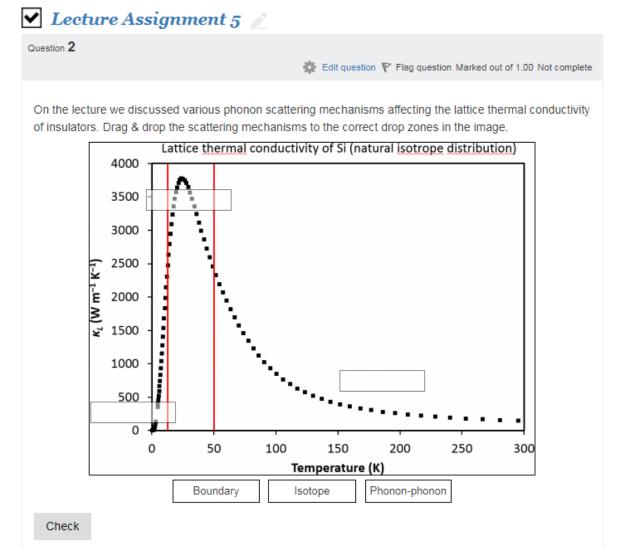
## Functional Inorganic Materials Lecture 5: Thermal Conductivity

Fall 2020

Antti Karttunen (antti.karttunen@aalto.fi)
Department of Chemistry and Materials Science

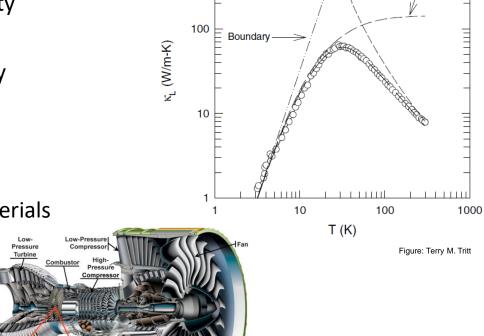


## Lecture Assignments 5-8: MyCourses Quiz



#### **Contents**

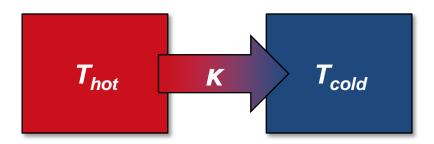
- Introduction to thermal conductivity
  - Atomic-level perspective
  - Electronic thermal conductivity
  - Lattice thermal conductivity
- Materials perspective
  - High thermal conductivity materials
  - Thermal insulators
- Applications
  - Microelectronics
  - Thermal barrier coatings
  - Thermoelectrics (to be discussed on Lecture 6)



3

Boundary + Point-defect

#### Thermal conductivity $\kappa$



- Ability of a substance to conduct heat (units: W m<sup>-1</sup> K<sup>-1</sup>)
- Very concrete property in our everyday life
  - Perhaps you've burnt your hand by touching the surface of a *hot metal* (a very good conductor of heat)
  - Perhaps after that, you've worn a thermally insulating glove in your hand
  - During the Finnish winter, it's good to live in a thermally insulated place
- Thermal conductivity is also very important material property for various technological applications:
  - Microelectronics (for example, CPU heat management)
  - Thermal barrier coatings in gas turbines (for example, airplane engines)
  - Thermoelectrics (direct heat-to-electricity conversion)

#### Warm-up

Do the following materials possess high or low thermal conductivity? Why?



Diamond

Silicon



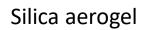
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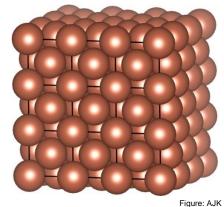


Polyethylene



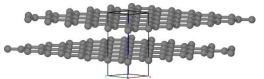






Copper

### $\kappa$ at 300 K (W m<sup>-1</sup> K<sup>-1</sup>)





~2200 (natural diamond)

Diamond



~2000 (in-plane); ~6 (out-of-plane)

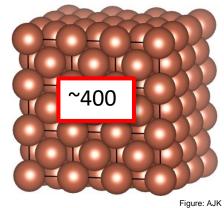
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Polyethylene







Silica aerogel

Copper

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# Atomic-level mechanisms behind thermal conductivity

- Metals
  - Heat is primarily carried by conduction electrons
- Insulators
  - Heat is primarily carried by **phonons** (lattice vibrations)
- Semiconductors
  - Low doping levels -> insulator-like behavior

Insulator

High doping levels -> both phononic and electronic thermal conductivity

Insulator – semiconductor – metal classification based on band structure:

