

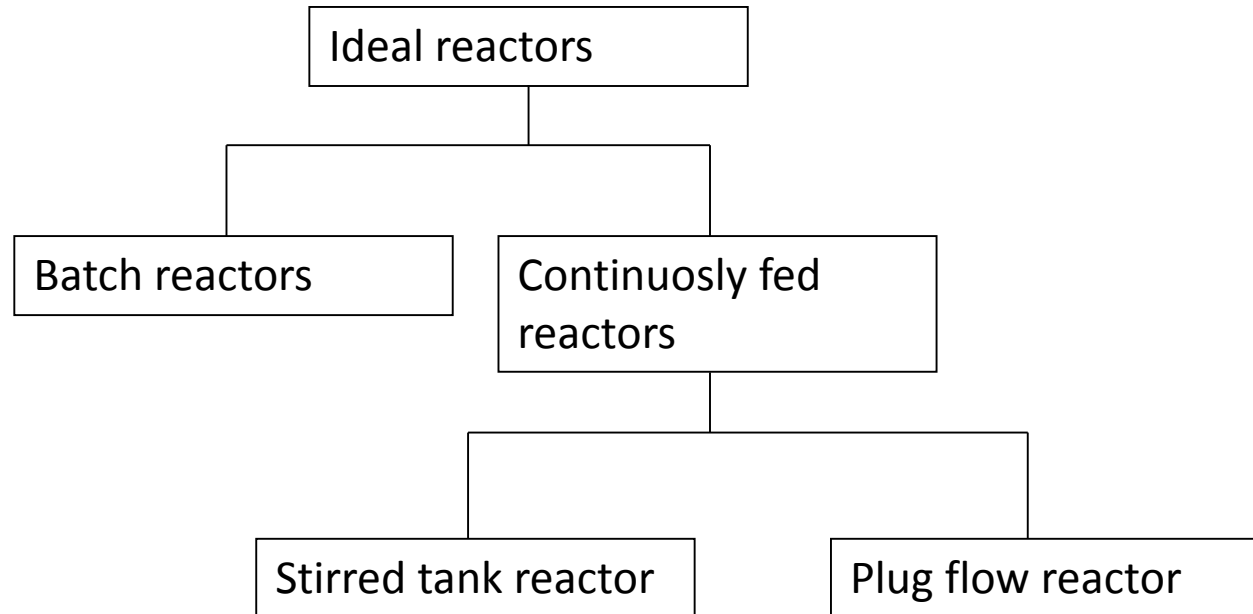
# Reactors

WAT-E2120 Physical and Chemical Treatment of Water and Waste

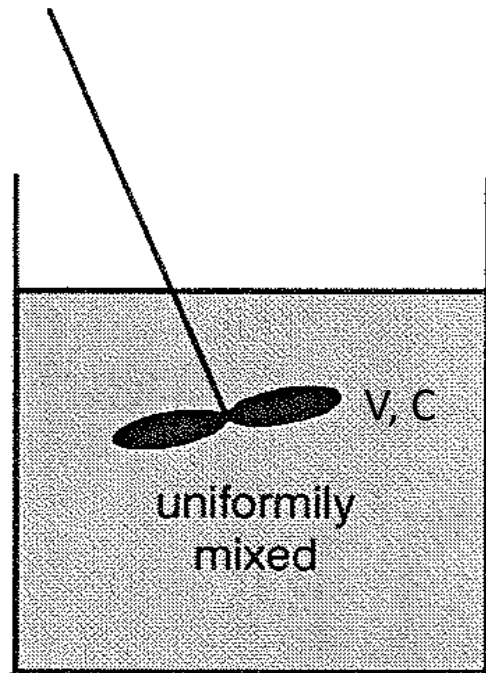
Pirjo Rantanen Lic. Tech.

Aalto University

# Designing reactors



# Batch reactor



- The reaction is let run until the desired yield is reached
- No flow in or out
- => The end products are available only after the reaction time is finished
- For a constant volume V:

$$V \frac{dC}{dt} = V r_c$$

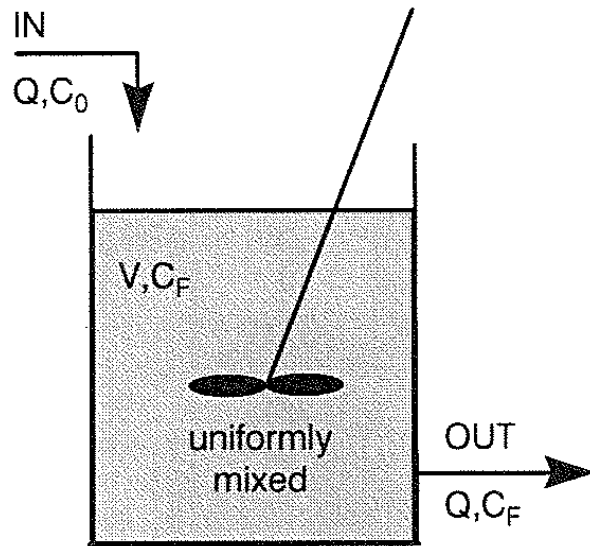
$$\frac{dC}{dt} = r_c$$

for a first-order reaction where C is consumed from an initial concentration of  $C_0$ :

