

# Lecture 10: Synchronous Motor Drives ELEC-E8402 Control of Electric Drives and Power Converters

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#### **Learning Outcomes**

After this lecture and exercises you will be able to:

- Identify, based on the cross-section of the rotor, if the motor is magnetically anisotropic
- ► Explain what is the reluctance torque
- Calculate operating points of synchronous motors and draw the corresponding vector diagrams
- ► Derive and explain the MTPA control principle

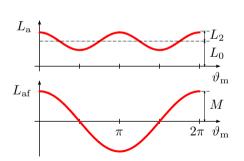
### **Common 3-Phase AC Motor Types**

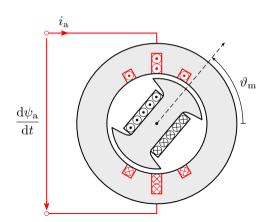
- Asynchronous motors
  - Induction motor with squirrel-cage rotor
  - ► Wound-rotor induction motor
- Synchronous motors
  - Synchronous motor with a field winding
  - ► Surface-mounted permanent-magnet synchronous motor (SPMSM)
  - ► Interior permanent-magnet synchronous motor (IPMSM)
  - ► Reluctance synchronous motor (SyRM)
  - ► Permanent-magnet-assisted SyRM (PM-SyRM)
- ► Same model and similar control can be used for these synchronous motors

### **Recap: Single-Phase Motor**

Assumption: ideal sinusoidal winding distribution

$$\psi_{a} = L_{a}(\vartheta_{m})i_{a} + L_{af}(\vartheta_{m})i_{f} = [L_{0} + L_{2}\cos(2\vartheta_{m})]i_{a} + M\cos(\vartheta_{m})i_{f}$$





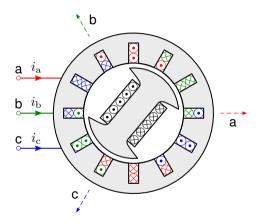
#### **3-Phase Synchronous Motor Model**

**Permanent-Magnet and Reluctance Synchronous Motors** 

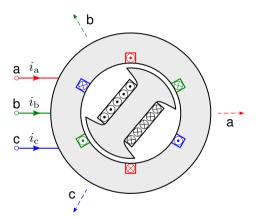
**Control of Synchronous Motors** 

### **3-Phase Synchronous Motor**

Sinusoidal phase windings and constant field-winding current  $\it i_{\rm f}$  will be assumed

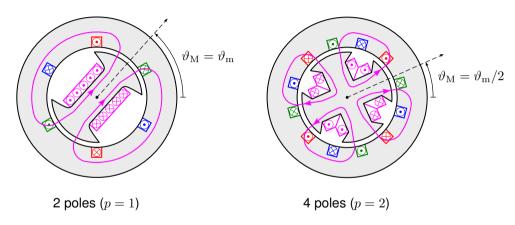


Example of a 3-phase distributed winding (Y or D connection)



Simplified representation will be used in the following

#### **Number of Pole Pairs**



Electrical angular speed  $\omega_{\rm m}=p\,\omega_{\rm M}$  and electrical angle  $\vartheta_{\rm m}=p\,\vartheta_{\rm M}$ 

Note that the stator and the rotor should have the same number of poles. What happens if their pole numbers differ?

#### **Space Vector Transformation**

▶ Instantaneous 3-phase quantities can be transformed to the  $\alpha\beta$  components

$$\begin{bmatrix} i_{\alpha} \\ i_{\beta} \end{bmatrix} = \frac{2}{3} \begin{bmatrix} 1 & -1/2 & -1/2 \\ 0 & \sqrt{3}/2 & -\sqrt{3}/2 \end{bmatrix} \begin{bmatrix} i_{\text{a}} \\ i_{\text{b}} \\ i_{\text{c}} \end{bmatrix}$$

where currents are used as an example

► Equivalently, the complex space vector transformation can be used

$$\underline{i}_{s} = i_{\alpha} + ji_{\beta} = \frac{2}{3} \left( i_{a} + i_{b} e^{j2\pi/3} + i_{c} e^{j4\pi/3} \right)$$

which gives the same components  $i_{\alpha}$  and  $i_{\beta}$ 

 3-phase motor can be modeled as an equivalent 2-phase motor with no loss of information