Empty bands:

Occupied bands:

Fermi level

Semiconductor

Metal

#### Electronic thermal conductivity

- Heat is carried by conduction electrons
- Thermal conductivity is directly related to the electrical conductivity (Wiedemann-Franz law):

$$\kappa_e = LT\sigma$$

$$L = 2.44 imes 10^{-8} \, \mathrm{W} \, \Omega \, \mathrm{K}^{-2}$$

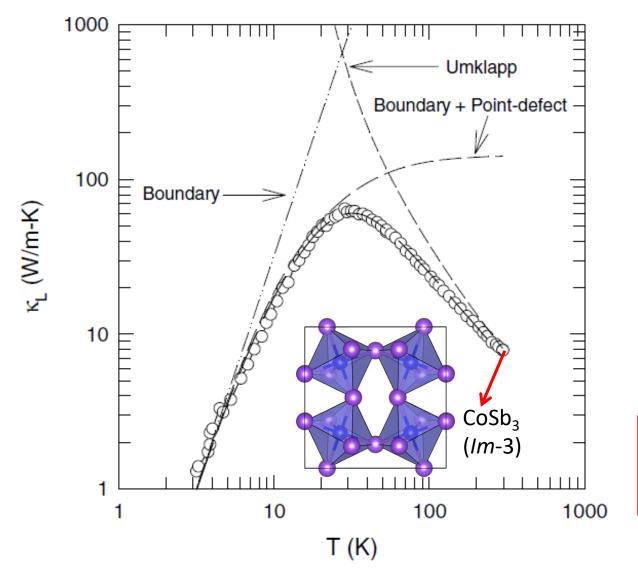
L is roughly constant, but not exactly same for all metals!

- Electrical conductivity
  - increases when T decreases
  - Decreases when T increases (electron-phonon scattering increases)

Metal	Electrical conductivity σ (S/m) at 300 K	Thermal conductivity κ (W m <sup>-1</sup> K <sup>-1</sup> )
Ag	$6.3 \times 10^7$	430
Cu	$6.0 \times 10^7$	400
Al	$3.5 \times 10^7$	235
Zn	$1.7 \times 10^7$	120
Pb	$4.6 \times 10^6$	35

#### Thermal conductivity of an insulator

Thermal conductivity of crystalline materials is usually highly temperature-dependent



Dots = experiment (CoSb<sub>3</sub>)

#### Dashed curves =

Theoretical limits imposed by various phonon scattering mechanisms:

- Boundary
- Point-defect / massdefect (isotope)
- Umklapp = phononphonon scattering
- At T > 100, phononphonon scattering dominates (1/T dependence)

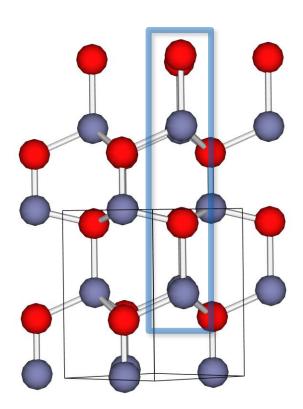
Here we focus on room temperature thermal conductivity

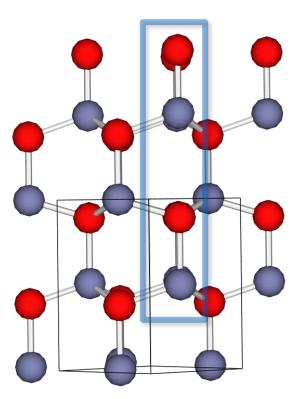
#### Lattice thermal conductivity

- In insulating solid-state materials, heat is carried by vibrational excitations called *phonons* (from greek  $\phi\omega v\dot{\eta} = phone = sound we will soon hear why)$
- Phonons give rise to *lattice thermal conductivity*,  $\kappa_{i}$
- Materials have finite thermal conductivity because of various phonon scattering mechanisms (boundary, point-defect, isotope, phonon-phonon, electron-phonon)
- Phonon-phonon scattering is the most important scattering mechanism for crystalline, electrically insulating materials at room temperature
  - Note that crystal with only harmonic phonons (vibrations) would have no phonon–phonon scattering
  - Phonon-phonon scattering arises due to anharmonicity (deviation from harmonic oscillator behavior)
  - Phonon anharmonicity is also the reason for negative thermal expansion (for example, silicon contracts when temperature increases from 18 K to 120 K)

