



Aalto University
School of Arts, Design
and Architecture

MAR-E1004 Basics of GIS: From points to surfaces

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Slides adopted from Kirsi Virrantaus, Paula Ahonen-Rainio & Salla Multimäki

Learning goals

In this session you will learn

From surfaces to points

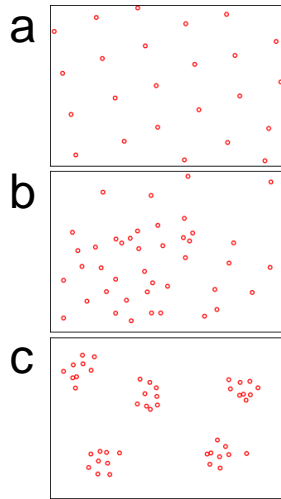
Simple: Use overlay with polygons or Sample tool (Spatial Analyst Tools -> Extraction -> Sample) with raster.

From a set of points to a surface

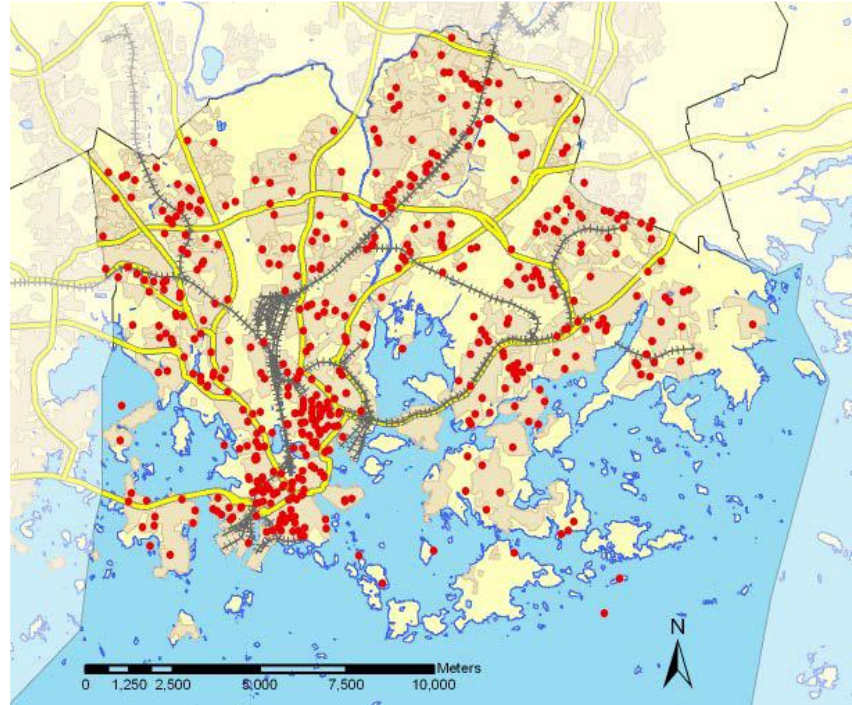
- **Density surface**
 - Kernel density

- **Spatial interpolation**
 - Thiessen polygons (cf. Voronoi diagram)
 - IDW
 - TIN