# **Equivalent 2-Phase Motor**

#### ► Stator flux linkages

$$\begin{bmatrix} \psi_{\alpha} \\ \psi_{\beta} \end{bmatrix} = \begin{bmatrix} L_{\alpha} & L_{\alpha\beta} \\ L_{\beta\alpha} & L_{\beta} \end{bmatrix} \begin{bmatrix} i_{\alpha} \\ i_{\beta} \end{bmatrix} + \begin{bmatrix} L_{\alpha f} \\ L_{\beta f} \end{bmatrix} i_{f}$$

$$L_{\alpha} = L_{0} + L_{2} \cos(2\vartheta_{m})$$

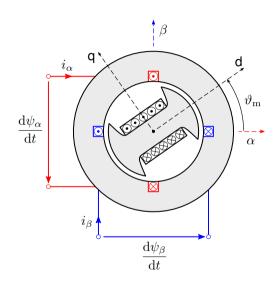
$$L_{\beta} = L_{0} - L_{2} \cos(2\vartheta_{m})$$

$$L_{\alpha\beta} = L_{\beta\alpha} = L_{2} \sin(2\vartheta_{m})$$

$$L_{\alpha f} = M \cos(\vartheta_{m}) \qquad L_{\beta f} = M \sin(\vartheta_{m})$$

#### ► Induced voltages

$$e_{\alpha} = \frac{\mathrm{d}\psi_{\alpha}}{\mathrm{d}t}$$
  $e_{\beta} = \frac{\mathrm{d}\psi_{\beta}}{\mathrm{d}t}$ 



Torque could be derived using the approach described in the previous lecture, but transforming the model to rotor coordinates allows us to use a shortcut, as shown in the following slides.

#### **Transformation to Rotor Coordinates**

lacktriangledown  $\alpha\beta$  components can be transformed to the dq components

$$\begin{bmatrix} i_{\rm d} \\ i_{\rm q} \end{bmatrix} = \begin{bmatrix} \cos(\vartheta_{\rm m}) & \sin(\vartheta_{\rm m}) \\ -\sin(\vartheta_{\rm m}) & \cos(\vartheta_{\rm m}) \end{bmatrix} \begin{bmatrix} i_{\alpha} \\ i_{\beta} \end{bmatrix}$$

Equivalent to the transformation for complex space vectors

$$i_{d} + ji_{q} = \underline{i}_{s} = e^{-j\vartheta_{m}}\underline{i}_{s}^{s}$$

$$= [\cos(\vartheta_{m}) - j\sin(\vartheta_{m})](i_{\alpha} + ji_{\beta})$$

$$= \cos(\vartheta_{m})i_{\alpha} + \sin(\vartheta_{m})i_{\beta} + j[-\sin(\vartheta_{m})i_{\alpha} + \cos(\vartheta_{m})i_{\beta}]$$

Inverse transformation is obtained similarly

#### **Model in Rotor Coordinates**

► Stator flux linkages

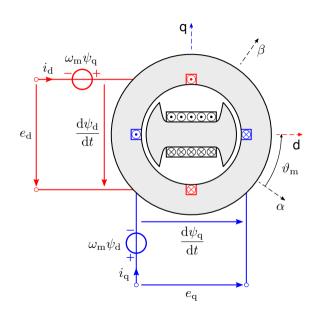
$$\begin{bmatrix} \psi_{\rm d} \\ \psi_{\rm q} \end{bmatrix} = \begin{bmatrix} L_{\rm d} & 0 \\ 0 & L_{\rm q} \end{bmatrix} \begin{bmatrix} i_{\rm d} \\ i_{\rm q} \end{bmatrix} + \begin{bmatrix} L_{\rm d} \\ 0 \end{bmatrix} i_{\rm F}$$