$$r_c = -kC$$

Integrated form with solved concentration by time:  $C = C_0 \exp(-kt)$

# Continuous flow stirred tank reactor (CFSTR, CSTR)



- Flow in and out =  $Q$
- Tank volume =  $V$
- Influent concentration =  $C_0$
- Effluent concentration =  $C_F$
- Completely mixed
- The concentration of the end products in the reactor = concentration in the outflow
  - The yield is limited because the influent is mixed to the whole tank volume

Steady-flow of water conditions:  $Q_{in} = Q_{out} = Q$  and  $\frac{dV}{dt} = 0$

**Mass Inflow + Mass generated = Mass outflow + Mass accumulated**

$$QC_0 + Vr_c = QC + V \frac{dC}{dt}$$

$$C_0 - C + \frac{V}{Q} r_c = \frac{V}{Q} \frac{dC}{dt}$$

Continues on next page

# CFSTR cont'd

From previous page

$$C_o - C + \frac{V}{Q} r_c = \frac{V}{Q} \frac{dC}{dt}$$

Definition: Retention time = hydraulic residence time = the time required for a reaction

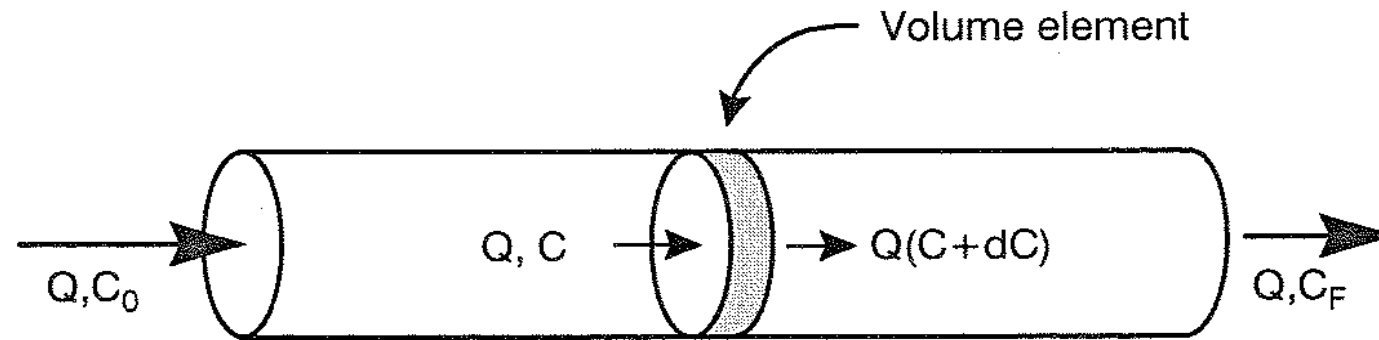
$$\theta = \frac{V}{Q}$$

In stationary state  $dC/dt = 0$

$$\Rightarrow C_o - C + \theta r_c = 0$$

(Exercise 3 b)

# Plug flow reactor (PFR)



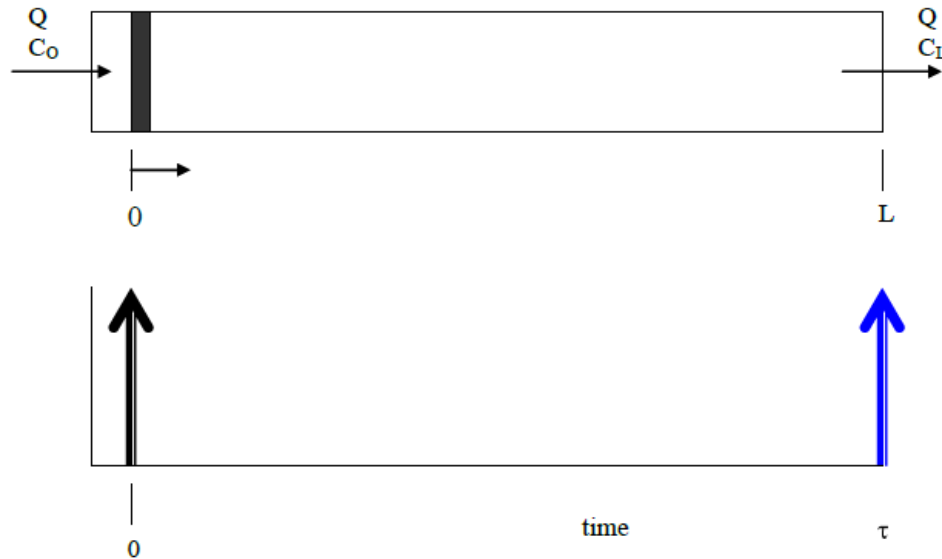
- Continuous flow reactor
- Influent fed to one end of the reactor
- Effluent drawn from the other end
- No mixing
- Reaction advances along the length of the reactor
- Concentrations different in the influent and effluent
- Hydraulic retention time is the same as for CFSTR

