



Aalto University  
School of Engineering

**MEC-E5003**

**FLUID POWER BASICS**

**Study Year 2020**

# Pumps

# Actuators

# Accumulators



Aalto University  
School of Engineering  
Mechanical Engineering / Engineering Design / Mechatronics / Fluid Power

# Lecture themes

Flow to the system – How?

Making use of the hydraulic power – How?

Storing energy in hydraulic system – Why and is that even possible?

# Hydrostatic pumps

Convert mechanical power into hydraulic power

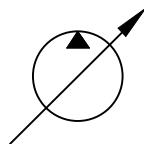
Hydrostatic pumps produce flow, not pressure

Unidirectional

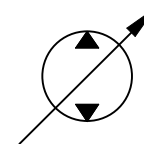
Bidirectional



Constant displacement



Variable displacement



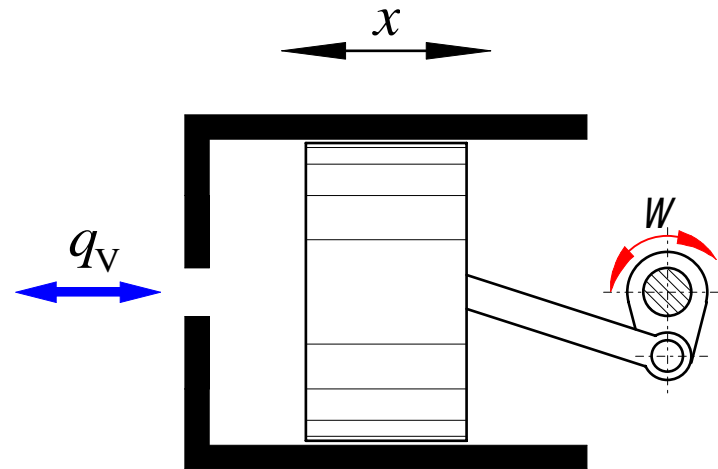
## Construction

Most common construction types:

- gear
- vane
- screw
- piston

All operate on positive displacement principle

## Positive displacement principle



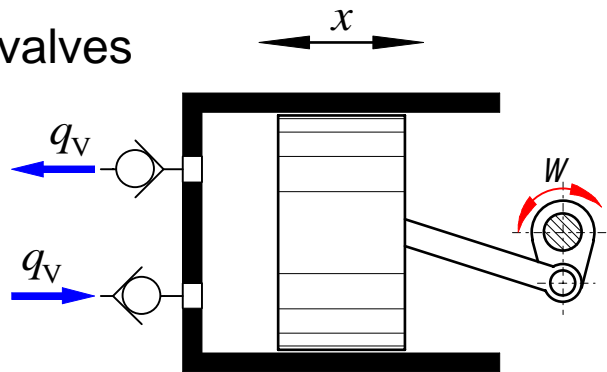
Operating phases:

Fluid flows into transfer volume – suction phase

Fluid flows out from volume – pressure phase

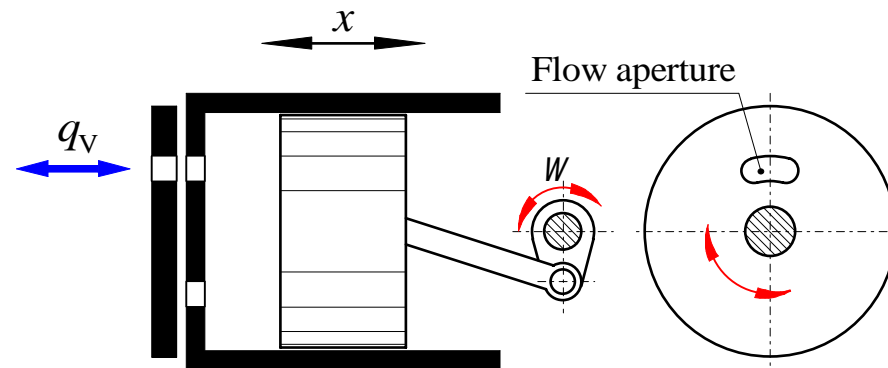
## Control of flow direction

Check valves

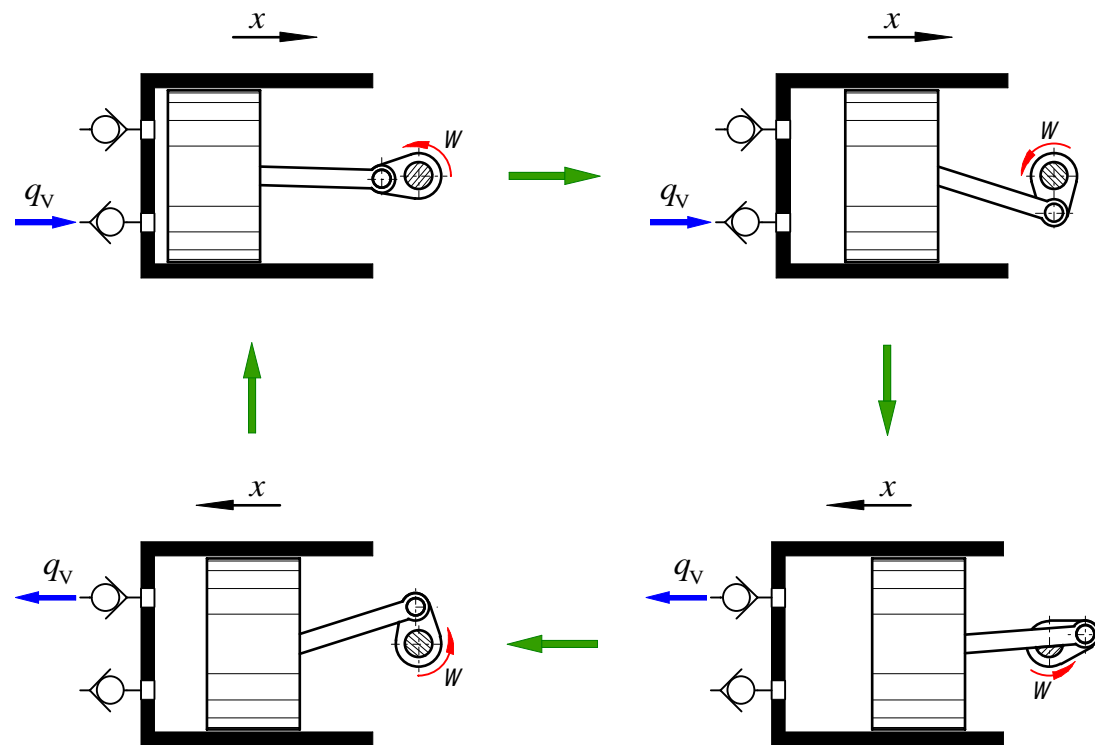


Pressure control  
aka valve control

Forced control ®

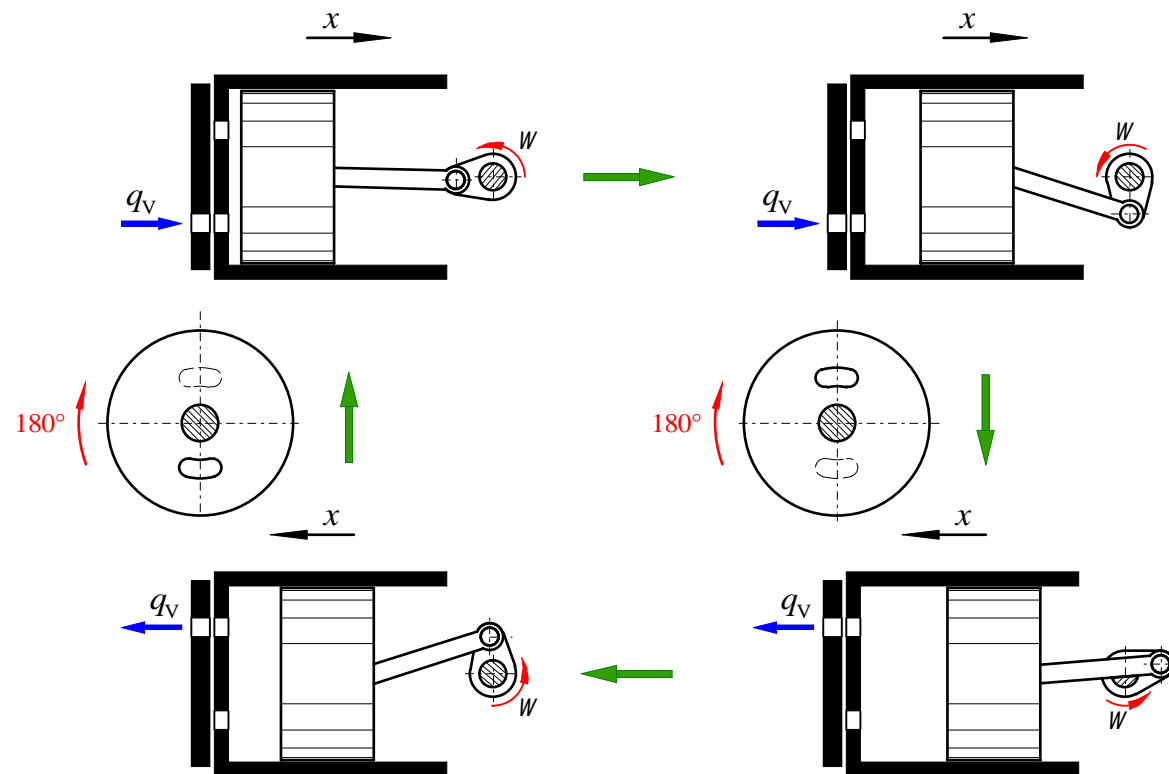


## Pressure control aka valve control



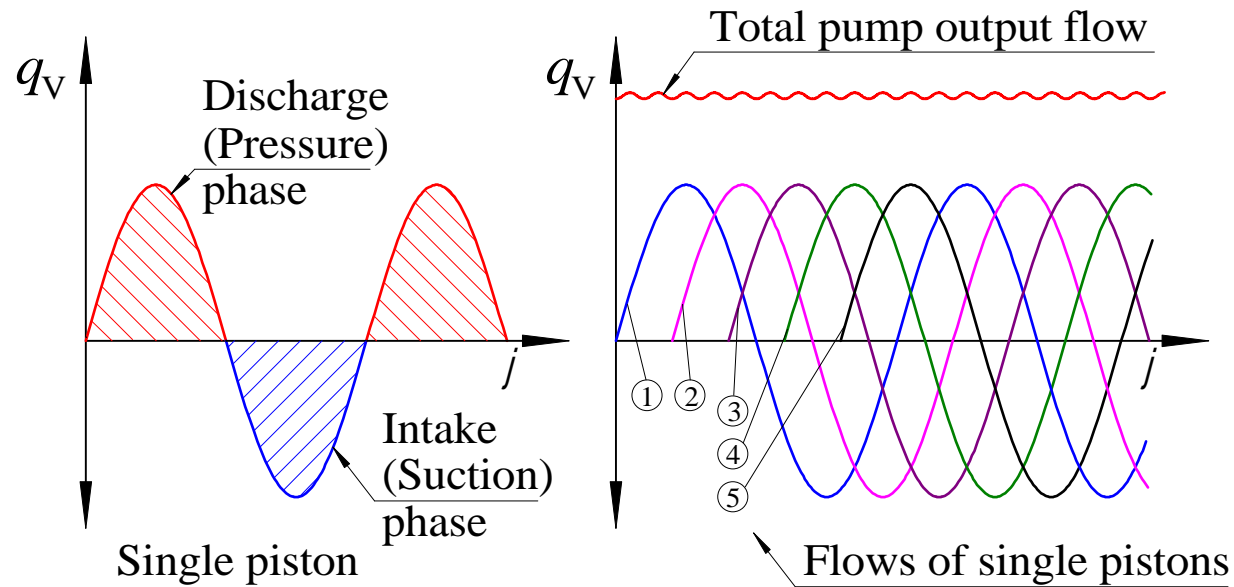


## Forced control



Output flow variation ->  
Internal pressure variation (depending  
on the system impedance) ->

**Flow pulsation** External (air) pressure variation -> Noise



Flow pulsation is due to intermittent  
nature of positive displacement principle

## Cavitation in pumps

Cause: Friction losses in inlet channel of pump

Pressure in fluid decreases to vapour pressure of the fluid

Ⓜ fluid starts to vaporize (also size of air bubbles increases)

Ⓜ vaporized fluid is pressurized in pump

Ⓜ vapour bubbles collapse rapidly ("implosion")

Ⓜ pressure shocks

Ⓜ material damages, noise, decreased output flow

Suction lines of pumps are

- short

- straight

- wide (large diameter) and the pump can be placed lower than the reservoir (tank) surface to avoid cavitation.