► Inductances are constant

$$L_{\rm d} = L_0 + L_2$$
  $L_{\rm q} = L_0 - L_2$ 

- ► Equivalent field-winding current  $i_F = (M/L_d)i_f$
- ► Induced voltages

$$e_{\rm d} = \frac{\mathrm{d}\psi_{\rm d}}{\mathrm{d}t} - \omega_{\rm m}\psi_{\rm q} \qquad e_{\rm q} = \frac{\mathrm{d}\psi_{\rm q}}{\mathrm{d}t} + \omega_{\rm m}\psi_{\rm d}$$



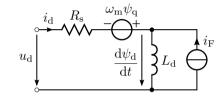
- Model can be expressed using space vectors
- ► Stator flux linkage

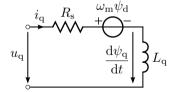
$$\underline{\psi}_{\rm s} = L_{\rm d}i_{\rm d} + \psi_{\rm F} + jL_{\rm q}i_{\rm q}$$

where  $\psi_{\rm F} = L_{\rm d} i_{\rm F}$ 

► Stator voltage

$$\underline{u}_{s} = R_{s}\underline{i}_{s} + \frac{d\underline{\psi}_{s}}{dt} + j\omega_{m}\underline{\psi}_{s}$$





Alternatively, space vectors could be represented using real-valued column vectors, e.g.,  $i_s = [i_d, i_q]^T$  instead of  $\underline{i_s} = i_d + ji_q$ . Real-valued vectors would allow expressing the flux linkage equation in a more convenient form.

#### **Power Balance**

$$\frac{3}{2}\operatorname{Re}\left\{\underline{u}_{s}\underline{i}_{s}^{*}\right\} = \frac{3}{2}R_{s}|\underline{i}_{s}|^{2} + \frac{3}{2}\operatorname{Re}\left\{\frac{d\underline{\psi}_{s}}{dt}\underline{i}_{s}^{*}\right\} + T_{M}\frac{\omega_{m}}{p}$$

Electromagnetic torque

$$T_{\rm M} = \frac{3p}{2} \operatorname{Im} \left\{ \underline{i}_{\rm s} \underline{\psi}_{\rm s}^* \right\} = \frac{3p}{2} \left[ \psi_{\rm F} + (L_{\rm d} - L_{\rm q}) i_{\rm d} \right] i_{\rm q}$$

Rate of change of the magnetic field energy

$$\operatorname{Re}\left\{\frac{\mathrm{d}\underline{\psi}_{\mathrm{s}}}{\mathrm{d}t}\underline{i}_{\mathrm{s}}^{*}\right\} = \frac{\mathrm{d}}{\mathrm{d}t}\left(\frac{1}{2}L_{\mathrm{d}}i_{\mathrm{d}}^{2} + \frac{1}{2}L_{\mathrm{q}}i_{\mathrm{q}}^{2}\right)$$

► This model is valid also for other synchronous motors

# Model in a Block Diagram Form

► Magnetic model is obtained from the flux linkage equation

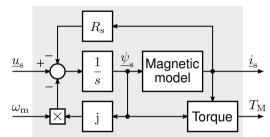
$$\underline{i}_{\rm s} = \frac{\psi_{\rm d} - \psi_{\rm F}}{L_{\rm d}} + \mathrm{j}\frac{\psi_{\rm q}}{L_{\rm q}}$$

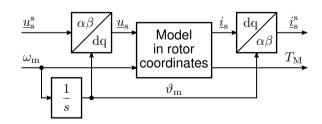
► If needed, magnetic saturation could be modeled in a form

$$\underline{i}_{\mathrm{s}} = i_{\mathrm{d}}(\psi_{\mathrm{d}}, \psi_{\mathrm{q}}) + \mathrm{j} i_{\mathrm{q}}(\psi_{\mathrm{d}}, \psi_{\mathrm{q}})$$

• Mechanical subsystem closes the loop from  $T_{\rm M}$  to  $\omega_{\rm m}$  (not shown)

