

# Mathematics for Economists

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Recap of Part II

# Review - Constrained Optimization

Optimization problems with equality constraints:

- ▶ NDCQ
- ▶ first order necessary conditions
- ▶ second order sufficient conditions for local extrema

Optimization problems with inequality constraints

- ▶ NDCQ, first order necessary conditions
- ▶ necessary and sufficient conditions for concave problems

## Review - Constrained Optimization

- ▶ Optimization problems with mixed constraints: NDCQ, first order necessary conditions
- ▶ Envelope theorems for unconstrained problems and constrained problems with equality or inequality constraints
  - ▶ interpretation of Lagrange multipliers

## Review - Difference equations

- ▶ First order linear difference equations with constant coefficients: General solution and stability
- ▶ Eigenvalues, eigenvectors and generalized eigenvectors
- ▶ Systems of linear difference equations: General solution (real eigenvalues) and stability

## Review - Differential equations

- ▶ First order ordinary differential equations: Linear equations with constant coefficients
- ▶ Linear second order differential equations with constant coefficients: General solution and stability
- ▶ Stability of autonomous first order equations, phase portraits
- ▶ First order linear systems of differential equations: General solution and stability
- ▶ Stability of autonomous first order systems

## Book chapters

- ▶ Optimization: chapters 18-19
- ▶ Eigenvalues, difference and differential equations: chapters 23-25
- ▶ note: in exam there will be no questions on topics not covered in the lecture and exercise material