Case: Incidents of domestic fire in Helsinki

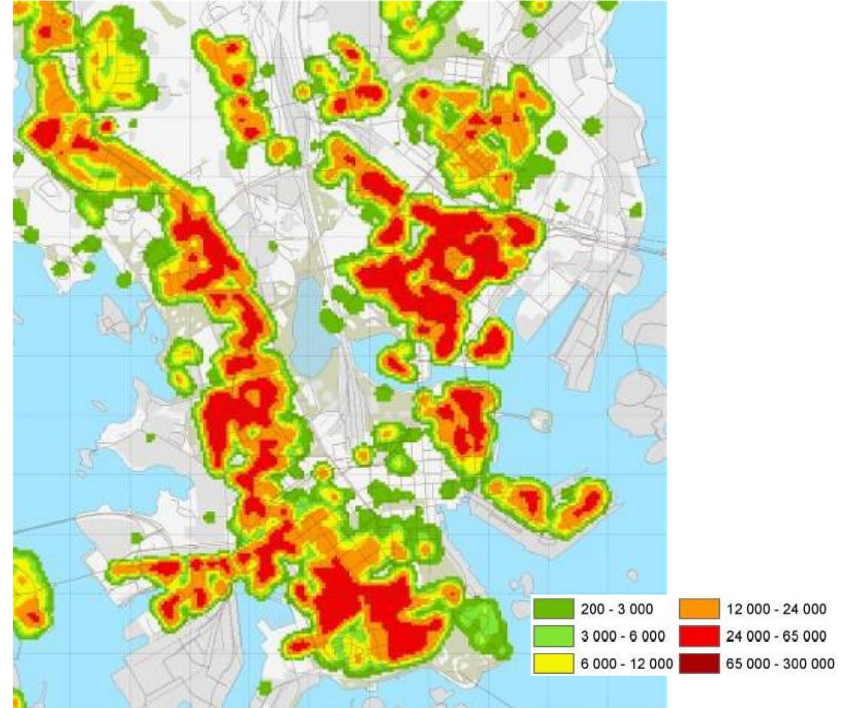
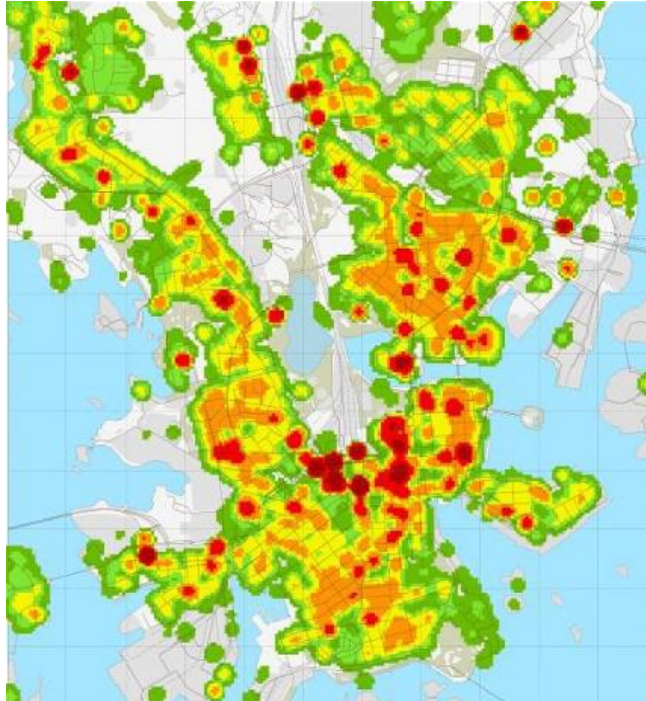


The distribution of the events is not regular (a) nor random (b)



Spatenkova 2009

Case: Incidents of domestic fire in Helsinki



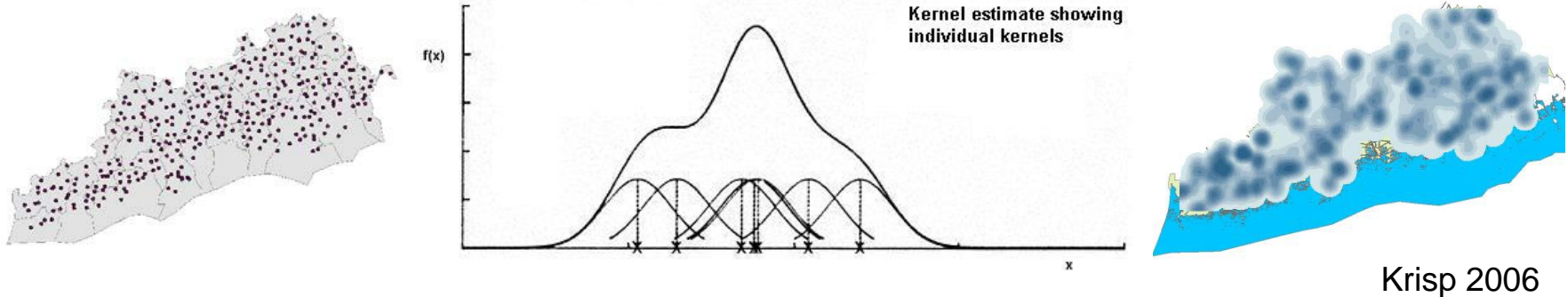
Spatenkova 2009

Kernel density estimation

- **Transformation from point objects to a density surface to visualize a point pattern to detect hot spots where the local density is estimated to be high**
- **to allow comparison of point data with a surface variable**
- **Density at any location in the study area**
 - estimated by counting the number of objects (or events) in a region (=kernel) centered at the location p where the estimate is made
- **Simple kernel: circle centered at the location p**
- **More sophisticated: a kernel function weighting nearby events**
- **Complexity: density is scale-dependent! (cf. kernel bandwidth)**

Kernel density surface

- **Kernel function (e.g., bell shape) for the local density**
 - Each point is replaced by a kernel
 - Density surface is the sum of these



Kernel density surface

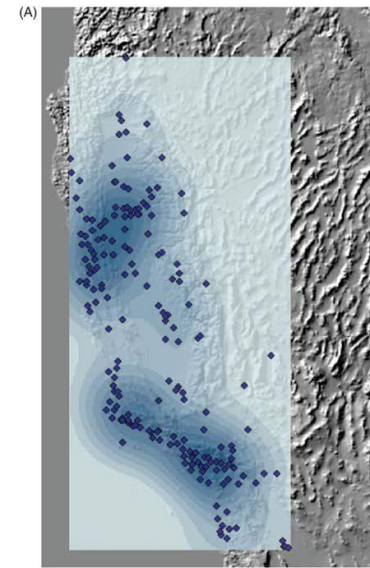
Kernel *bandwidth* affects the resulting density surface

- Large bandwidth results to smooth variation, densities get close to the global average across the study area
- Small bandwidth results to surface pattern focusing strongly to individual events and zero densities between remote events

Example: Density estimation using two different distance parameters in the respective kernel functions.