#### Model in rotor coordinates

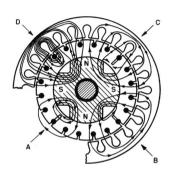




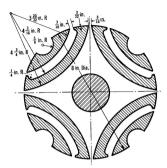
**3-Phase Synchronous Motor Model** 

#### **Permanent-Magnet and Reluctance Synchronous Motors**

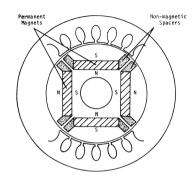
**Control of Synchronous Motors** 



PM synchronous motor (with a damping cage)<sup>1</sup>



Reluctance synchronous motor<sup>2</sup>

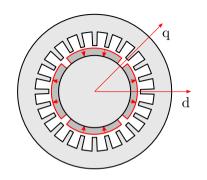


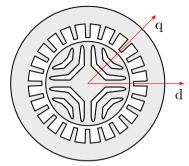
Interior PM synchronous motor<sup>3</sup>

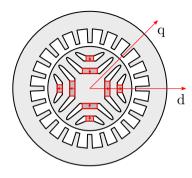
<sup>&</sup>lt;sup>1</sup>Merrill, "Permanent-magnet excited synchronous motors," AIEE Trans., 1955.

<sup>&</sup>lt;sup>2</sup>Kostko, "Polyphase reaction synchronous motors," J. AIEE, 1923.

<sup>&</sup>lt;sup>3</sup> Jahns, Kliman, and Neumann, "Interior permanent-magnet synchronous motors for adjustable-speed drives," IEEE Trans. Ind. Appl., 1986.







Surface-mounted PM synchronous motor

$$L_{\rm d}=L_{\rm g},\,\psi_{\rm F}={\sf const}$$

Reluctance synchronous motor

$$L_{\rm d} > L_{\rm q}$$
,  $\psi_{\rm F} = 0$ 

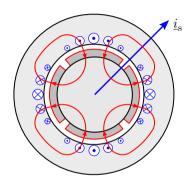
Interior PM synchronous motor

$$L_{\rm q} > L_{\rm d}$$
,  $\psi_{\rm F} = {\rm const}$ 

Permeability of PMs ( $\mu_{\rm r} \approx$  1.05) almost equals the permeability of air ( $\mu_{\rm r} \approx$  1)

## **Surface-Mounted PM Synchronous Motor (SPMSM)**

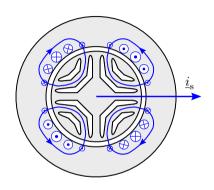
- Either distributed or concentrated
   3-phase stator winding
- Rare-earth magnets (NdFeB or SmCo) mounted at the rotor surface
- ► High efficiency (or power density)
- ► Limited field-weakening range
- Expensive due to the magnets and manufacturing process
- ► Typical motor type in servo drives



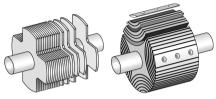
What are the current components  $i_{\rm d}$  and  $i_{\rm q}$  in the figure?

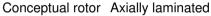
## Reluctance Synchronous Motor (SyRM)

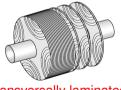
- Distributed 3-phase stator winding
- ► Transversally laminated rotor
- lacktriangle Flux barriers are shaped to maximize  $L_{
  m d}/L_{
  m q}$
- Rotor tries to find its way to the position that minimizes the magnetic field energy
- ► Cheaper than PM motors
- More efficient than induction motors
- ► Poor power factor (means a larger inverter)
- Magnetic saturation has to be taken into account in control
- ► Competitor to induction motors



What is the electromagnetic torque in the figure?



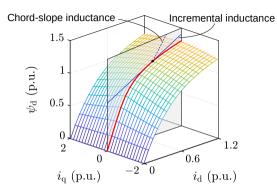


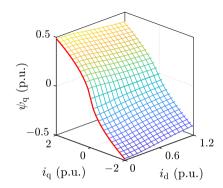






Figures: (left) Fukami, Momiyama, Shima, et al., "Steady-state analysis of a dual-winding reluctance generator with a multiple-barrier rotor," IEEE Trans. Energy Conv., 2008; (right) ABB.





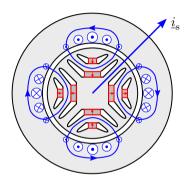
- ► Magnetic model of a 6.7-kW motor shown as an example
- ► Can be measured at constant speed<sup>4</sup> or identified at standstill<sup>5</sup>

<sup>&</sup>lt;sup>4</sup>Armando, Bojoi, Guqlielmi, et al., "Experimental identification of the magnetic model of synchronous machines," IEEE Trans. Ind. Appl., 2013.