#### Vibrations in molecules and solids

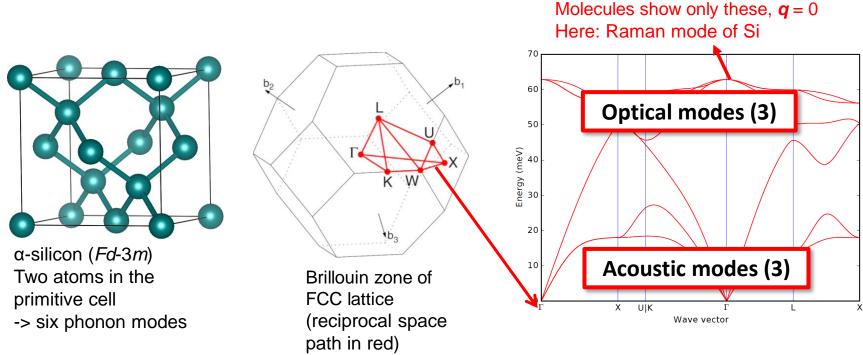
- A molecule with N atoms shows 3N 6 vibrational modes  $\omega_i$
- A crystal with *N* atoms in the primitive cell shows 3*N* vibrational modes
  - Atoms in neighboring cells can vibrate in-phase or out-of-phase!
- In-phase and anti-phase Zn–O stretching in ZnO:





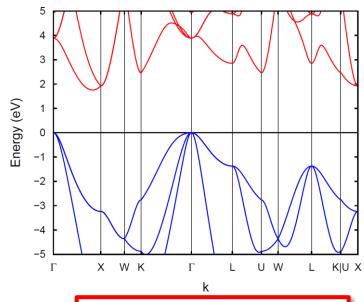
#### Phonon dispersion relations

- The vibrational modes of a solid are described as a function of wavevector q in the reciprocal space:  $\omega_i(q) = \mathbf{phonon\ dispersion\ relations}$ 
  - Phonon dispersion relations account for the periodic nature of the crystal
  - Atoms in neighboring cells can vibrate in a different phase

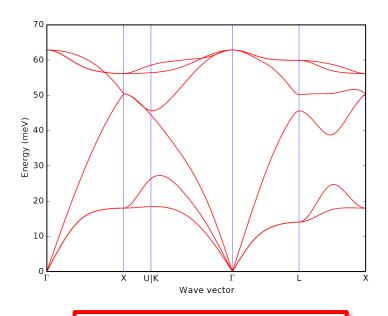


#### Phonons vs. electrons

- Electronic band structures are plotted as a function of wavevector k
  - The crystal orbitals can be in a different phase in neighboring cells
- Phonon dispersion relations are plotted as a function of wavevector q
  - Atoms in neighboring cells can vibrate in a different phase



