dt}$$
 (inflation rate)

- Note that we have set the foreign price level to unity,  $P^f=1$ , so that the log of it  $\ln P^f=\ln 1=0$
- Note also that inflation responds to excess demand y<sup>d</sup> y
   inflation rate will increase if aggregate demand exceed aggregate long-run output
- This system can be reduced to two equations:

$$p = \underbrace{m - k\overline{y} + lr^{f}}_{L} + l\Theta(\overline{s} - s)$$
$$= L - l\Theta(s - \overline{s})$$
$$\dot{p} = \pi [h(s - p) - \overline{y}]$$

that is one equation for the price level and another for the rate of inflation Jouko Vilmunen (BoF) Open Economy Macroeconomics, Aalto Unive 08.03.2017 17 / 27

### Formal model: long-run equilibrium

- Long-run equilibrium:  $y^d \overline{y} = 0$ , so the price level is stable, ie. rate of inflation is zero p = 0
- Hence, from the inflation adjustment equation we have

$$h(\overline{s}-\overline{p})-\overline{y}=0 \iff \overline{s}-\overline{p}=\overline{q}=rac{\overline{y}}{h}$$

- There is strong implication here, reflecting the classical monetary aspects of the Dornbusch model: *in the long-run, only the (growth of the) capacity output will affect the real exchange rate; any change in the nominal exchange rate S is matched by a change in the price level*
- The expected rate of depreciation Δs<sup>e</sup> is in the long-run zero, since S is in equilibrium; hence

$$\overline{p} = L = m - k\overline{y} + lr^f$$

hence in the long-run equilibrium the price level is equal to the ratio of the money stock to the level of demand when it is at its long-run level or when the domestic and foreign interest rates are equal

## Formal model: long-run equilibrium

• Finally, the long-run equilbrium for the nominal exchange rate can be obtained by combining the two last equations

$$\overline{s} = (h^{-1} - k) \overline{y} + m + lr^{f}$$

- Now, all of our previous analysis is vindicated by the last two equations: an increase in the domestic money stock pushes up the long-run values of the domestic price level and exchange rate in the same proportion and hence leaves the real exchange rate and, by implication, aggregate output untouched
- Short-run dynamics (disequilibrium): inflation adjustment can now, given the long-run solution, written conveniently as

$$\dot{p} = \pi h(q - \overline{q})$$

so that the larger deviations of the real exchange rate from its long-run equilibrium level will generate higher rates of inflation

# Formal model: short-run dynamics (disequilibrium)

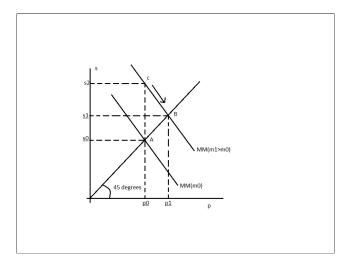
 Money market equilibrium implies, on the other hand, that deviations of the price level from its long-run level are given by

$$p - \overline{p} = -I\Theta(s - \overline{s})$$
 (SRMM)

(Note! In Copelands book, ch 7 p. 207 the sign is not correct)

- This is a necessary condition for the *short-run* equilibrium in the money market
- Hence, the system adjust so as to preserve this relationship at all times, which means that the economy lies somewhere along a downward sloping line in the (p, s) -space (with slope  $-\frac{1}{I\Theta}$ )
- See next figure, where we have drawn the long-run condition p = 0 together with (SRMM)

## Formal model: Graphics



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## Formal model: Graphics

- Economy starts at  $(p0, \underline{s0})$ , where the money supply is m0
- Money supply increases to m1: MM curve shifts out and to the right (MM (m0) to MM(m1))
- Price level fixed, nominal exchange rate jumps from <u>s0</u> to s2
- Post jump convergence **along** the *MM*(*m*1) curve from point *C* towards point *B*:
  - new long-run equilibrium  $(\underline{p1}, \underline{s1})$ : that is the change in the price level equals the change in the nominal exchange rate dp = ds  $(d = \Delta)$
- Short-run overshooting: size  $s2 \underline{s1}$
- Now, **perfect foresight** means expectations are fullfilled at any point in time: hence expected values equal realized values, ie

$$\Delta s^e = \Delta s = \dot{s}$$
  
 $\Delta p^e = \Delta p = \dot{p}$ 

• We have

$$\dot{p} = \pi h(q - \overline{q})$$

$$= \pi h(s - p - \overline{s} + \overline{p})$$

$$= \pi h(s - \overline{s} - (p - \overline{p}))$$

$$= \pi h(1 + I\Theta)(s - \overline{s})$$

• On the other hand, money market equilibrium implies

$$p = L - I\Theta(s - \overline{s})$$
, ie  
 $\dot{p} = -I\Theta\dot{s} = I\Theta^2(s - \overline{s})$ 

