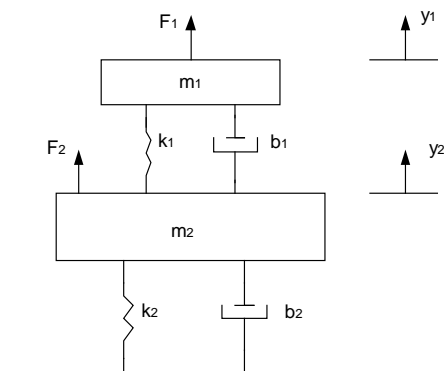


## ELEC-E8116 Model-based control systems /exercises 3

**Problem 1.** Consider the mass/spring/damper system shown in the figure. The control forces are  $F_1$  and  $F_2$ . Parameter values:  $k_1=1$ ,  $k_2=4$ ,  $b_1=0.2$ ,  $b_2=0.1$ ,  $m_1=1$ ,  $m_2=2$ .

- Form a differential model of the system.
- Form a state-space representation of the system.
- Plot the singular values as functions of frequency (Matlab).
- Calculate the  $H_\infty$ -norm of the obtained system (Matlab).



**Problem 2.** (Matlab) Consider the transfer function matrix

$$G(s) = \begin{bmatrix} \frac{10(s+1)}{s^2 + 0.2s + 100} & \frac{1}{s+1} \\ \frac{s+2}{s^2 + 0.1s + 10} & \frac{5(s+1)}{(s+2)(s+3)} \end{bmatrix}$$

Determine a realization and plot the singular values.

**Problem 3.** Two systems are given by the two transfer function matrices below. Calculate the poles and zeros

$$G_1(s) = \begin{bmatrix} \frac{2(s+1)(s+2)}{s(s+3)(s+4)} & \frac{s+2}{(s+1)(s+3)} \end{bmatrix} \quad G_2(s) = \begin{bmatrix} \frac{1}{s+1} & \frac{s+3}{(s+1)(s-2)} \\ \frac{10}{(s-2)} & \frac{5}{s+3} \end{bmatrix}$$

**Problem 4.** By considering the static system  $G(s) = \begin{bmatrix} 0 & 100 \\ 0 & 0 \end{bmatrix}$ , prove that

eigenvalues do not give a reliable view about the gain of a multivariable system. What is a better alternative?