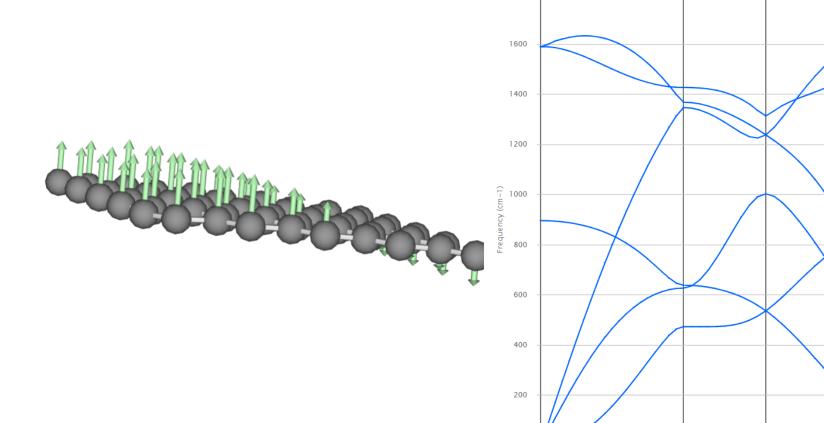
Electronic band structure of α-silicon



Phonon dispersion relations of α-silicon

### Visualization of phonons

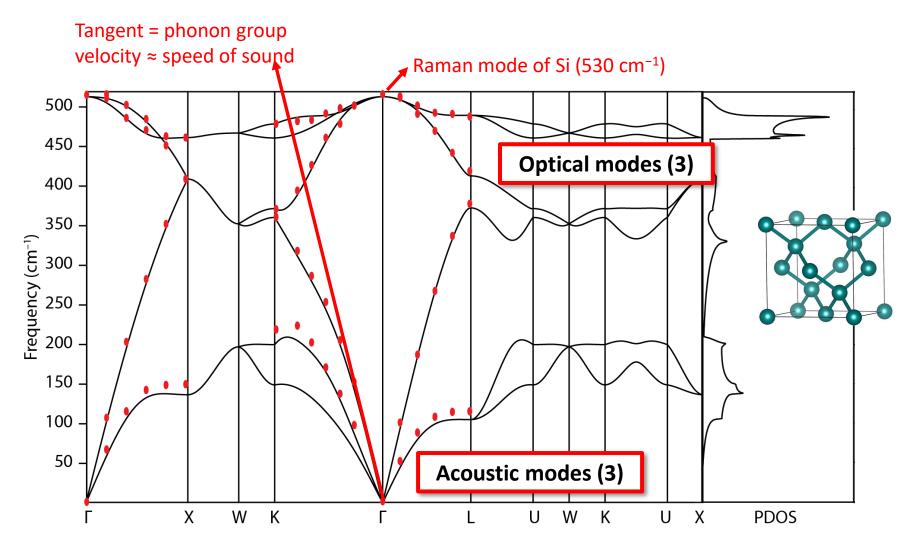
- http://henriquemiranda.github.io/phononwebsite/phonon.html
- Let's have a look for example on the acoustic modes of graphene





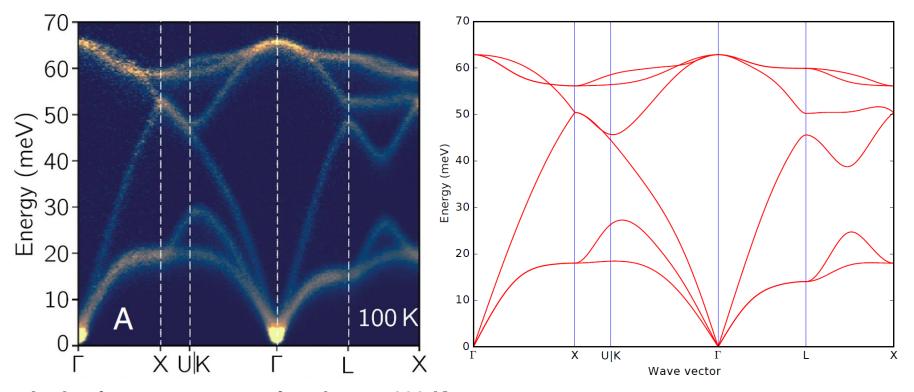
### Phonon dispersions for silicon (1)

Red = *Inelastic Neutron Scattering*. Calculated lines: Density Functional Theory.



### Phonon dispersions for silicon (2)

- Experimental data on previous slide were from the 1960s
- Excellent agreement also between theory and recent state-of-the-art inelastic neutron scattering data (Kim et al. 2018, figure below)
- Calculated phonon dispersion relations: Density Functional Theory

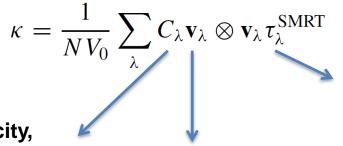


Inelastic neutron scattering data at 100 K (*Proc. Natl. Acad. Sci.* 2018, *115*, 1192)

Figure: AJK (theory, DFT-PBE0-SVP)

# Lattice thermal conductivity $\kappa_L$ from Boltzmann Transport Equation

- In the past few years, the theoretical methods have evolved to a level, where it is possible to predict the lattice thermal conductivity of non-metallic materials with a good precision (5-10%)
- $\kappa_l$  can be solved with the help of the semiclassical Boltzmann Transport Equation
- In Single-Mode Relaxation Time approximation:



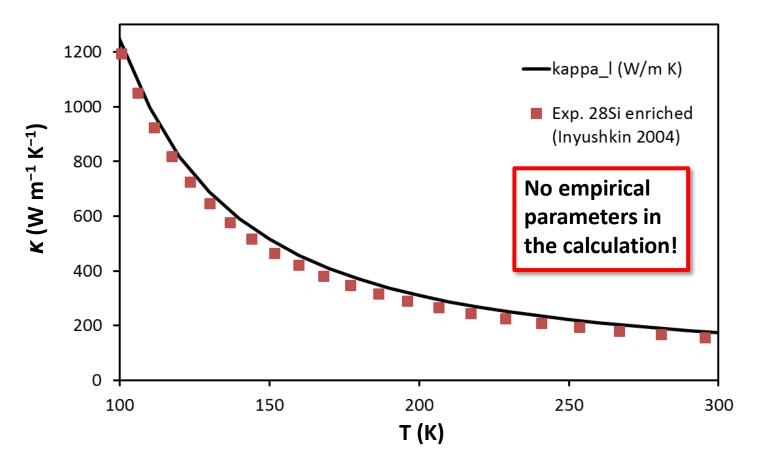
Heat capacity, calculated from phonon dispersions