<sup>&</sup>lt;sup>5</sup>Hinkkanen, Pescetto, Mölsä, *et al.*, "Sensorless self-commissioning of synchronous reluctance motors at standstill without rotor locking," *IEEE Trans. Ind. Appl.*, 2017.

### **Interior PM Synchronous Motors (IPMSM)**

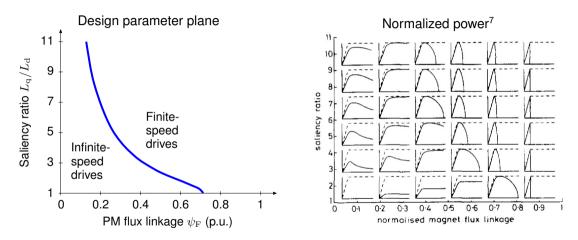
- Reluctance synchronous motor can be improved by placing either rare-earth or ferrite magnets inside the flux barriers
- Magnets improve the power factor and contribute to the torque
- ► Excellent field-weakening performance
- Minor risk of overvoltages due to the low back-emf induced by the magnets
- ► If the reluctance torque dominates, these motors are called PM-assisted reluctance synchronous motors (PM-SyRM)<sup>6</sup>



What is the reluctance torque in the figure?

<sup>&</sup>lt;sup>6</sup>Guglielmi, Pastorelli, Pellegrino, et al., "Position-sensorless control of permanent-magnet-assisted synchronous reluctance motor," *IEEE Trans. Ind. Appl.*, 2004.

#### Optimal field-weakening design criterion $\psi_F = L_d i_N$ , where $i_N$ is the rated current

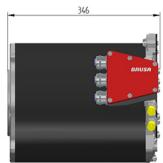


<sup>&</sup>lt;sup>7</sup>Soong and Miller, "Field-weakening performance of brushless synchronous ac motor drives," *IEE Proc. EPA*, 1994.

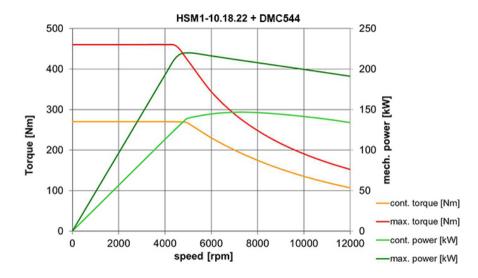
#### Example: Brusa HSM1-10.18.22

- ► For truck and bus applications
- ► Low magnetic material
- ► IPMSM or PM-SyRM?

- ► Speed: 4400 r/min (nom), 12000 r/min (max)
- ► Torque: 270 Nm (S1), 460 Nm (max)
- ► Power: 145 kW (S1), 220 kW (max)
- ► DC-bus voltage: 400 V
- ► Weight: 76 kg







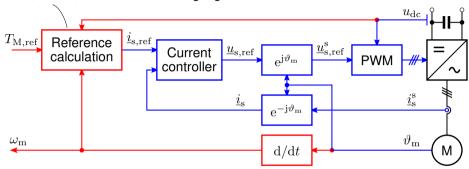
**3-Phase Synchronous Motor Model** 

**Permanent-Magnet and Reluctance Synchronous Motors** 

**Control of Synchronous Motors** 

### **Typical Vector Control System**

MTPA, MTPV, and field-weakening algorithms



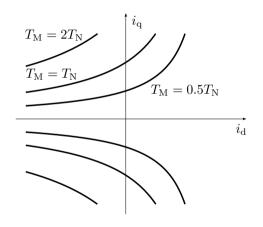
- ► Fast current-control loop
- ▶ Rotor position  $\vartheta_{\rm m}$  is measured (or estimated)
- ightharpoonup Current reference  $\underline{i}_{s,ref}$  is calculated in rotor coordinates
- Control of PM and reluctance synchronous motors will be considered

# **Constant Torque Loci in the Current Plane**

 Same torque can be produced with different current components

$$T_{\rm M} = \frac{3p}{2} \left[ \psi_{\rm F} + (\underline{L_{\rm d}} - \underline{L_{\rm q}}) i_{\rm d} \right] i_{\rm q}$$

- ▶ IPMSM ( $L_{\rm q}/L_{\rm d}=1.7$  and  $\psi_{\rm F}=0.7$  p.u.) is used as an example motor
- ► How are the loci for  $L_{\rm d} = L_{\rm q}$  (SPMSM) and for  $\psi_{\rm F} = 0$  (SyRM)?
- ► How to choose  $i_d$  and  $i_q$ ?