## Pump characteristics

Theoretical output flow  $q_{V,\text{theor}} = n \times V_g$

Swept volume  $V_g$  [m<sup>3</sup>/r]

$$\text{cm}^3/\text{r} = 10^{-6} \text{ m}^3/\text{r}$$

Rotation speed  $n$  [r/s]

$$\text{r/min} = 1/60 \text{ r/s}$$

$$q_{V,\text{theor}} = \omega \times V_{\text{rad}}$$

$$\omega = 2\pi \times n$$

Angular velocity  $\omega$  [rad/s]

$$V_{\text{rad}} = \frac{V_g}{2\pi}$$

Swept volume per radian  $V_{\text{rad}}$  [m<sup>3</sup>/rad]

Effective output flow

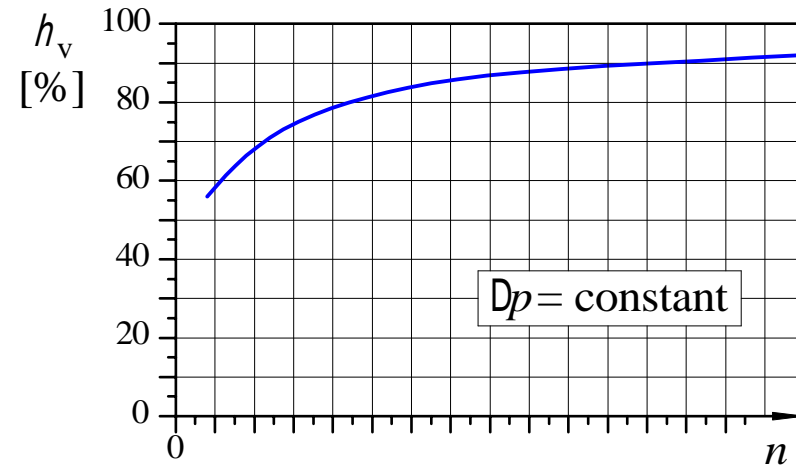
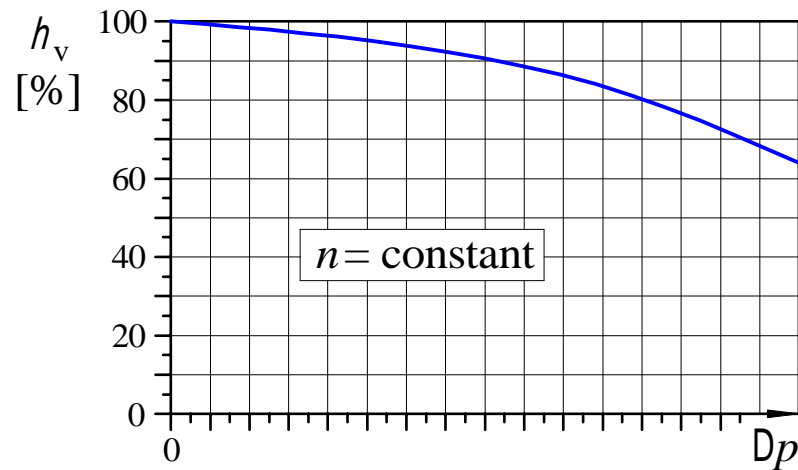
$$q_{V,\text{real}} = n \times V_g \times h_v$$

Leakage – volumetric efficiency  $h_v$

Wilson's pump model

$$q_{V2} = \varepsilon V_i n - C_s \frac{V_i \Delta p}{2\pi \nu \rho}$$

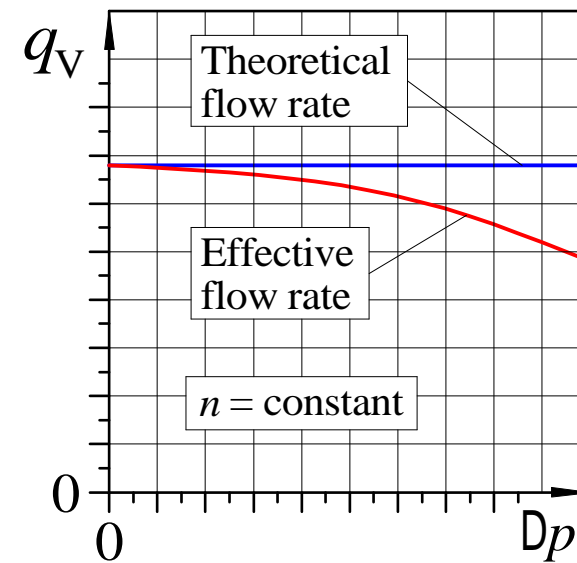
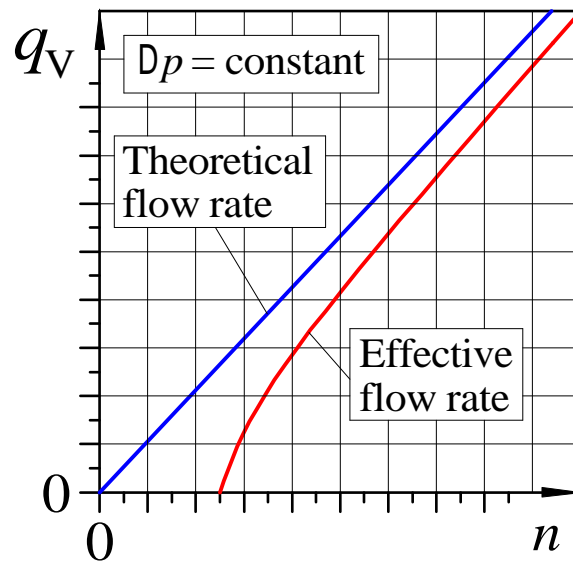
$\nu$  dynamic viscosity



Wilson's pump model

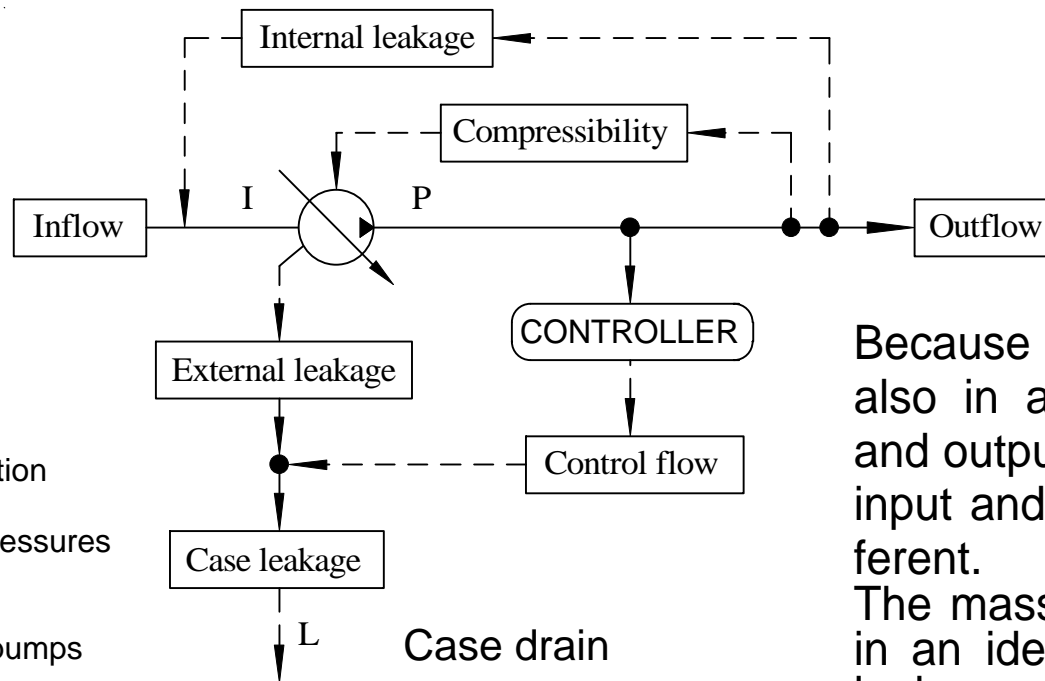
$$q_{v2} = \varepsilon V_i n - C_s \frac{V_i \Delta p}{2\pi \nu \rho}$$

## Theoretical output flow – Effective output flow



- $\varepsilon$  pump angle set value (0 - 1)
- $V_i$  max. displacement (per revolution)
- $n$  rotational speed (1/s)
- $C_s$  laminar flow loss coefficient
- $Dp$  pressure difference over pump
- $\nu$  fluid kinematic viscosity
- $\rho$  fluid density

## Leakage flows in pumps



### Internal leakage

- All pumps

### External leakage

- With case drain connection
- To protect shaft seal
- To prevent high case pressures

### Controller drain

- If pump has a controller
- Variable displacement pumps

Because of the fluid compressibility also in an **ideal pump** the input and output flow rates are different if input and output pressures are different.

The mass flow rates are the same in an ideal pump without external leakage.



Theoretic drive torque  $T_{\text{theor}} = \frac{Dp \cdot V_g}{2 \cdot p}$

Swept volume  $V_g$  [m<sup>3</sup>/r]

Pressure difference  $Dp$  [N/m<sup>2</sup>]



# Performance of pumps and motors

## PUMP

Wilson's model

Flow rate (output)

$$q_{v2} = \varepsilon V_i n - C_s \frac{V_i \Delta p}{2\pi \nu \rho}$$

Pump torque (input)

$$T = \varepsilon \frac{V_i \Delta p}{2\pi} + C_f \frac{V_i \Delta p}{2\pi} + C_v V_i n \nu \rho + T_c$$

$\varepsilon$	Pump angle set value (0 - 1)
$V_i$	displacement (per revolution)
$n$	rotational speed (1/s)
$C_s$	laminar flow loss coefficient
$\Delta p$	pressure difference over pump
$\nu$	fluid kinematic viscosity
$\rho$	fluid density
$C_f$	Coulomb friction coefficient
$C_v$	viscous friction coefficient
$T_c$	constant torque loss

Ideal pump and motor

Wilson's model is very simplistic and it can't explain all the phenomena in pumps (and motors).

Reference:

Ellmann, A., Kauranne, H. Kajaste, J. & Pietola, M.

EFFECT OF PARAMETER UNCERTAINTY ON RELIABILITY OF HYDRAULIC TRANSMISSION SYSTEM SIMULATION

Proceedings of IMECE2005 2005 ASME International Mechanical Engineering Congress and Exposition November 5-11, 2005, Orlando, Florida USA

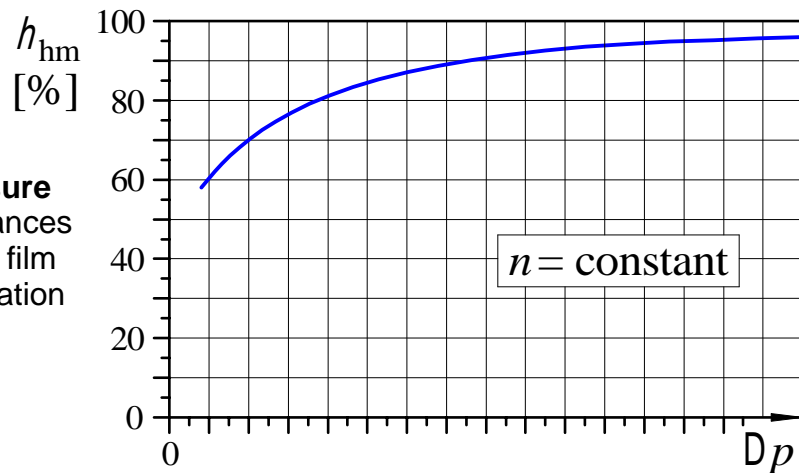
Effective drive torque

$$T_{\text{real}} = \frac{Dp \times V_g}{2 \times \pi \times h_{\text{hm}}}$$

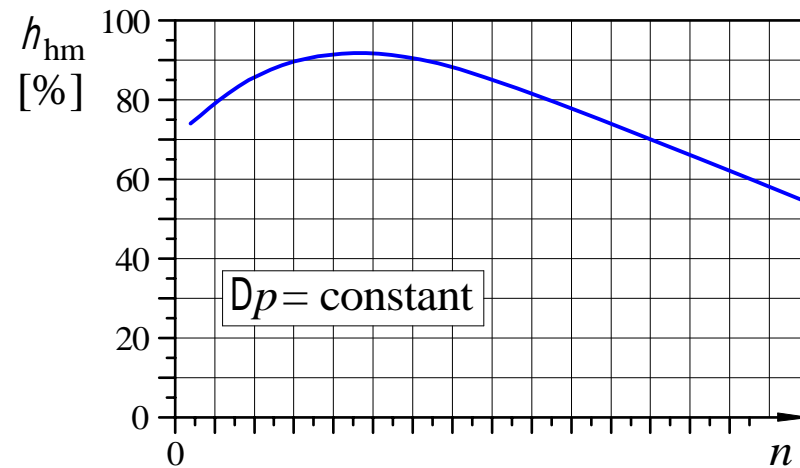
Wilson's pump model does not explain the phenomena seen in the figures below well