Phonon group velocity, calculated from phonon dispersions

Phonon relaxation time, calculated from phonon scattering rates (using phonon dispersions and anharmonic force constants)

#### Lattice thermal conductivity of silicon

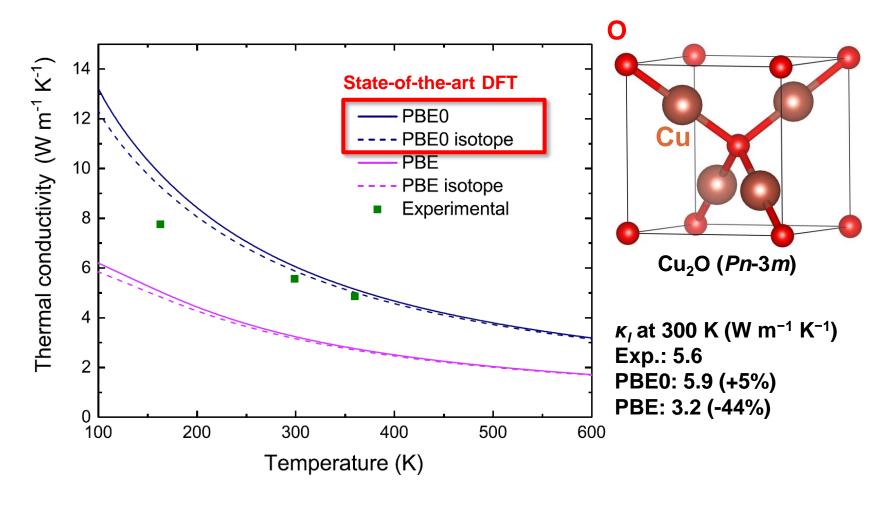
For a simple semiconductor like silicon,  $\kappa_l$  can be predicted with good accuracy using Density Functional Theory (DFT) and semiclassical Boltzmann Transport Equation



Experiment: A. V. Inyushkin et al. Phys. Status Solidi C 2004, 1, 2995–2998.

DFT results: A. J. Karttunen, unpublished results.

## Lattice thermal conductivity of Cu<sub>2</sub>O



#### Lattice thermal conductivity of NiO

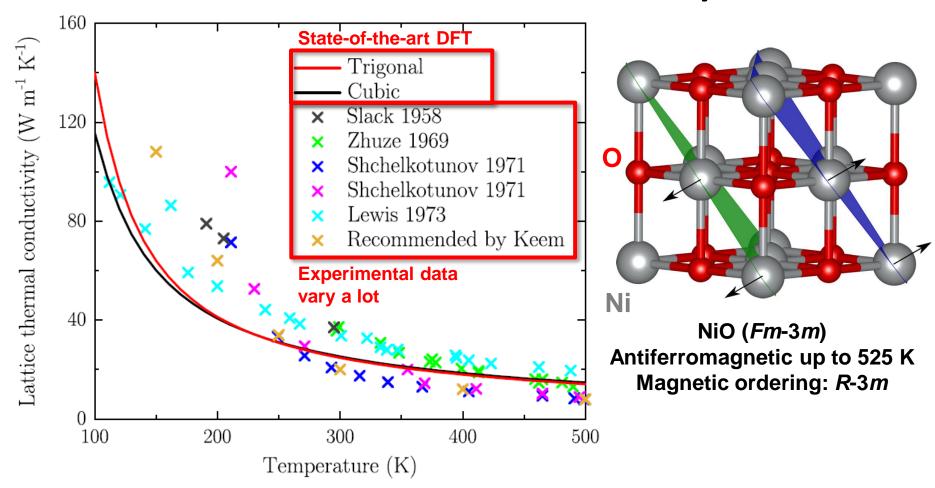


FIG. 4. Lattice thermal conductivity of NiO calculated using both the trigonal (red line) and cubic (black line) primitive cells. Crosses denote the different experimental data points [48–52].