$$\theta = \frac{V}{Q}$$

# Plug flow reactor

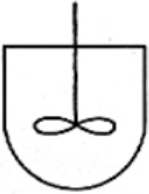
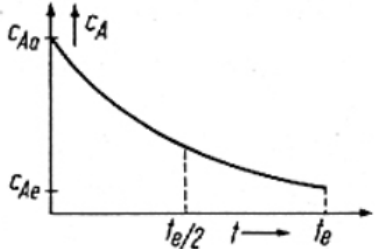
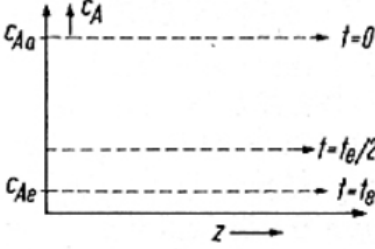
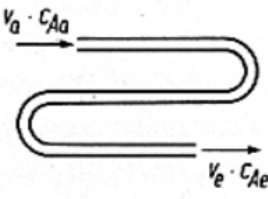
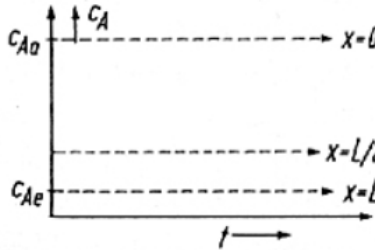
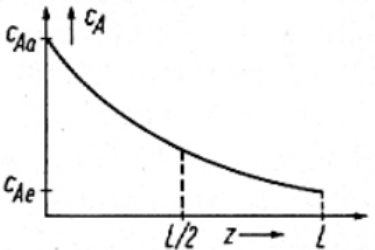
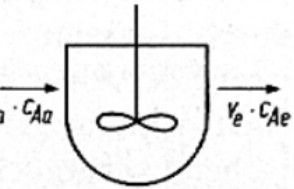
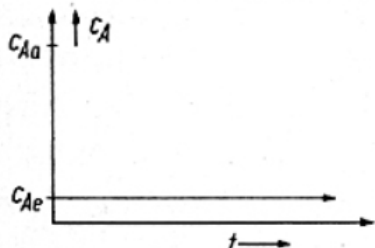
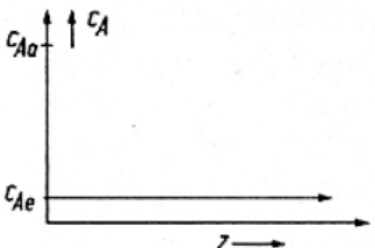
Characteristics of ideal plug flow

- PERFECT MIXING IN THE RADIAL DIMENSION (UNIFORM CROSS SECTION CONCENTRATION)
- NO MIXING IN THE AXIAL DIRECTION, OR NO AXIAL DISPERSION (SEGREGATED FLOW)