# **Current and Voltage Limits**

Maximum current

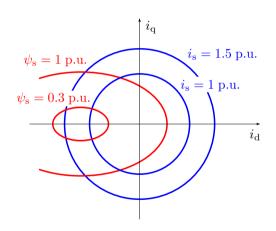
$$i_{\mathrm{s}} = \sqrt{i_{\mathrm{d}}^2 + i_{\mathrm{q}}^2} \le i_{\mathrm{max}}$$

► Maximum flux linkage

$$\psi_{\rm s} = \sqrt{\psi_{\rm d}^2 + \psi_{\rm q}^2} \le \frac{u_{\rm max}}{|\omega_{\rm m}|}$$

where

$$\psi_{\rm d} = L_{\rm d}i_{\rm d} + \psi_{\rm F}$$
$$\psi_{\rm q} = L_{\rm q}i_{\rm q}$$



#### **Control Principle**

- ► Goal is to produce the requested torque at minimum losses and to maximize available torque for the given drive capacity ( $i_{max}$  and  $u_{max}$ )
- Speeds below the base speed
  - ► Maximum torque per ampere (MTPA) locus minimizes the copper losses
- Higher speeds
  - ► MTPA locus cannot be used due to the limited voltage
  - lacktriangle To reach higher speeds, the flux linkage  $\psi_{
    m s}$  has to be reduced by negative  $i_{
    m d}$
  - ► Maximum torque per volt (MTPV) limit has to be taken into account

# **Maximum Torque per Ampere (MTPA)**

- lacktriangle Current magnitude  $i_{
  m s}=\sqrt{i_{
  m d}^2+i_{
  m q}^2}$
- ► Torque is expressed as

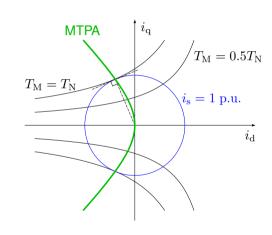
$$T_{\rm M} = \frac{3p}{2} \left[ \psi_{\rm F} + (L_{\rm d} - L_{\rm q}) i_{\rm d} \right] \sqrt{i_{\rm s}^2 - i_{\rm d}^2}$$

lacktriangle Maximum torque at  $\partial T_{\mathrm{M}}/\partial i_{\mathrm{d}}=0$ 

$$i_{\rm d}^2 + i_{\rm d} \frac{\psi_{\rm F}}{L_{\rm d} - L_{\rm g}} - i_{\rm q}^2 = 0$$

► Special cases

$$i_{
m d}=0$$
 for  $L_{
m d}=L_{
m q}$  (SPMSM)  $|i_{
m d}|=|i_{
m q}|$  for  $\psi_{
m F}=0$  (SyRM)



## **Maximum Torque per Volt (MTPV)**

► Flux magnitude

$$\psi_{\rm s} = \sqrt{(\psi_{\rm F} + L_{\rm d}i_{\rm d})^2 + (L_{\rm q}i_{\rm q})^2}$$

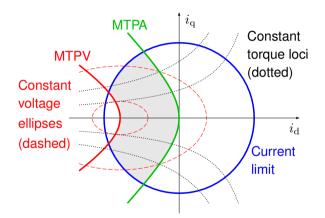
► MTPV condition can be derived similarly as the MTPA condition

$$(\psi_{\rm F} + L_{\rm d}i_{\rm d})^2 + \frac{L_{\rm q}}{L_{\rm d} - L_{\rm q}}\psi_{\rm f}(\psi_{\rm F} + L_{\rm d}i_{\rm d}) - (L_{\rm q}i_{\rm q})^2 = 0$$