<sup>20</sup> 

#### Periodic trends

- Lattice thermal conductivity depends strongly on the interatomic forces
- The stronger the interactomic forces, the more strongly the atoms are coupled to each other
  - Strong bonds -> larger phonon velocities
  - Speed of sound in diamond: 12 000 m/s
  - Si: 8500 m/s
  - Pb: 1300 m/s
- Strong covalent bonds show the largest interatomic force constants, resulting in the highest lattice thermal conductivity
- In ionic materials, the interatomic force constants are smaller and the phonon velocities lower
  - For NaCl,  $\kappa = 6.5 \text{ W m}^{-1} \text{ K}^{-1}$

	Thermal conductivity κ (W m <sup>-1</sup> K <sup>-1</sup> )	
С	~2200	
	(diamond)	
Si	~150	
Ge	~60	
Sn	~60 (metal)	
Pb	~35 (metal)	

### Crystalline vs. amorphous

- So far, we have mainly discussed crystalline materials
- For amorphous, non-crystalline materials, phonons are not well-defined
- Generally, they possess low thermal conductivity (e.g. acrylic glass  $0.2 \text{ W m}^{-1} \text{ K}^{-1}$ )

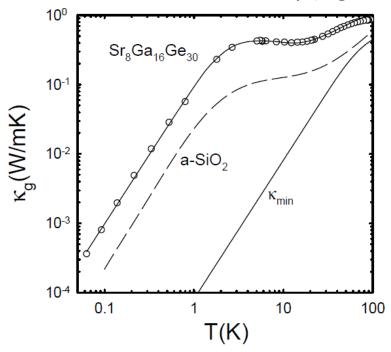


FIG. 2. Lattice thermal conductivity measured from 60 mK to 100 K for  $Sr_8Ga_{16}Ge_{30}$  with a fit (solid curve) to the model discussed in the text (see also Fig. 3). The dashed line is for a-SiO<sub>2</sub>, and the solid curve labeled  $\kappa_{min}$  is the calculated minimum thermal conductivity of Ge.

25 January 1999

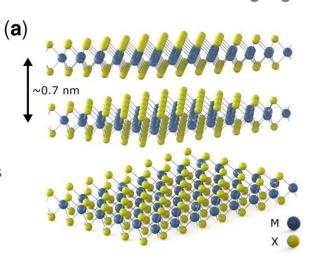
#### Low- $\kappa_i$ crystalline materials

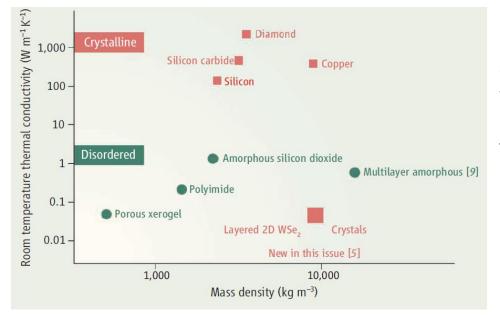
19 JANUARY 2007 VOL 315 SCIENCE www.sciencemag.org

## Ultralow Thermal Conductivity in Disordered, Layered WSe<sub>2</sub> Crystals

Catalin Chiritescu, David G. Cahill, Ngoc Nguyen, David Johnson, Arun Bodapati, Pawel Keblinski, Paul Zschack

The cross-plane thermal conductivity of thin films of WSe<sub>2</sub> grown from alternating W and Se layers is as small as 0.05 watts per meter per degree kelvin at room temperature, 30 times smaller than the c-axis thermal conductivity of single-crystal WSe<sub>2</sub> and a factor of 6 smaller than the predicted minimum thermal conductivity for this material. We attribute the ultralow thermal conductivity of these disordered, layered crystals to the localization of lattice vibrations induced by the random stacking of two-dimensional crystalline WSe<sub>2</sub> sheets. Disordering of the layered structure by ion bombardment increases the thermal conductivity.





#### Search for the worst.

Room-temperature thermal conductivities of a few representative materials compared with new data for ordered **WSe**<sub>2</sub> films. The material sets a record for the lowest thermal conductivity of a fully dense material at 300 K. Remarkably, the ultralow conductivity is achieved through the introduction of crystalline order.