(A) the surface shows the density of ozone-monitoring stations in California, using a kernel radius of 150 km

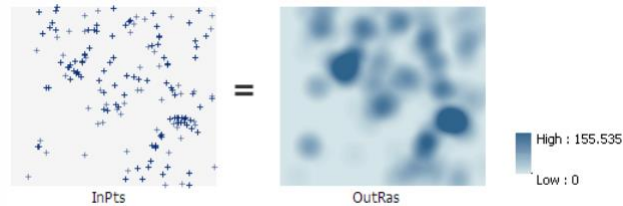
(B) zoomed to an area of Southern California, a kernel radius of 16 km is too small for this dataset, as it leaves each kernel isolated from its neighbors



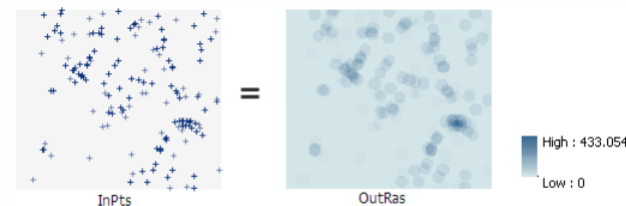
Longley et al.
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Kernel density in ArcMap

- Use the fire and rescue mission dataset from session 2 (prontodata)
- Analyze the density of these missions in Helsinki using Kernel and Point Density tools in Spatial Analyst Tools -> Density



OutRas = KernelDensity(InPts, None, 30)



OutRas = PointDensity(InPts, None, 30)

Density surface and spatial interpolation

Density surface estimates the variation of the density of discrete events (events = point objects)

- Population of known cities

Spatial interpolation predicts the values of a spatially continuous variable at unsampled locations from the measurements (known values) made at control points (sample points) in the same area

- Temperature in measurement points

Spatial interpolation

Values of a field measured at a number of sample points

⇒ need to estimate the continuous field

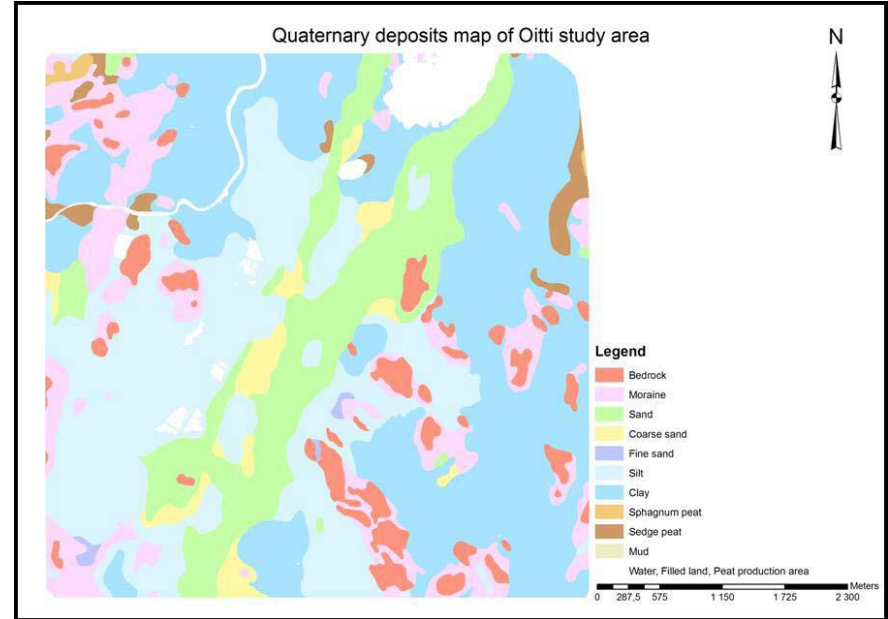
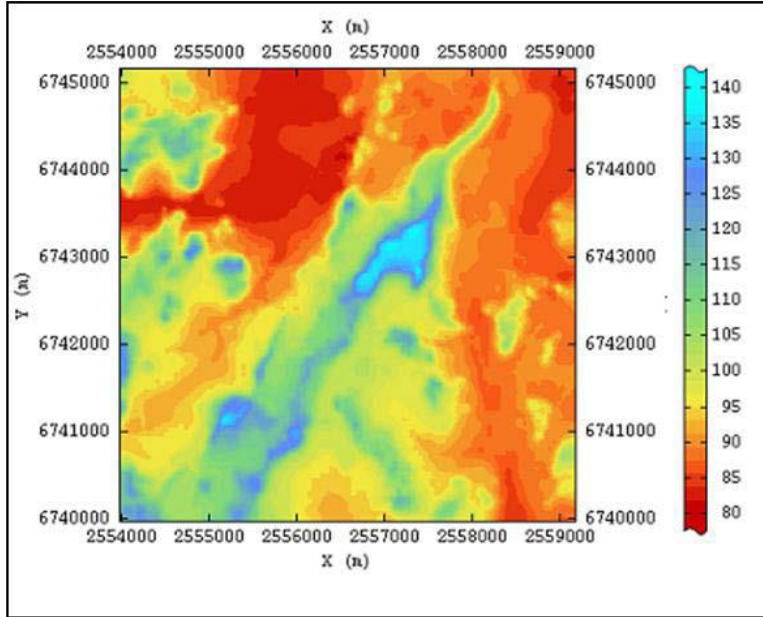
i.e. values at points where the field was not measured (points to be estimated)