Friction – hydromechanical efficiency  $h_{\text{hm}}$

$$T = \varepsilon \frac{V_i \Delta p}{2\pi} + C_f \frac{V_i \Delta p}{2\pi} + C_v V_i n v \rho + T_c$$

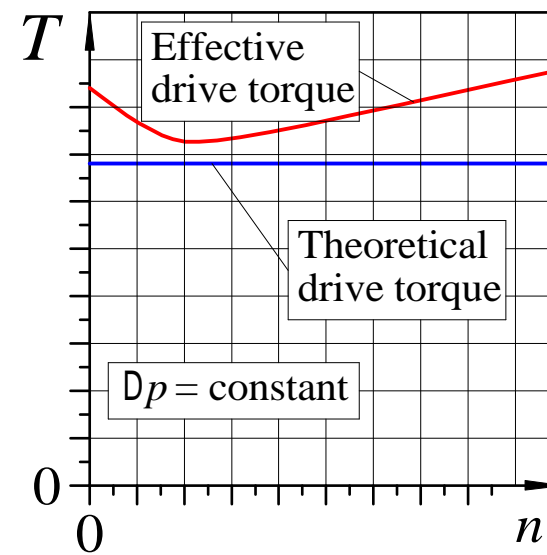
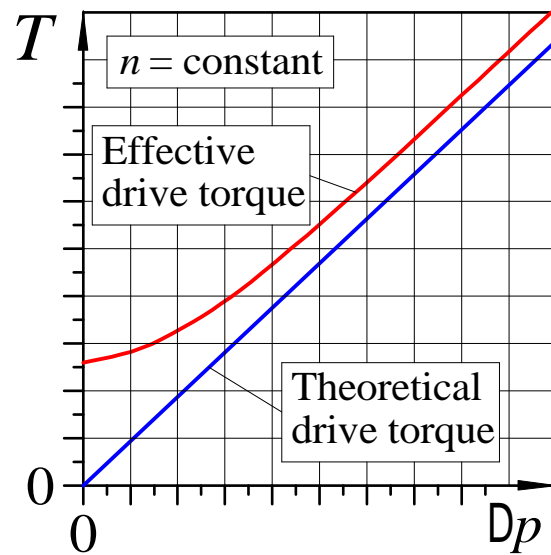


- Higher pressure**
- Wider clearances
  - Thicker fluid film
  - Better lubrication



- Effect of  $n$**
- At first Coulomb friction dominates
  - Then better lubrication
  - Finally hydraulic losses increase

## Theoretical drive torque – Effective drive torque



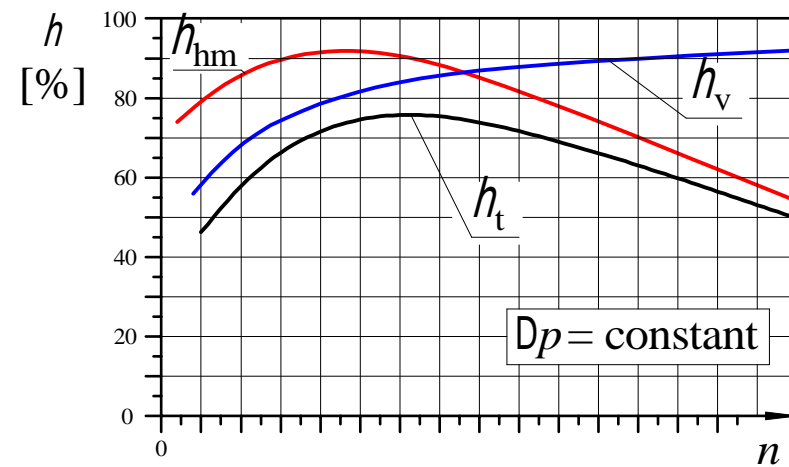
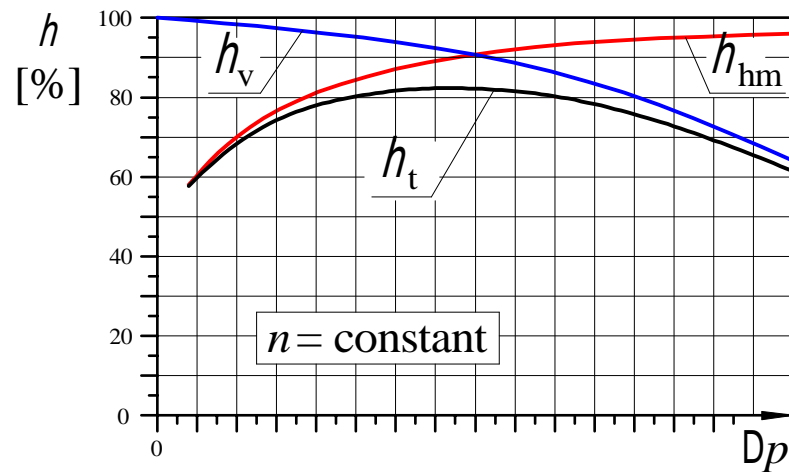
Theoretic drive power

$$P_{\text{theor}} = q_V \Delta p$$

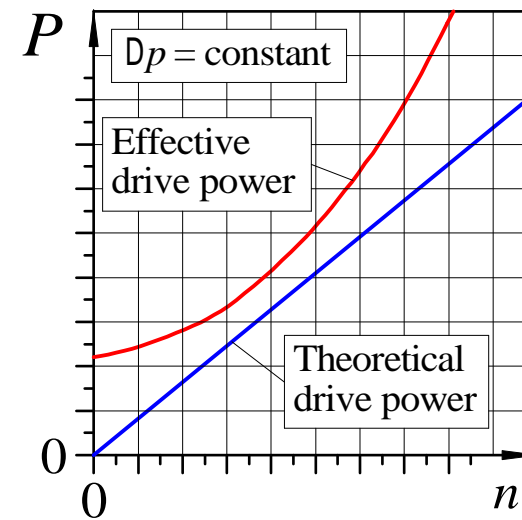
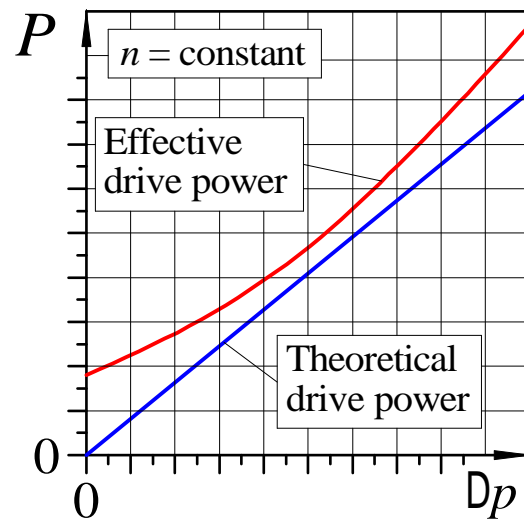
Effective drive power

$$P_{\text{real}} = \frac{q_V \Delta p}{h_t}$$

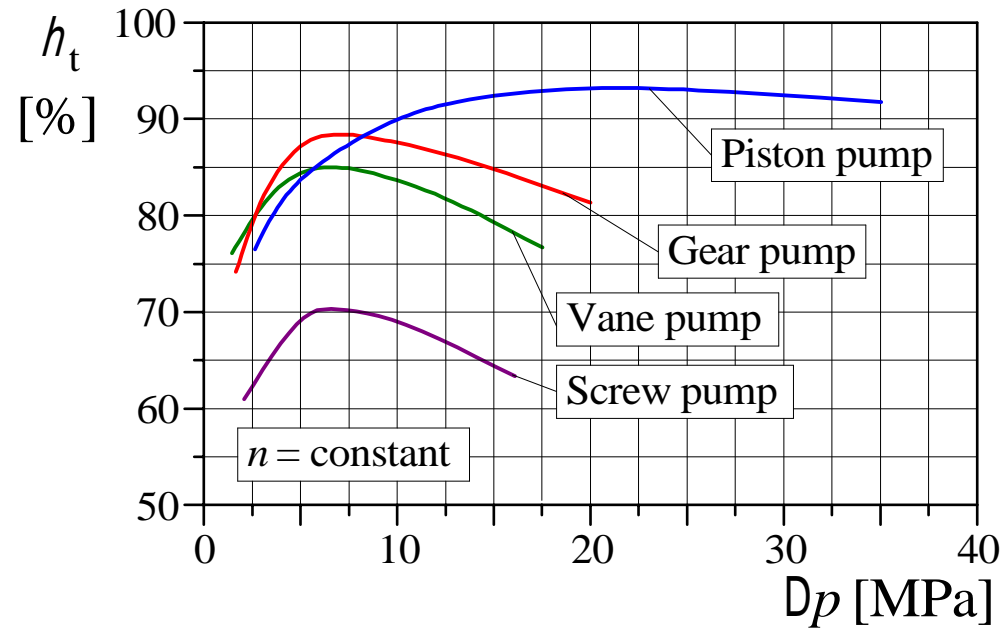
$$h_t = h_v \Delta h_{\text{hm}}$$



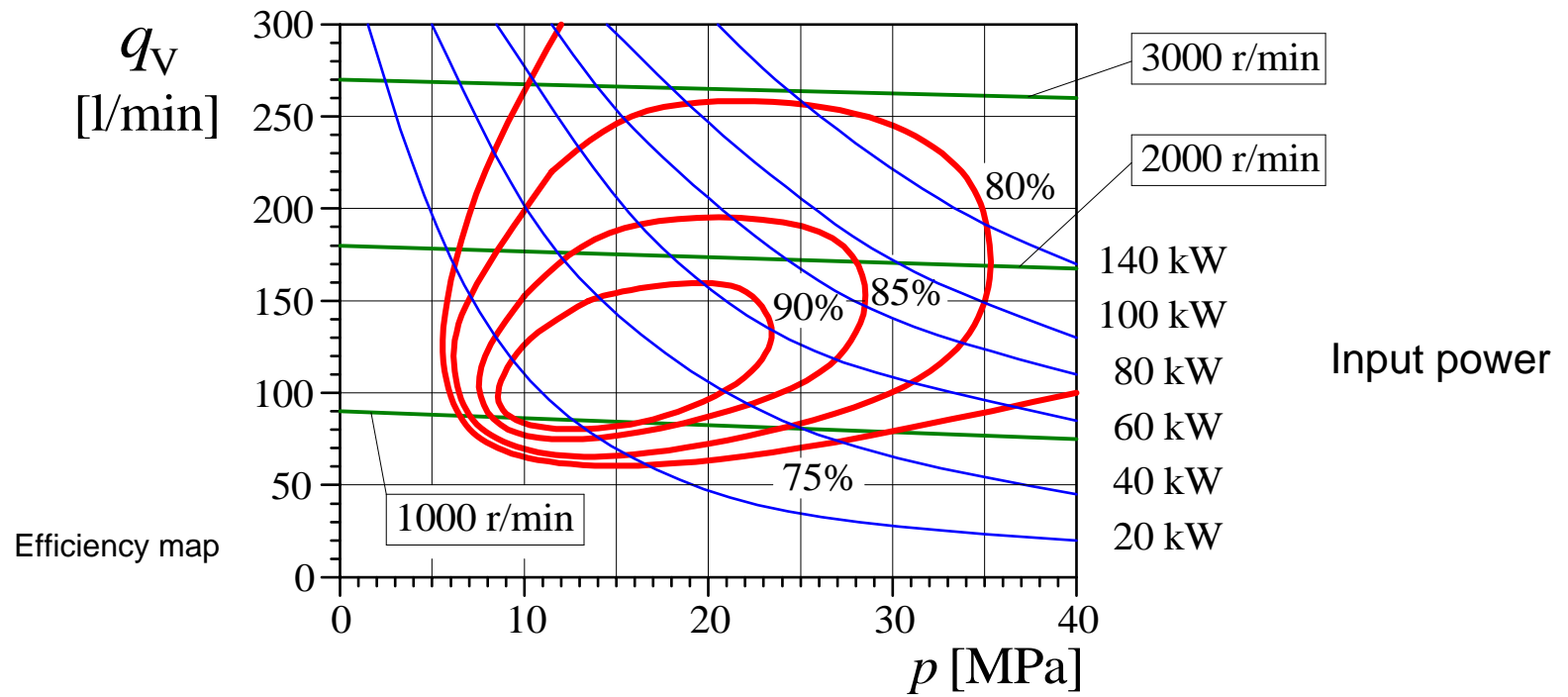
## Theoretical drive power – Effective drive power