#### Thermal engineering

- How to decrease the thermal conductivity of materials?
  - In general: add *disorder*
  - Alloying: From Si (150) and Ge (60) to Si-Ge alloy (50-50%): 10 W  $m^{-1}$  K<sup>-1</sup>
  - Doping: electronic doping also introduces kind of point defects, decreasing lattice thermal conductivity.
    - For example, ZnO: **43** W m<sup>-1</sup> K<sup>-1</sup>; 2% Al doping decreases the thermal conductivity to ~**7** W m<sup>-1</sup> K<sup>-1</sup>
  - Create interfaces that scatter phonons
    - Superlattices
- How to increase thermal conductivity?
  - Prepare samples with high isotopic purity (the effect will be large < 100 K, but only ~10% at room temperature
  - Create better materials!

#### Oxide-organic superlattices

Nano Energy (2016) 22, 338-348



Available online at www.sciencedirect.com

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journal homepage: www.elsevier.com/locate/nanoenergy

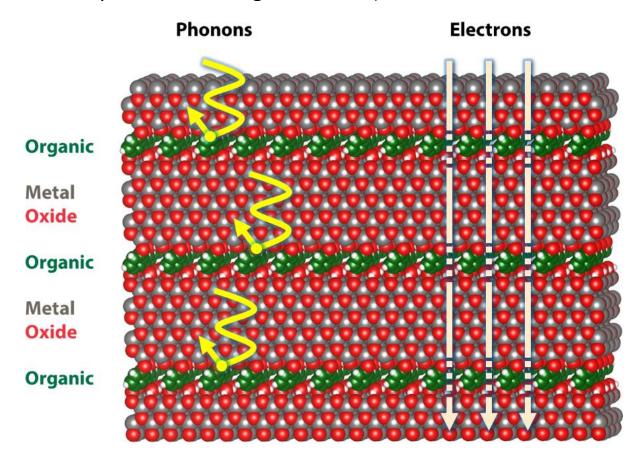
FULL PAPER

Layer-by-layer design of nanostructured thermoelectrics: First-principles study of ZnO:organic superlattices fabricated by ALD/MLD

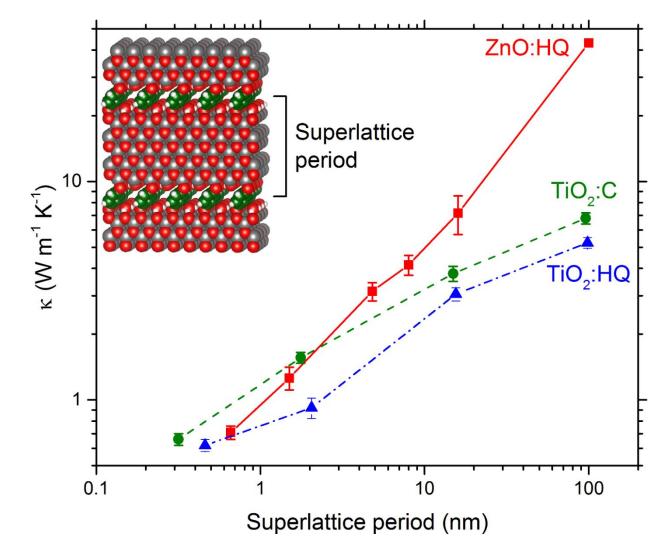
Antti J. Karttunen\*, Tommi Tynell, Maarit Karppinen

#### Oxide-organic superlattices

Try to create phonon-blocking interfaces (that would not scatter electrons as much)



#### Oxide-organic superlattices



J.-P. Niemelä, A. J. Karttunen, M. Karppinen, J. Mater. Chem C 2015, 3, 10349.

## Thermal-barrier coatings for more efficient gas-turbine engines

David R. Clarke, Matthias Oechsner, and Nitin P. Padture,

Guest Editors MRS BULLETIN • VOLUME 37 • OCTOBER 2012 • www.mrs.org/bulletin ■ 891

#### Introduction

Thermal-barrier coatings (TBCs) are refractory-oxide ceramic coatings applied to the surfaces of metallic parts in the hottest part of gas-turbine engines (Figures 1 and 2), enabling modern engines to operate at significantly higher gas temperatures than their predecessors (see recent reviews<sup>1-6</sup>). Gas-turbine engines, used to propel aircraft and to generate electricity, are Carnot engines where their efficiency and core power are directly related to the gas temperature entering the turbine section.<sup>7,8</sup> Further increases in the energy efficiency of gasturbine engines, both to increase the electricity output and, for jet engines, the thrust-to-weight ratio and durability, will rely on further improvements in TBCs. At the same time, as gas temperatures are increased in the pursuit of higher engine efficiency, there are new challenges to existing TBCs.

