

Answer all five questions (in English, Finnish, or Swedish).

- Describe the field-oriented control system of permanent-magnet synchronous motors. Draw also the block diagram of the control system, label the signals in the diagram, and describe the tasks of the blocks.

Solution:

See lectures and readings.

- Answer briefly to the following questions:
 - Why a speed reduction gear is often used in electric drives?
 - Why three-phase machines are preferred to single-phase AC machines?
 - What is the operating principle of a synchronous reluctance motor?

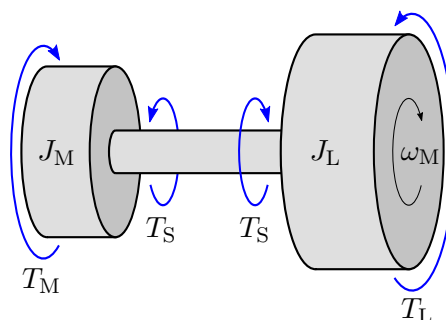
Solution:

See lectures, exercises, and readings.

- A shaft torque sensor is mounted between a motor shaft and a load shaft. The load torque is constant $T_L = 300$ Nm and the load inertia is $J_L = 0.8$ kgm². The motor inertia is $J_M = 0.4$ kgm².
 - The rotor speed $\omega_M = 100$ rad/s is kept constant. What is the electromagnetic torque T_M in this condition? What is the torque sensor reading?
 - The speed is decreased from $\omega_M = 100$ rad/s to zero in 0.5 s with a constant angular acceleration. What is the electromagnetic torque T_M during the deceleration? What is the torque sensor reading?

Solution:

The system is illustrated in the figure below.



- The shaft torque at constant speed equals the electromagnetic torque:

$$T_S = T_M = T_L = 300 \text{ Nm}$$

- (b) The shaft is assumed to be rigid. The total inertia is $J = J_M + J_L = 1.2 \text{ kgm}^2$. The angular acceleration is

$$\alpha_M = \frac{d\omega_M}{dt} = -\frac{100 \text{ rad/s}}{0.5 \text{ s}} = -200.0 \text{ rad/s}^2$$

During the deceleration, the torque produced by the motor is

$$T_M = J\alpha_M + T_L = (-1.2 \cdot 200 + 300) \text{ Nm} = 60 \text{ Nm}$$

On the other hand, the torque sensor measures the shaft torque, which is

$$T_S = T_M - J_M\alpha_M = (60 + 0.4 \cdot 200) \text{ Nm} = 140 \text{ Nm}$$

Alternatively, the shaft torque can be calculated from the load side as

$$T_S = T_L + J_L\alpha_M = (300 - 0.8 \cdot 200) \text{ Nm} = 140 \text{ Nm}$$

4. A DC motor with a separately excited field winding is considered. The rated armature voltage is $U_N = 500 \text{ V}$, rated torque $T_N = 220 \text{ Nm}$, rated speed $n_N = 1600 \text{ r/min}$, and maximum speed $n_{\max} = 3200 \text{ r/min}$. The losses are omitted.
- The flux factor k_f is kept constant at its rated value. When the armature voltage is varied from 0 to U_N , the speed varies from 0 to n_N . Determine the rated armature current I_N .
 - A load is to be driven in the speed range from n_N to n_{\max} by weakening the flux factor while the armature voltage is kept constant at U_N . Determine the torque available at maximum speed, if the rated armature current I_N is not exceeded.
 - Sketch the armature voltage U_a , flux factor k_f , torque T_M , and mechanical power P_M as a function of the speed, when the armature current is kept at I_N . Clearly label axes of your graph.