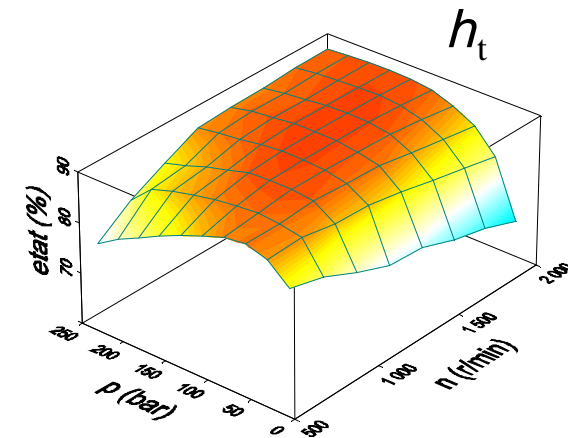
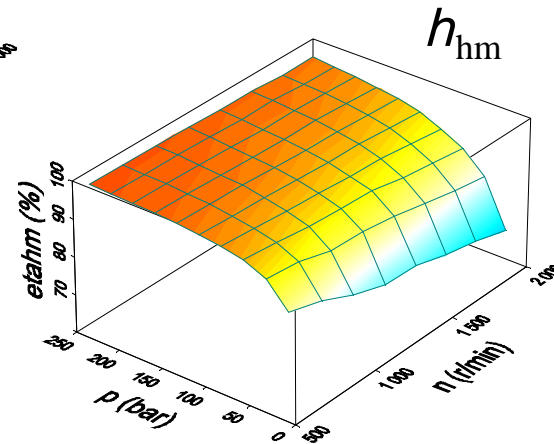
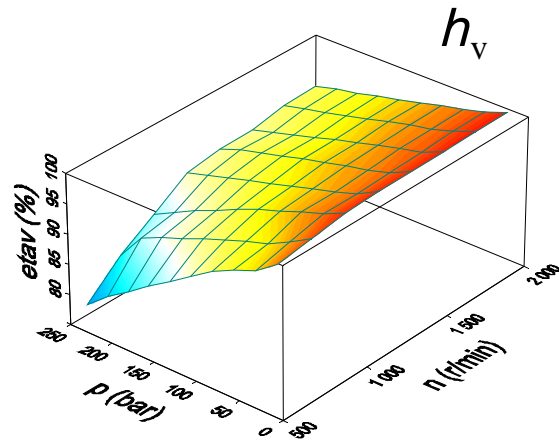
## Comparison of structure types



## Characteristic curves of pump



Example:  
Pressure-rotational speed-  
dependency of axial piston  
pump



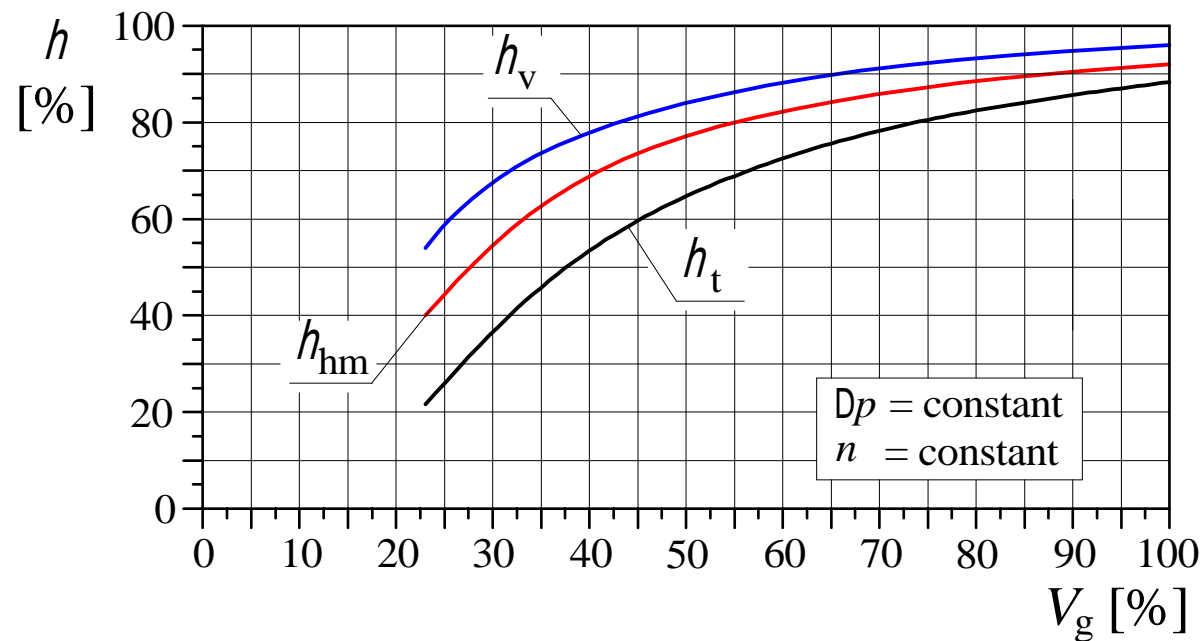


$$T = \varepsilon \frac{V_i \Delta p}{2\pi} + C_f \frac{V_i \Delta p}{2\pi} + C_v V_i n v \rho + T_c \quad \leftarrow \text{Wilson's model (check the effect of decreasing } \varepsilon)$$

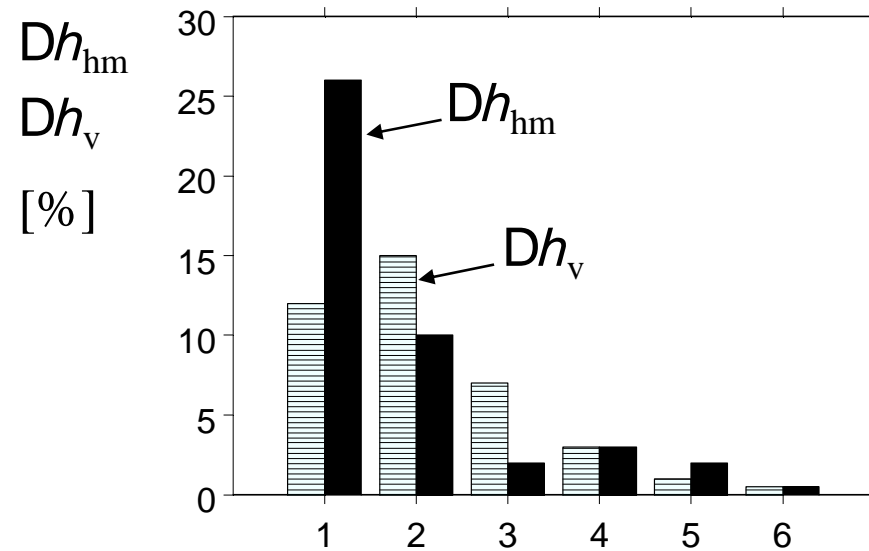
$\varepsilon$  Pump angle set value (0 - 1) (axial piston pumps)

$$q_{v2} = \varepsilon V_i n - C_s \frac{V_i \Delta p}{2\pi v \rho}$$

Effect of displacement setting value to the efficiencies in variable displacement pumps



## Factors affecting efficiency



1: pressure      2: swept volume      3: rotational speed  
4: temperature      5: pump specimen      6: fluid

# Pump types

## **Gear pumps**

- external gear
- internal gear

## **Screw pumps**

## **Vane pumps**

- vanes in rotor
- vanes in stator

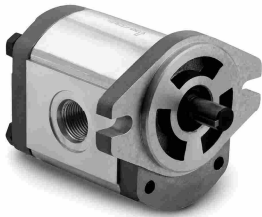
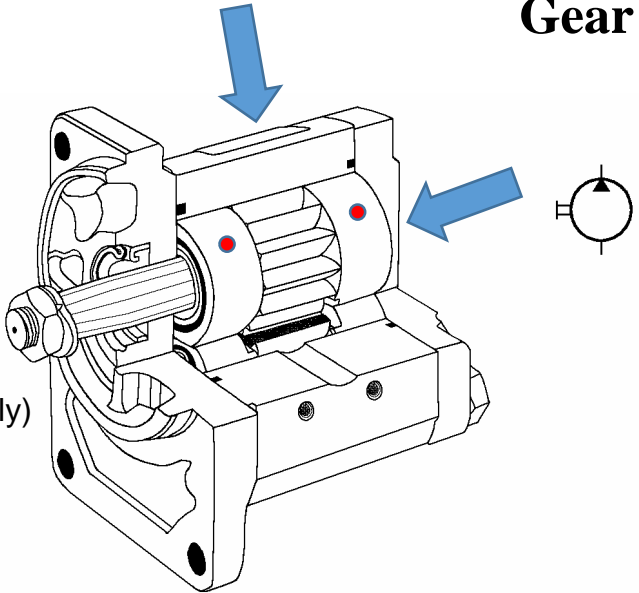
## **Piston pumps**

- line piston pumps
- radial piston pumps
- axial piston pumps

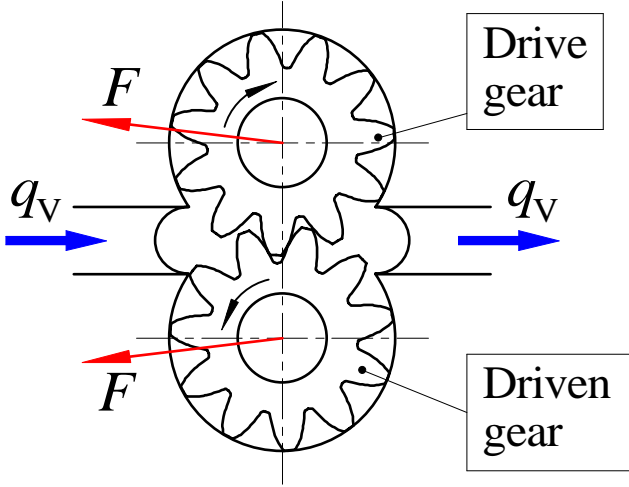
# Gear pumps

Reduction of leakage by  
 - axial gap compensation  
 - radial gap compensation  
 in some models

- Hydrodynamic bearings (typically)
- Roller bearings



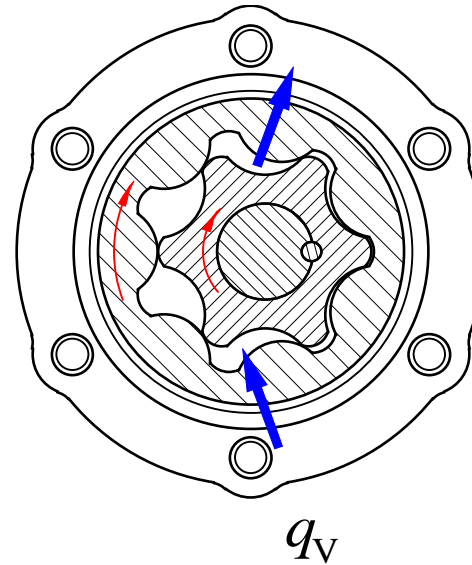
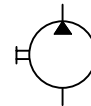
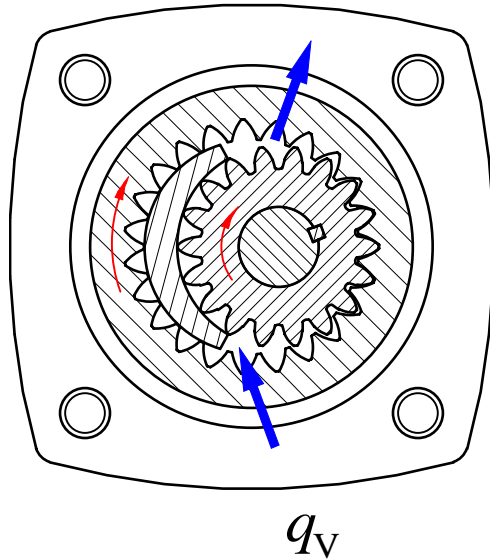
External gear  
 - two gear  
 - multi gear



Internal rotor  
External rotor

Axial compensation  
Radial compensation  
possible

- Low noise
- Even flow



Internal rotor  
External rotor

Also "roller rotor" design

## Internal gear

- crescent (segment pump)
- gerotor (ring pump)

## Performance characteristics of gear pumps

Total efficiency max.  $\eta_t \gg 0.8 - 0.93$

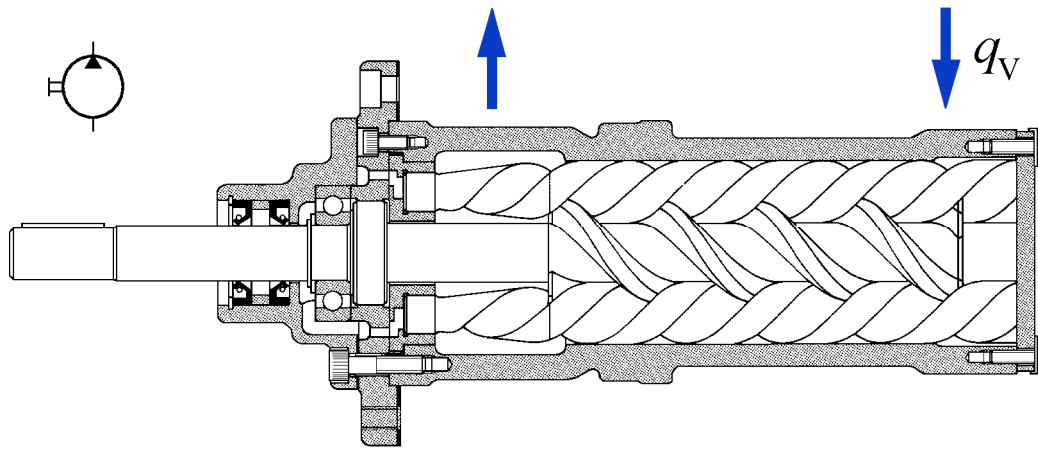
Rotational speed range  $n \gg 500 - 5000$  r/min