#### Formal model: Perfect foresight

 So, along the perfect foresight path these two expressions for the inflation rate has to be consistent with each other: this can happen only if the the expectations parameter Θ satisfies

$$\begin{aligned} I\Theta^2 &= \pi h (1 + I\Theta) \iff \\ \Theta &= \pi h \left[ 1 + \left( \frac{1}{I\Theta} \right) \right] \end{aligned}$$

- There's nothing magical about this particular parameter value or nothing particularly illuminating in computing this value:
  - what may be interesting is to note that the model as presented includes a special case where the market's apparently rule of thumb (of forming expectations) is self-fulfilling, so that its anticipations always turn out to be correct in the short- as well as in the long-run (perfect foresight = rational expectations)
- How do we prove that overshooting takes place? Take the semi-reduced solution to the price level

$$p = L - I\Theta(s - \overline{s})$$

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### Formal model: Overshooting

• In the long run:  $dm = d\overline{s}$  and, importantly, at the time of the money supply changes, the price level is fixed, ie. dp = 0

$$0 = (1 + I\Theta)dm - I\Theta ds \iff$$
$$ds|_{dp=0} = \left[1 + \left(\frac{1}{I\Theta}\right)\right]dm > dm$$

- So that the nominal exchange rate indeed overshoots its long-run equilibrium level
- What about empirical testing of the overshooting hypothesis?
- The Dornbusch model is very difficult to test
  - permanent increases in the money supply
  - expectations formation
  - lags in the response of the exchange rate to money supply changes
  - etc
- Instead, use the approach proposed by Jeffrey Frankel: it is based on real interest rate differentials

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#### Empirical testing: Frankel approach

 The starting point of the Frankel approach is a small addition to the Dornbusch expectations mechanisms: denote by a tilde above the variable x, x, the ratio of domestic x to foreign x<sup>f</sup>. so that

$$\Delta s^{e} = \Theta \left( \overline{s} - s \right) + \Delta \widetilde{p}^{e}$$

that is the difference between expected domestic and foreign inflation rates enters foreign exchange rate expectations

- Frankel extension amounts to a generalization of the Dornbusch mechanism to accommodate long-run inflation
- UIRP now gives

$$\begin{aligned} \widetilde{r} &= \Theta\left(\overline{s}-s\right) + \Delta \widetilde{\rho}^e \text{ or } \\ \overline{s} &= s + \frac{1}{\Theta}\left(\widetilde{r} - \Delta \widetilde{\rho}^e\right) \end{aligned}$$

 Next, follow Dornbusch in assuming that the monetary model only determines the (long-run) equilibrium, not the actual exchange rate:

$$\overline{s} = \widetilde{m} - k\widetilde{y} + l\Delta\widetilde{p}^{e}$$

### Empirical testing: Frankel approach

- The above is a familiar formulation, apart from the last term
- If PPP does not hold, real exchange rates have to diverge: under UIRP real interest rates have to diverge too
- To get an estimable equation combine the above two equations

$$s = \widetilde{m} - k\widetilde{y} + l\Delta\widetilde{p}^{e} - \frac{1}{\Theta}\left(\widetilde{r} - \Delta\widetilde{p}^{e}\right)$$

which clearly shows the role of played by the real interest rate differential  $(\tilde{r}-\Delta\tilde{p}^e)$ 

- If we can find a measure of inflation expectations, we can test the last equation
- Note that as a special case the above equation includes the basic monetary model: if ⊕ increases without bound (ie s = s̄ at all times), then the coefficient on the real interest rate will be zero
- Frankel's evidence suggests that this equations works in the 1970's (for DM/\$ exchange rate)
- Since 1980's in particular, the model fails on exchange rate data