Solution:

The losses are omitted, i.e., $R_a = 0$ holds. Hence, the steady-state equations of the DC motor are

$$U_a = k_f\omega_M \quad T_M = k_f I_a \quad P_M = T_M\omega_M = U_a I_a$$

- (a) Let us first calculate the rated rotor speed in radians per second:

$$\omega_N = 2\pi n_N = 2\pi \cdot \frac{1600 \text{ r/min}}{60 \text{ s/min}} = 167.6 \text{ rad/s}$$

The rated flux factor is

$$k_{fN} = \frac{U_N}{\omega_N} = \frac{500 \text{ V}}{167.6 \text{ rad/s}} = 2.98 \text{ Vs}$$

The rated armature current is

$$I_N = \frac{T_N}{k_{fN}} = \frac{220 \text{ Nm}}{2.98 \text{ Vs}} = 73.8 \text{ A}$$

(b) The maximum rotor speed in radians per second is

$$\omega_{\max} = 2\pi n_{\max} = 2\pi \cdot \frac{3200 \text{ r/min}}{60 \text{ s/min}} = 335.1 \text{ rad/s}$$

The flux factor at the maximum speed is

$$k_f = \frac{U_N}{\omega_{\max}} = \frac{500 \text{ V}}{335.1 \text{ rad/s}} = 1.49 \text{ Vs}$$

The torque at the maximum speed is

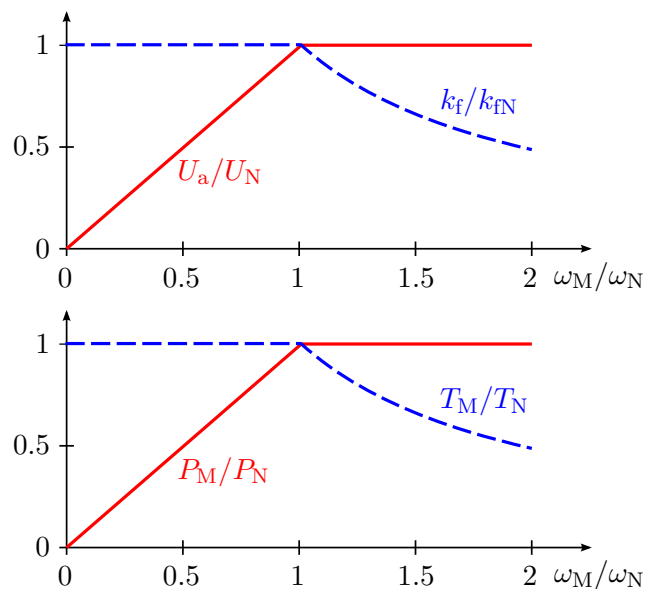
$$T_M = k_f I_N = 1.49 \text{ Vs} \cdot 73.8 \text{ A} = 110 \text{ Nm}$$

The same result could be obtained as $T_M = (n_N/n_{\max})T_N$, i.e. the torque reduces inversely proportionally to the speed in the field-weakening region.

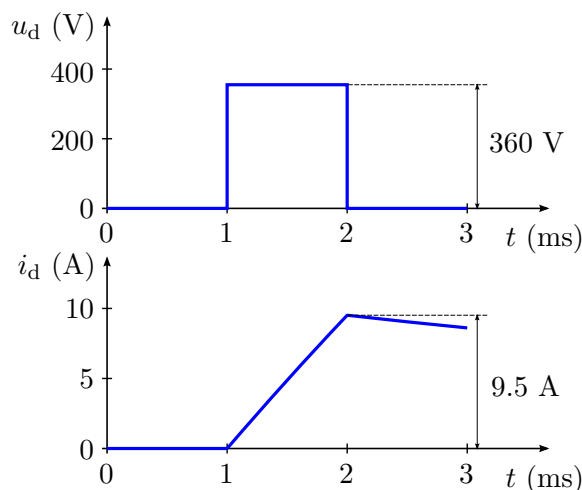
(c) The requested characteristics are shown in the figure below.

Based on $U_a = k_f \omega_M$, the armature voltage increases linearly with the rotor speed until the rated (maximum) voltage U_N is reached at the rated speed. In order to reach higher speeds, the flux factor k_f has to be reduced inversely proportionally to the speed.

Since $I_a = I_N$ is constant, the torque $T_M = k_f I_a$ follows the characteristics of the flux factor k_f . Based on $P_M = T_M \omega_M$, the mechanical power $P_M = T_M \omega_M$ increases linearly with the speed until the rated speed and remains constant at speeds higher than the rated speed. It is important to notice the same mechanical power is obtained also using the electrical quantities, $P_M = U_a I_a$, since the losses are omitted.