Operating pressure max.  $p \gg 14 - 21 (-32)$  MPa

- depends on compensation of leakage  
and radial forces

Screw crests roll against screw roots and seal fluid chambers

## Screw pumps



Fluid volumes do not change during movement  
- Even flow  
- Low noise  
- High rotational speeds possible

Number of screws

- one
- two
- three

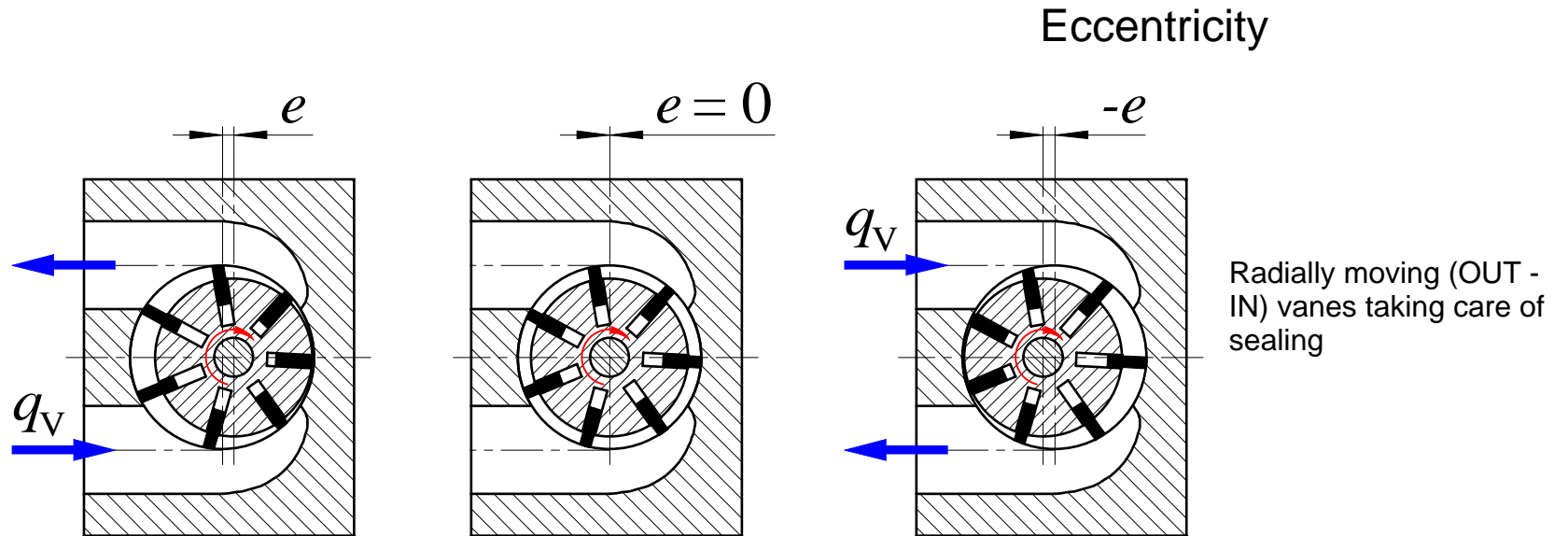
Total efficiency max.  $\eta_t \gg 0.7 - 0.8$

Rotational speed max.  $n \gg 30000$  r/min

Operating pressure max.  $p \gg 14 - 20$  MPa

By altering eccentricity of rotor the displacement and even the flow direction can be changed.

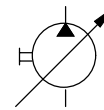
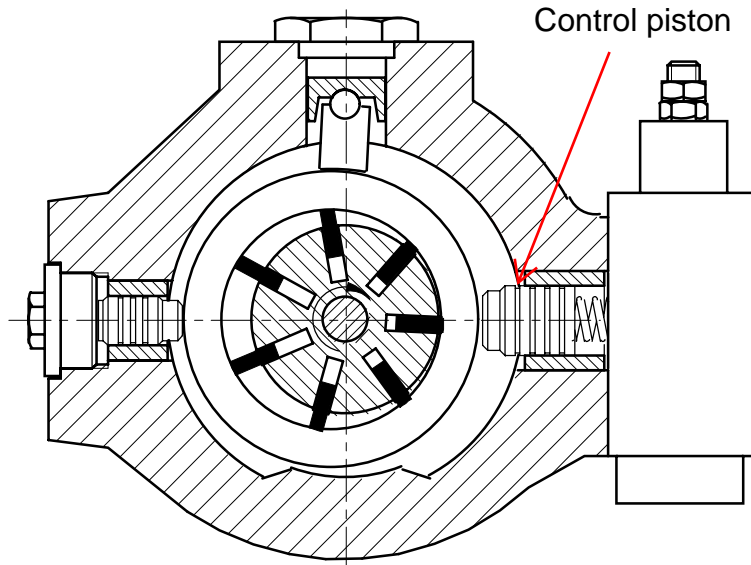
## Vane pumps



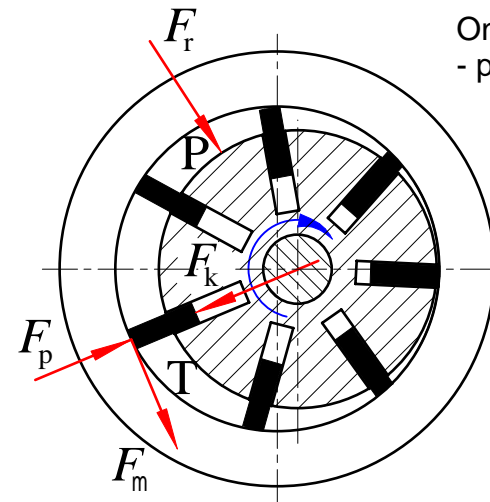
Vanes are pushed outwards to make a contact with the pump body  
- with extra force behind vane (spring or pressure)  
- "centrifugal force" (not a real force)



Variable displacement operation



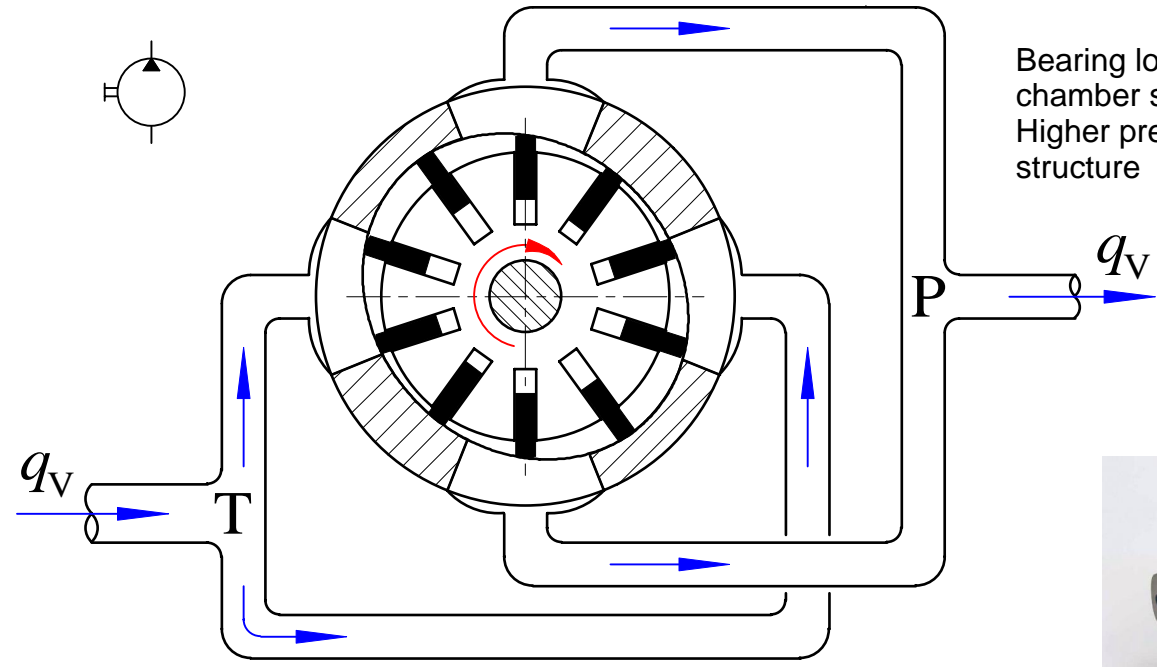
Vanes in rotor  
- one chamber



One chamber structure  
- pressure forces acting on the shaft

Even flow  
- low noise

Two chamber structure doubles the flow rate  
(compared with one chamber models)

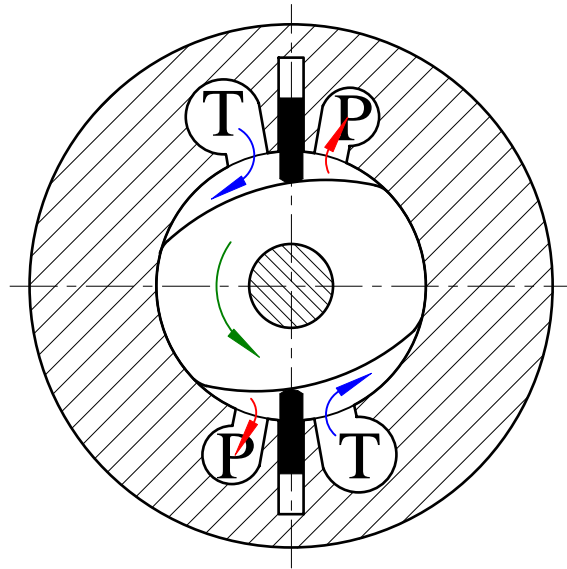


Bearing load forces are smaller than in one chamber structure  
Higher pressures possible than in one chamber structure

Variable displacement operation possible with two pump rings in series



Vanes in rotor  
- two chamber



Flow rate varies slightly more than in other structures

Vanes in stator

## Performance characteristics of vane pumps

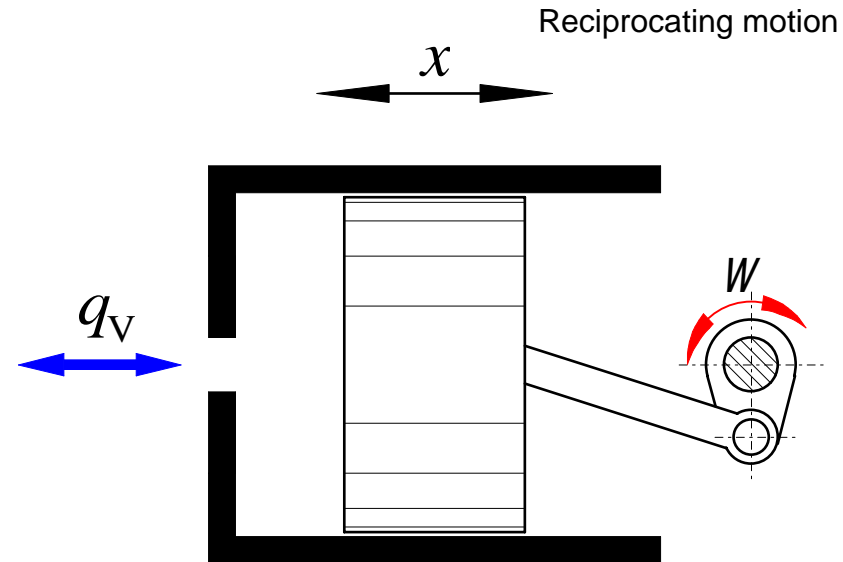
Total efficiency max.  $\eta_t \gg 0.8 - 0.92$