Interpolation is not possible without positive spatial autocorrelation: locations close to each other are more similar than locations far away

Which method?

- Characteristics of the represented phenomenon
- Continuous or categorized values

Continuous or categorical data



Sunila 2009

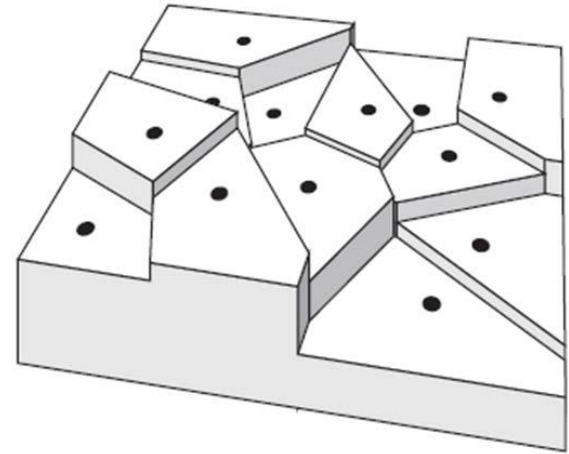
Methods for spatial interpolation

- **Thiessen polygons: nearest value method**
- **TIN model: linear interpolation on the planes of triangles**
- **IDW: Inverse distance weighted spatial average**

Thiessen polygons

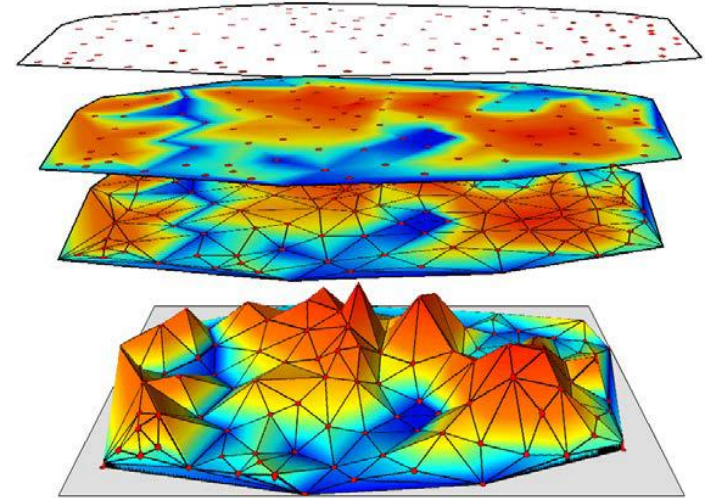
Every unsampled point gets the value of its nearest control point

- **Proximity polygon of a [control] point: that region of the space which is closer to this point than any other**
- **Abrupt changes in adjacent polygons**
 - May suit well for some phenomena, and not at all for others
 - The approach is quite obvious when visualized; no wrong expectations of the accuracy
- **Useful for nominal data**
 - But may not be considered interpolation in these cases (rather a transformation)



TIN represents the surface *per se*

- **Sample points are connected to form triangles**
- **The field inside each triangle is represented as a plane**
- The value of the variable (i.e. the field) at any location p inside the triangle can be calculated from the values at the vertices and the distances from the location p to the vertices



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Inverse distance weighted spatial average = IDW

Nearer locations are considered more prominent

-> the values of sample points around the point to be interpolated are weighted according to the inverse distance

- for example, $w=1/d^2$ (decreases the effect of more distance points)
- weights at any interpolated point shall sum to 1