► Special cases

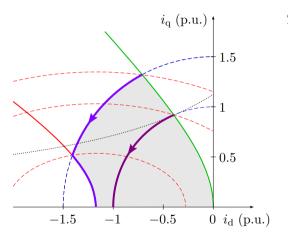
$$i_{
m d}=-\psi_{
m F}/L_{
m d}$$
 for  $L_{
m d}=L_{
m q}$  (SPMSM)  $|\psi_{
m d}|=|\psi_{
m q}|$  for  $\psi_{
m F}=0$  (SyRM)

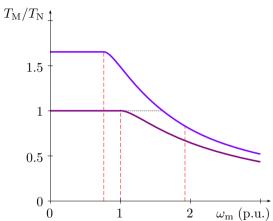
### Feasible Operating Area<sup>8</sup>

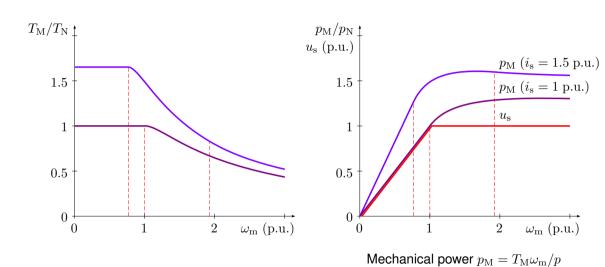


<sup>&</sup>lt;sup>8</sup>Morimoto, Takeda, Hirasa, et al., "Expansion of operating limits for permanent magnet motor by current vector control considering inverter capacity," *IEEE Trans. Ind. Appl.*, 1990.

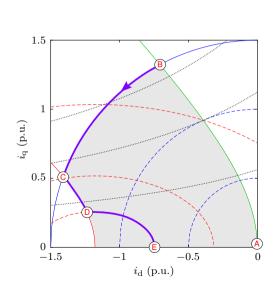
# Example: Acceleration Loci for $i_{max} = 1$ p.u. and $i_{max} = 1.5$ p.u.

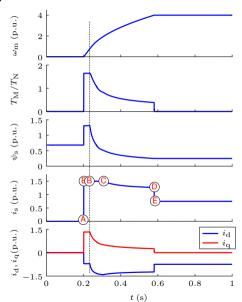




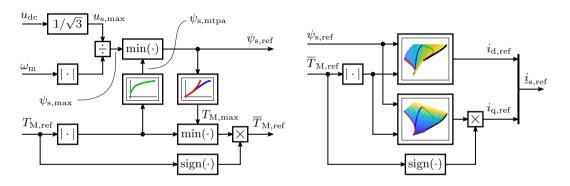


# **Example: Time-Domain Waveforms**





#### Feedforward Reference Calculation Method<sup>9,10</sup>



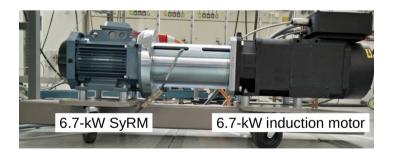
- Control lookup tables numerically solved from the magnetic model
- Other control structures and control variables are possible

<sup>&</sup>lt;sup>9</sup>Meyer and Böcker, "Optimum control for interior permanent magnet synchronous motors (IPMSM) in constant torque and flux weakening range," in *Proc. EPE-PEMC*, 2006.

<sup>10</sup> Awan, Song, Saarakkala, et al., "Optimal torque control of saturated synchronous motors: Plug-and-play method," IEEE Trans. Ind. Appl., 2018.

#### **Experimental Results: 6.7-kW SyRM**

- ► Rated values: 3175 r/min; 105.8 Hz; 370 V; 15.5 A
- Sampling and switching frequency 5 kHz
- ► Current-control bandwidth 500 Hz
- ► Flux linkages used as state variables in the current controller<sup>11</sup>



<sup>11</sup> Awan, Saarakkala, and Hinkkanen, "Flux-linkage-based current control of saturated synchronous motors," IEEE Trans. Ind. Appl., 2019.

- ► Acceleration to 2 p.u. (212 Hz)
- ► Control takes the magnetic saturation into account
- ► Saturation affects significantly the optimal current components