To place this in context, gas-turbine engines are a \$42 billion industry worldwide (2010), with ~65% of the sales accounting for jet engines and the remainder land-based engines for electricity generation.9 The latter, fueled by natural gas or liquid A refractory material retains its strength at high temperatures

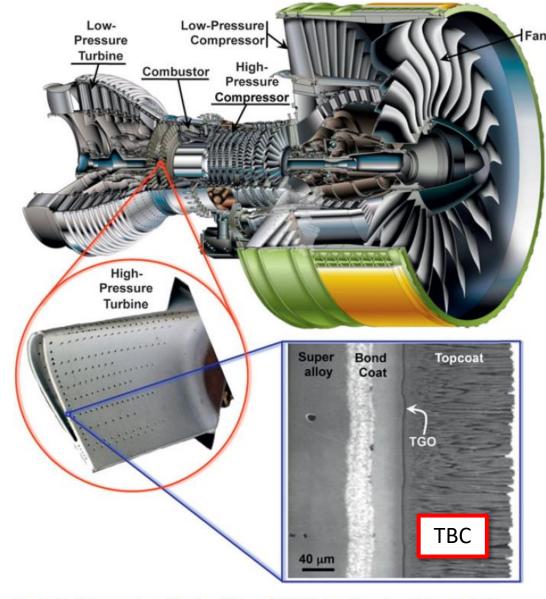
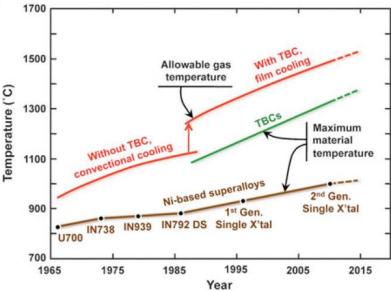


Figure 1. Cutaway view of Engine Alliance GP7200 aircraft engine, photograph of a turbine blade (~10 cm long) with thermal-barrier coating (TBC) from the high-pressure hot section of an engine, and a scanning electron microscope (SEM) image of a cross-section of an electron beam physical vapor deposited 7 wt% yttria-stabilized zirconia TBC. (Engine image courtesy of Engine Alliance, turbine blade photograph courtesy of YXLON, and the SEM micrograph is from Reference 44.) TGO, thermally grown oxide.

#### **TBCs**



**Figure 3.** Progression of temperature capabilities of Ni-based superalloys and thermal-barrier coating (TBC) materials over the past 50 years. The red lines indicate progression of maximum allowable gas temperatures in engines, with the large increase gained from employing TBCs. Based on a diagram from the late Professor Tony Evans.

#### Yttria-stabilized Zirconia (YSZ)

• Zirconia,  $ZrO_2$ , is potentially a very useful ceramic material with a high melting point of ~2700 °C but on cooling it undergoes a series of phase transitions:

```
cubic (fluorite) \xrightarrow{2400\,^{\circ}\text{C}} tetragonal \xrightarrow{1050\,^{\circ}\text{C}} monoclinic (baddeleyite)
```

- The tetragonal to monoclinic transition is associated with an increase in unit cell volume by  $\sim$ 9% -> ceramic bodies fabricated at high T shatter on cooling
- The transitions can be avoided by creating a solid solution ZrO<sub>2</sub>-Y<sub>2</sub>O<sub>3</sub>

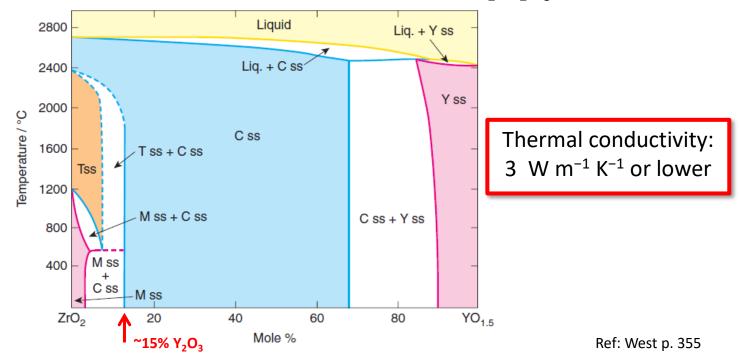


Figure 7.28  $ZrO_2$ – $Y_2O_3$  phase diagram. M, T and C refer to the monoclinic, tetragonal and cubic polymorphs of zirconia, and their solid solutions, ss. Y = yttria,  $Y_2O_3$ .