Rotational speed range  $n \gg 600 - 2500$  r/min

Operating pressure max.  $p \gg 7 - 14 (-18) (-21 - 28)$  MPa

- depends on compensation of leakage,  
radial forces and number of chambers

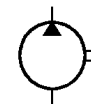
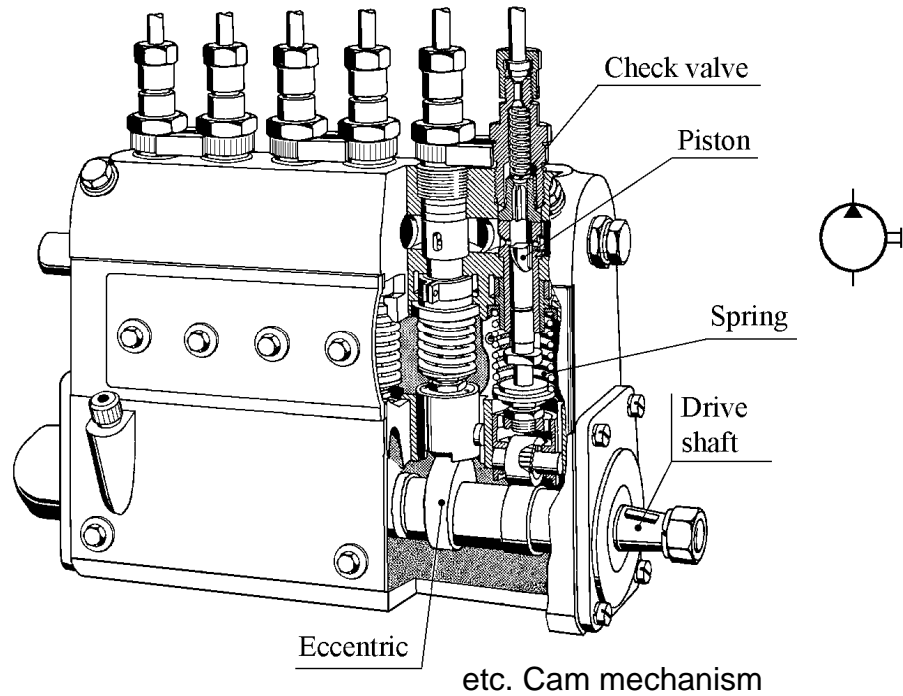
## Piston pumps



Piston pumps

- line piston pumps
- radial piston pumps
- axial piston pumps

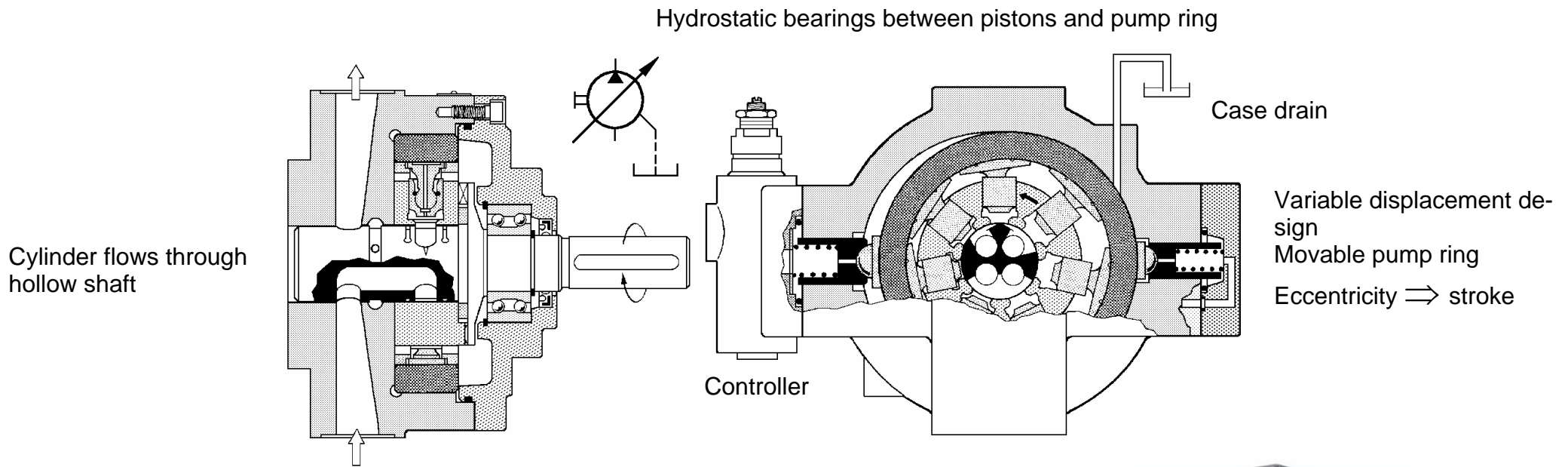
Small clearances  $\Rightarrow$  Small leakages  $\Rightarrow$  Good volumetric efficiency



Mainly for very high pressures  
 $\Rightarrow$  1200 bar  $\Rightarrow$  2500 bar



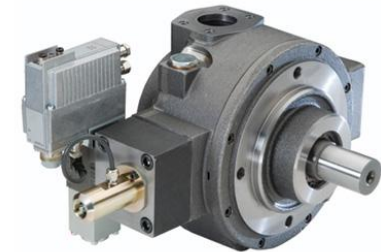
## Line piston pumps

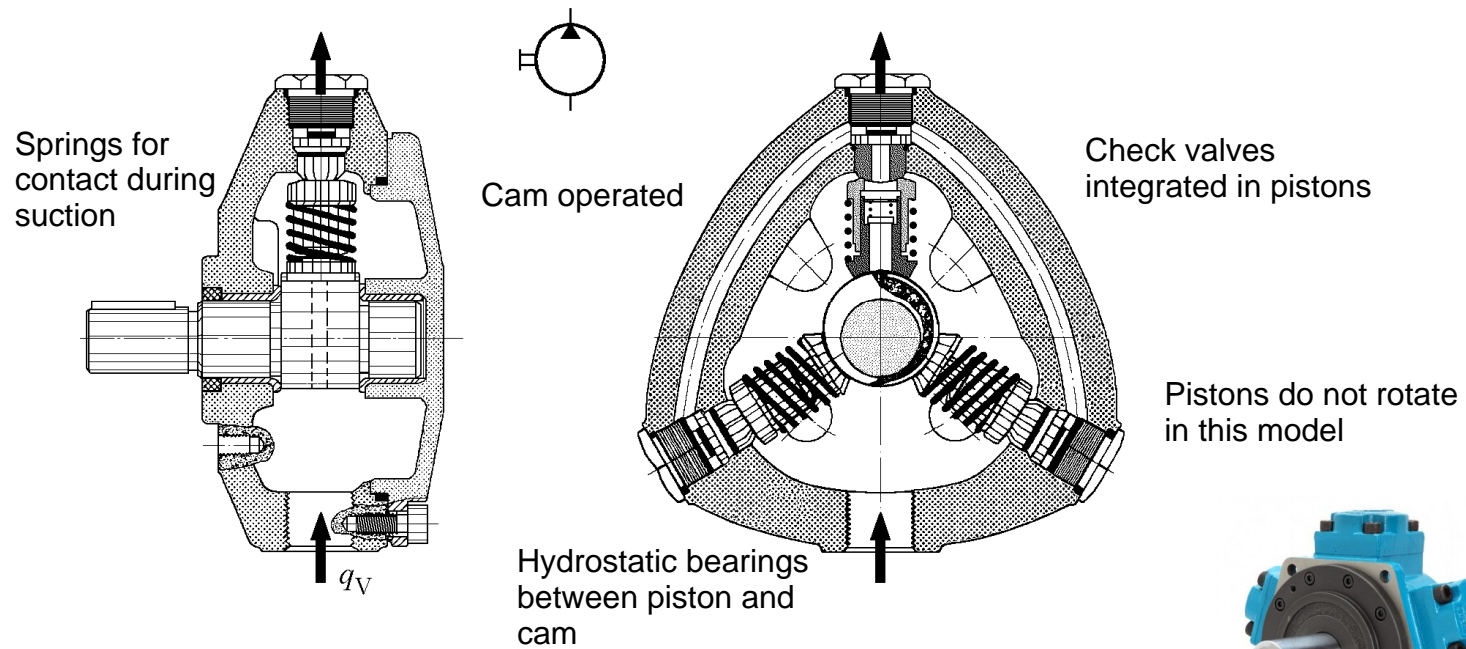


## Radial piston pumps

- internal flow channels
- external flow channels

High pressures possible up to 450 bar



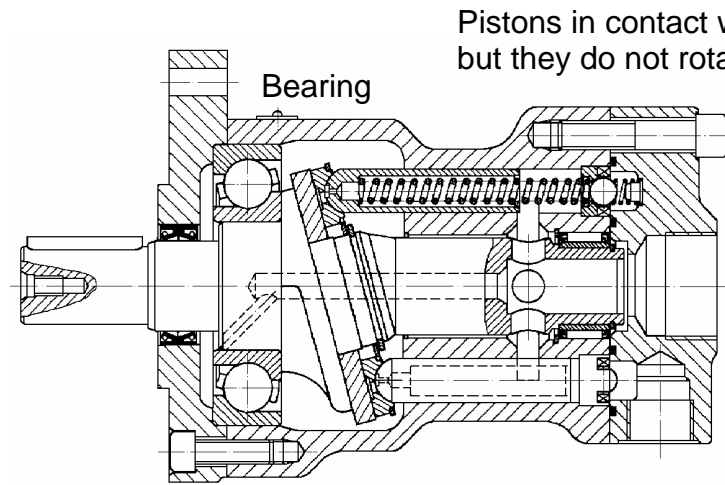


High pressures up to 600 - 700 bar possible



Radial piston pumps  
 - internal flow channels  
 - external flow channels





Pistons in contact with the plate,  
but they do not rotate

Bearing



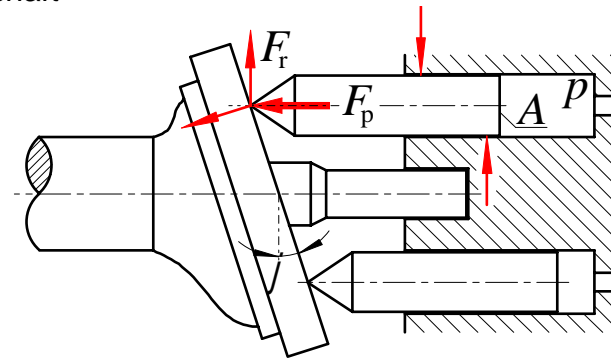
Possibility to transform this type to  
"digital" by disconnecting some of  
the pistons

The rotating masses are not in  
balance which limits the rotational  
speed

Without special arrangements the contact  
forces between piston and wobble plate  
cause radial forces to piston

Pistons in parallel with the shaft

Wobble plate rotates with shaft



Axial piston pumps

- wobble plate pumps
- swash plate pumps
- bent axis pumps

The direction of flow can be changed in some models

(-18° <sup>®</sup> ) 0° <sup>®</sup> +18°

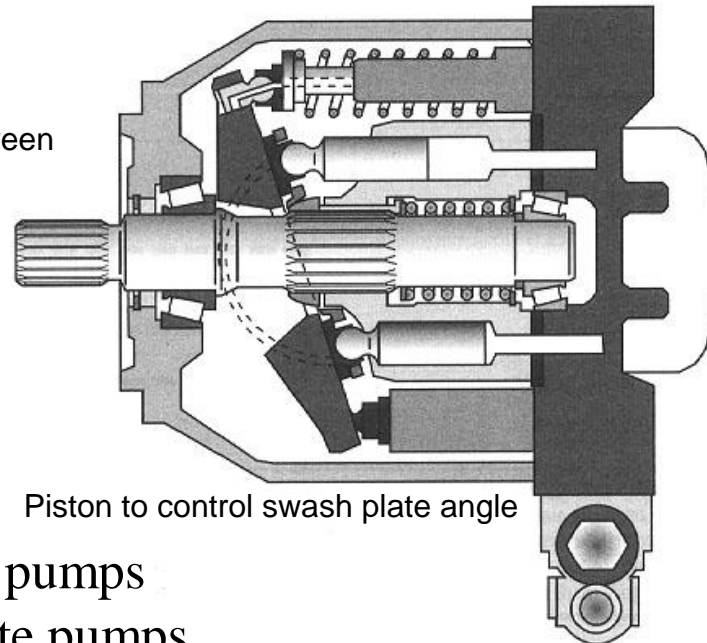
Contact forces between pistons and swash plate limit the control angle

Rotational speeds can be 1500 - 3000 rpm

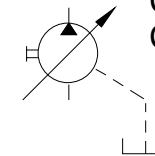
Cylinder block rotates with the shaft  
Swash plate does not rotate, it can turn to control the piston stroke and pump displacement

Counter piston for swash plate control

Hydrostatic bearing between pistons and swash plate



Piston to control swash plate angle

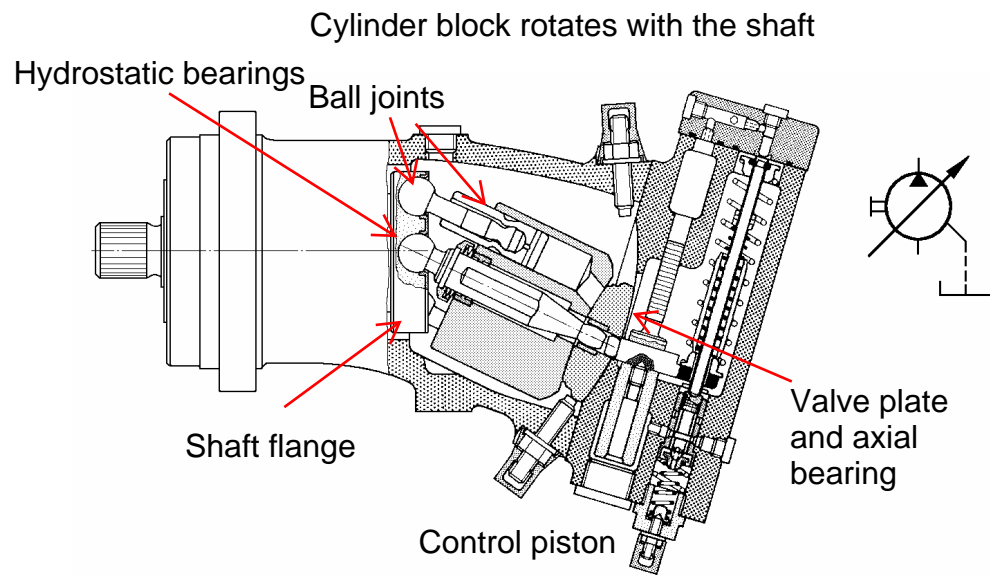


Case drain because of hydrostatic bearings  
Case pressure must be kept small!