TRACER PULSE INPUT AT  $t = 0$  TRANSLATED TO EQUAL PULSE

# Ideal reactors

Type		Concentration course	
		time	space
Batch			
	a) TFR 		
	b) CSTR 		

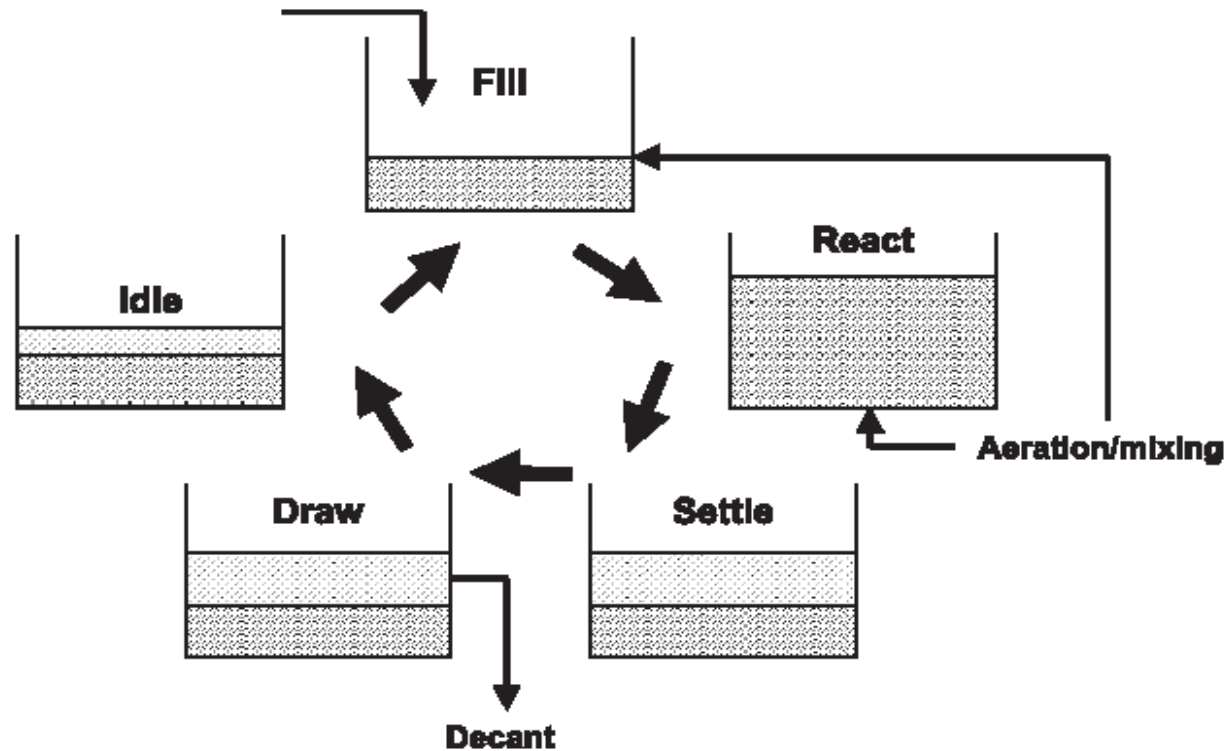
**the batch stirred tank reactor:** concentration is constant in the whole tank, but it is dropping down with the time. The reactor is **not stationary in (both) space and time.**

**the continuous plug (tubular) flow reactor:** concentration is constant over the time at different length positions along the tube. The concentration drops down along the reactor length. The reactor is **not stationary in (both) space and time.**

**the continuous stirred tank reactor:** concentration is stationary in space and time. The reactor is **stationary in space and time.** (not in the start-up-, shutdown- or disturbed operation phase)

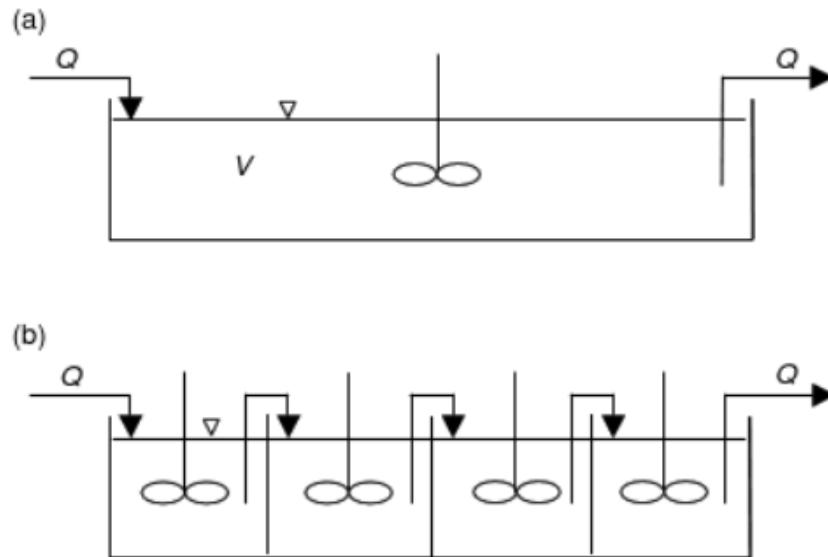


# Semicontinuous batch reactor SBR – especially in wastewater treatment



All phases happen in the same tank sequentially

# Reactors in series



**FIGURE 2-18.** (a) A single CFSTR with volume  $V$ , and (b) the same tank divided into four equal-sized ( $V/4$ ) CFSTRs in series.

- CFSTRs are sometimes used in series.
- Increases the yield, without adding volume
- The more CFSTRs in series the more it approaches PFR