5. Consider an inverter-fed three-phase permanent-magnet synchronous motor, whose rated speed is 1 500 r/min and number of pole pairs is $p = 3$. The motor parameters are determined using the following three tests:
- The rotor speed is zero. The constant current vector $\underline{i}_s = i_d = 5.0$ A is fed into the stator winding by means of closed-loop current control. In this steady-state condition, the voltage vector is $\underline{u}_s = u_d = 18.0$ V according to the inverter control algorithm. Determine the stator resistance R_s .
 - The rotor speed is zero also in this test. The inverter produces a 1-ms 360-V voltage pulse along the d-axis, as shown in the figure below, while the q-axis voltage is kept at zero. The measured d-axis current response is also shown in the figure. Determine the stator inductance L_s based on this test (you may assume $R_s = 0$). What is the torque produced by the motor during this test?
 - The motor is controlled to rotate at the speed of 1 200 r/min in a no-load condition. The line-to-line rms voltage of 253.9 V is supplied by the inverter. Determine the PM flux linkage ψ_f .



Solution:

In rotor coordinates, the stator voltage and the flux linkage are

$$\underline{u}_s = R_s \underline{i}_s + \frac{d\underline{\psi}_s}{dt} + j\omega_m \underline{\psi}_s \quad (1)$$

$$\underline{\psi}_s = L_s \underline{i}_s + \underline{\psi}_f \quad (2)$$

respectively. The parameters R_s , L_s , and ψ_f are determined using the three tests.

- This test is carried out in the steady state at zero speed, i.e., $d/dt = 0$ and $\omega_m = 0$ hold. Hence, the stator resistance is simply

$$R_s = \underline{u}_s / \underline{i}_s = 18.0 \text{ V} / 5.0 \text{ A} = 3.6 \Omega$$

- The second test is also carried out at zero speed, $\omega_m = 0$. Inserting (2) into (1) and taking the real part yields the d-axis voltage is

$$u_d = R_s i_d + L_s \frac{di_d}{dt} \quad (3)$$

where $d\psi_f/dt = 0$ since ψ_f is constant. Assuming $R_s = 0$, an approximate value for the stator inductance is obtained:

$$L_d = u_d \frac{\Delta t}{\Delta i_d} = \frac{360 \text{ V} \cdot 1 \text{ ms}}{9.5 \text{ A}} = 38 \text{ mH}$$

The torque expression is

$$T_M = \frac{3p}{2} \text{Im} \left\{ \underline{i}_s \underline{\psi}_s^* \right\} = \frac{3p}{2} \psi_f i_q$$

Since the q-axis current is zero during the test, no torque is produced.

Remark: The exact value was not asked, but it could be obtained using the step response of (3):

$$i_d(t) = i_{d\infty} (1 - e^{-t/\tau_d}) \quad (4)$$

where $i_{d\infty} = u_d/R_s = 360 \text{ V}/3.6 \text{ } \Omega = 100 \text{ A}$ and $\tau_d = L_d/R_s$. From (4), the inductance L_d can be solved as

$$L_d = -\frac{t}{\ln[1 - i_d(t)/i_{d\infty}]} R_s = -\frac{1 \text{ ms}}{\ln(1 - 9.5/100)} \cdot 3.6 \text{ } \Omega = 36 \text{ mH}$$

For practical purposes, the approximate value is close to the exact value.

(c) During this test, the electrical angular speed of the rotor is

$$\omega_m = p\omega_M = 3 \cdot 2\pi \cdot \frac{1 \text{ 200 r/min}}{60 \text{ s/min}} = 2\pi \cdot 60 \text{ rad/s}$$

At this speed, the line-to-neutral voltage $e_s = \sqrt{2/3} \cdot 253.9 \text{ V} = 207.3 \text{ V}$ is induced in the stator winding. Hence, the PM flux linkage is

$$\psi_f = \frac{e_s}{\omega_m} = \frac{207.3 \text{ V}}{2\pi \cdot 60 \text{ rad/s}} = 0.55 \text{ Vs}$$