Axial piston pumps

- wobble plate pumps
- **swash plate pumps**
- bent axis pumps

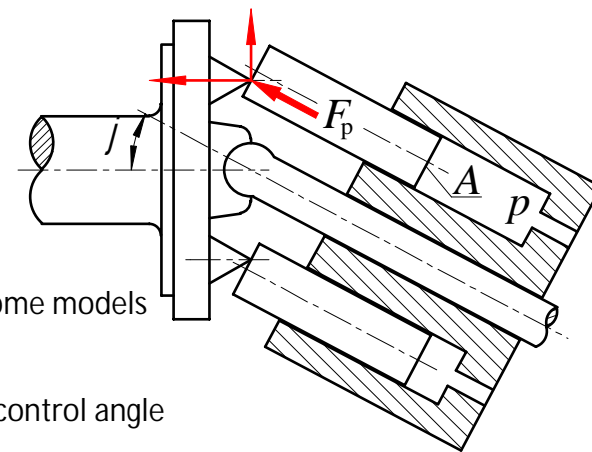
swashplate pump - inline piston pump



Size is typically large especially with controllers

- Rotation transmitted with
- Cardan shaft
  - Bevel gear
  - Pistons

Radial forces on piston are small



## Axial piston pumps

- wobble plate pumps
- swash plate pumps
- bent axis pumps

The direction of flow can be changed in some models  
 (-25°  $\text{\textcircled{R}}$  ) 0°  $\text{\textcircled{R}}$  +25°

Contact forces of pistons do not limit the control angle as much in this model  
 Rotational speeds can be 800 - 8000 rpm

## Performance characteristics of piston pumps

Total efficiency max.  $\eta_t \gg 0.8 - 0.9$  even higher

Rotational speed range  $n \gg 300 - 8000$  r/min

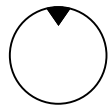
Operating pressure max.  $p \gg 20 - 35$  (– 45) (– 70) (– 250) MPa  
- depends on structure type

# Hydraulic motors

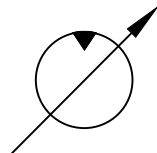
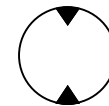
Convert hydraulic power into mechanical power

Unidirectional

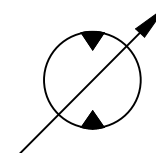
Bidirectional



Constant displacement



Variable displacement



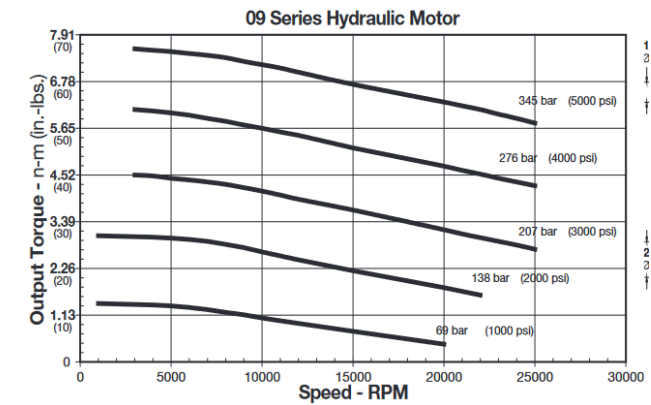
## Speed ranges and structures

Speed range	r/min
Slow	1- 150
Middle	10- 750
High	300- 5000



Most common construction types:

- gear
- vane
- piston

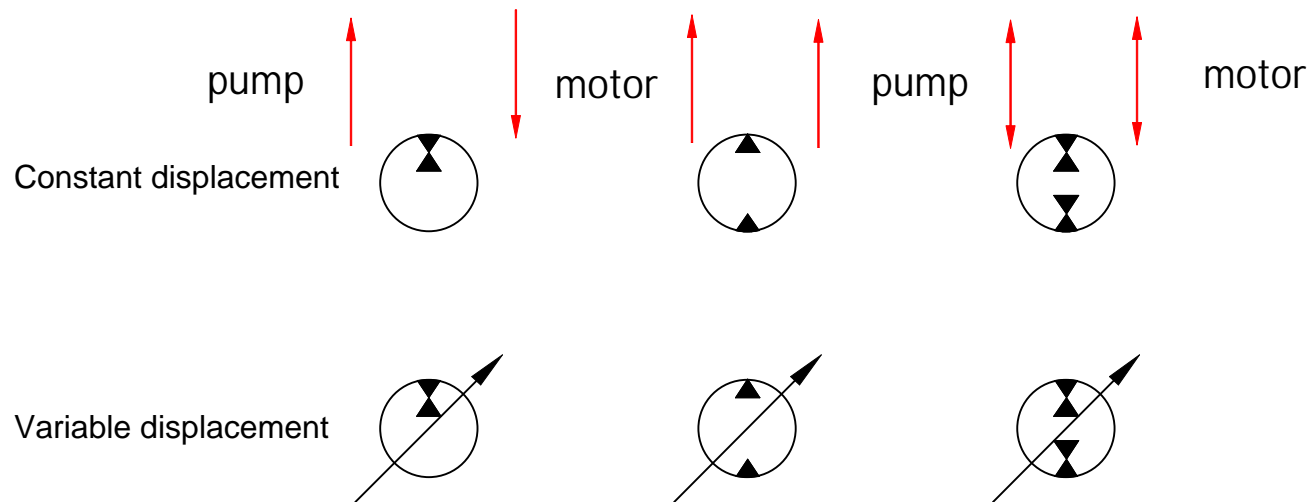


Parker Oildyne 09 gear motor

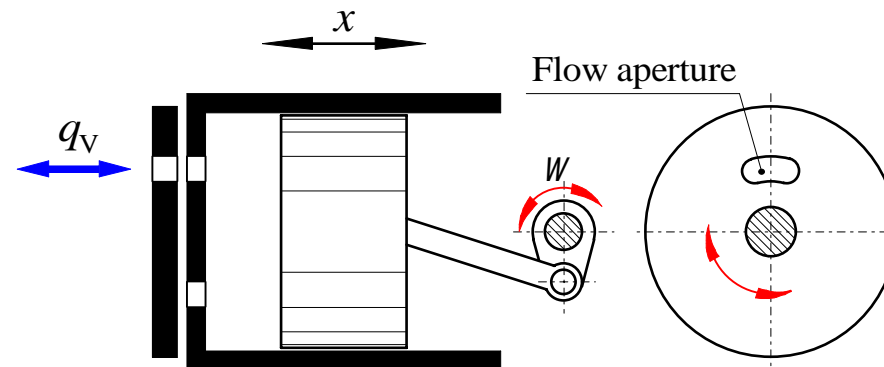
All operate on positive displacement principle

<http://www.parker.com/literature/Oildyne/Oildyne%20-%20PDF%20Files/07%20-%2009%20Series%20hydraulic%20gear%20motors.pdf>

## Pump-motors



## Control of flow direction



Only forced control is applicable

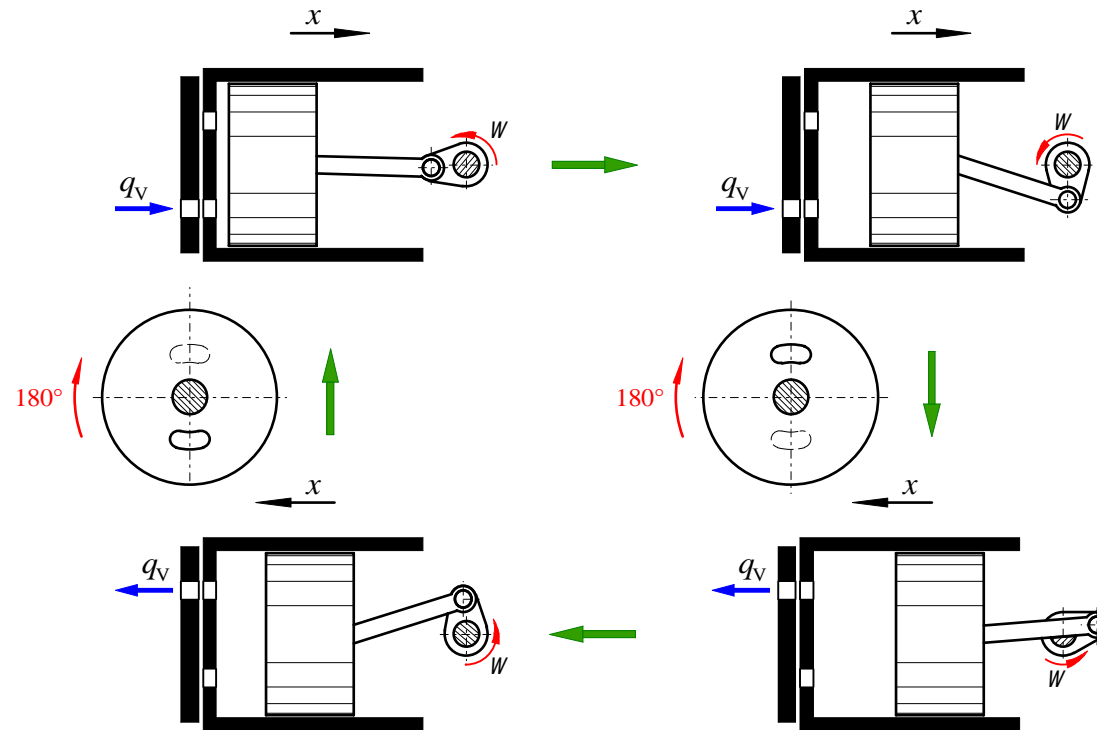
Operating phases:

Fluid flows into transfer volume – work phase

Fluid flows out from volume – free phase



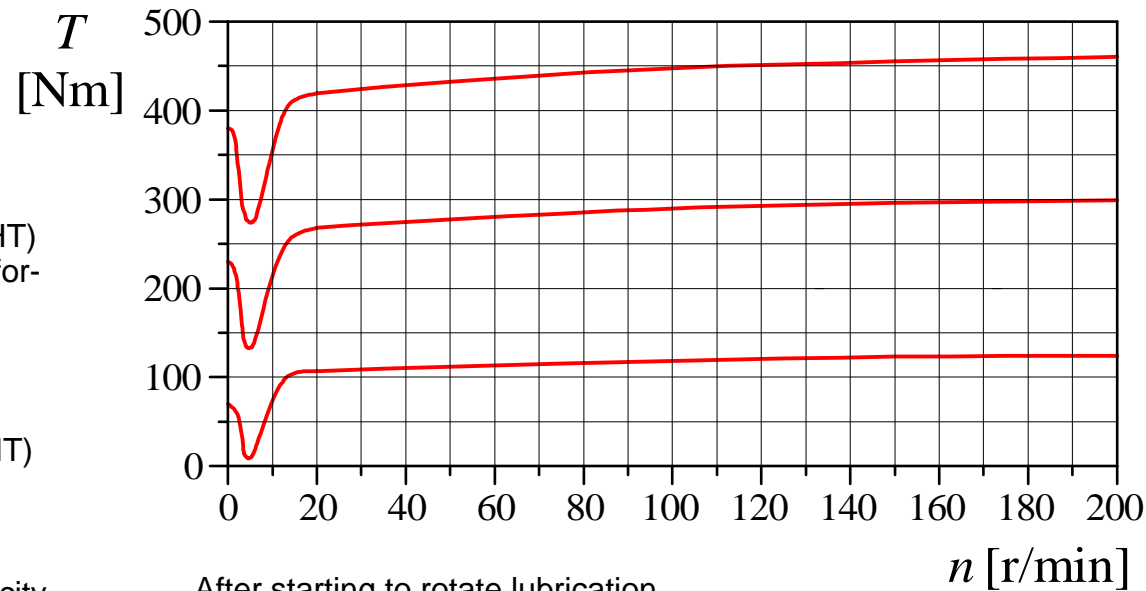
# Forced control



# Motor characteristics

## Starting characteristics

Especially at low rotational speeds  
the operation can be uneven  
a) rotational speed  
b) torque  
- displacement  
- leakage  
- friction (bearing type)  
change

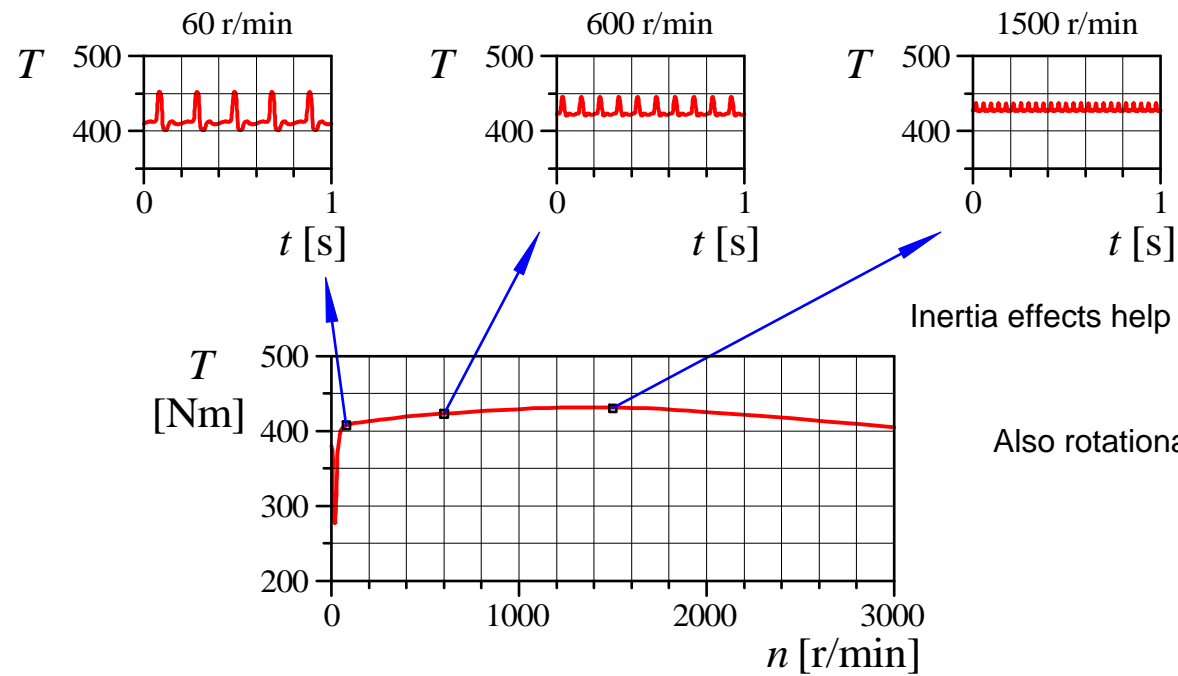


Low Speed High Torque (LSHT)  
motors have good quality performance at low speeds!  
Bearings  
hydrostatic - hydrodynamic  
Loading of motor?  
Full load at slow speeds (LSHT)

Higher speeds:  
- less (relative) leakage  
- inertia effects -> steady velocity

After starting to rotate lubrication  
problems with low speeds ->  
torque diminishes

## Running characteristics



Inertia effects help at high rotational speeds

Also rotational speed can be uneven

Theoretical flow demand  $q_{V,\text{theor}} = n \triangleright V_g$

Swept volume  $V_g$  [m<sup>3</sup>/r]

$$\text{cm}^3/\text{r} = 10^{-6} \text{ m}^3/\text{r}$$

Rotation speed  $n$  [r/s]

$$\text{r/min} = 1/60 \text{ r/s}$$

$$q_{V,\text{theor}} = \omega \triangleright V_{\text{rad}}$$

$$\omega = 2\pi \triangleright n$$

Angular velocity  $\omega$  [rad/s]

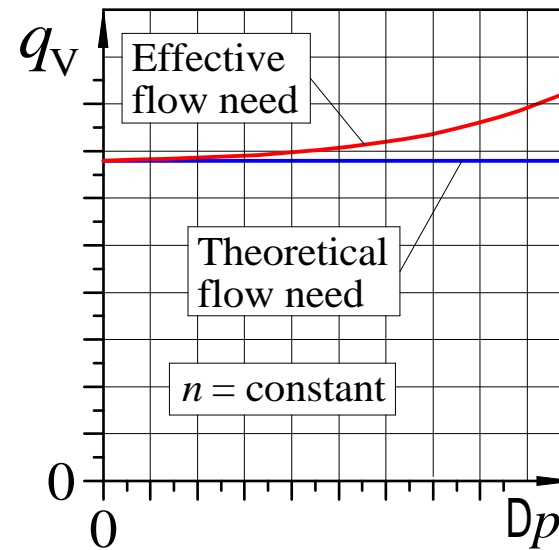
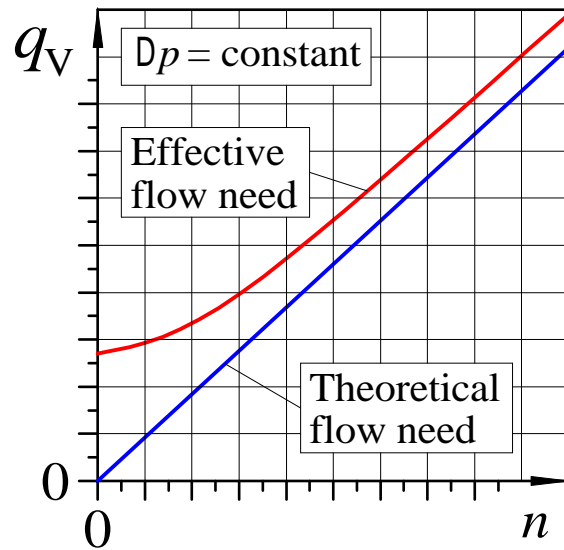
$$V_{\text{rad}} = \frac{V_g}{2\pi}$$

Swept volume per radian  $V_{\text{rad}}$  [m<sup>3</sup>/rad]

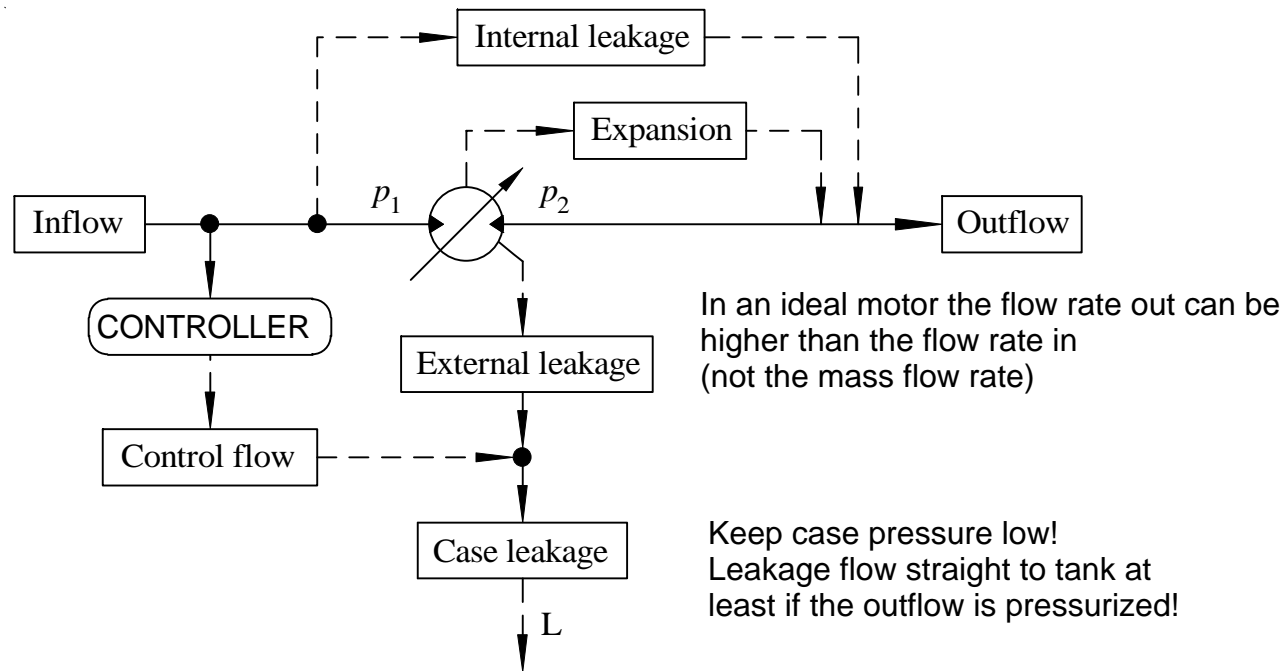
Effective flow demand

$$q_{V,\text{real}} = \frac{n > V_g}{h_v}$$

Leakage – volumetric efficiency  $h_v$



## Leakage flows in motors



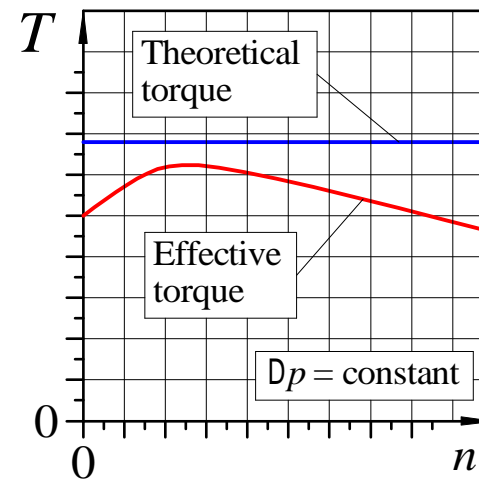
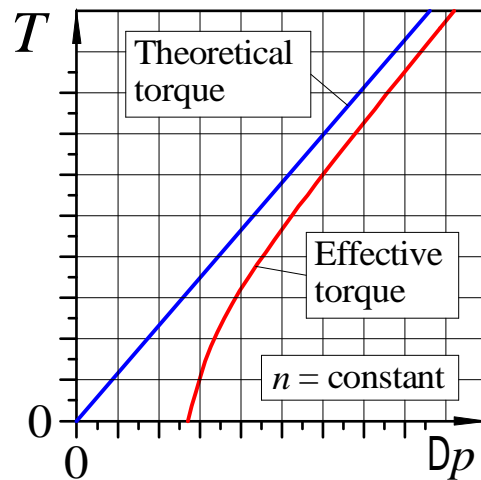
Theoretic pressure demand

$$Dp_{\text{theor}} = \frac{2 \rho g T}{V_g}$$

Effective pressure demand

$$Dp_{\text{real}} = \frac{2 \rho g T}{V_g \eta_{\text{hm}}}$$

Friction – hydro-mechanical efficiency  $\eta_{\text{hm}}$

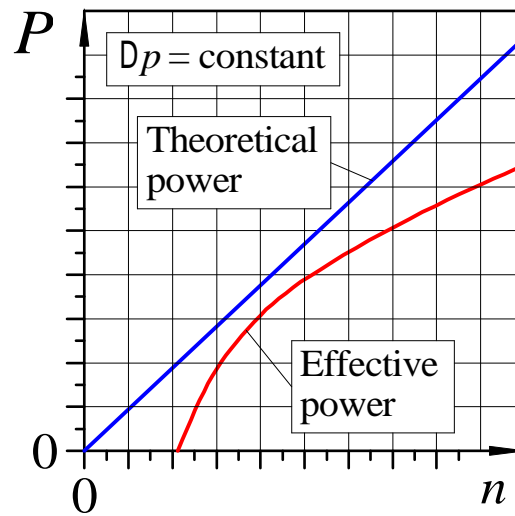
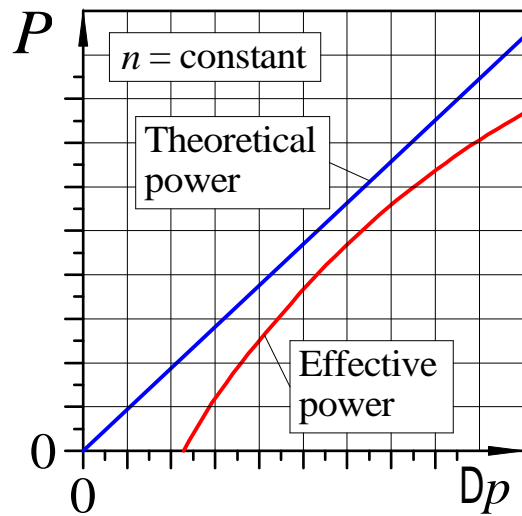


Theoretic power demand

$$P_{\text{theor}} = q_v \times \Delta p = T \times \omega$$

Effective power demand

$$P_{\text{real}} = q_v \times \Delta p = \frac{T \times \omega}{h_t} \quad h_t = h_v \times h_{\text{hm}}$$

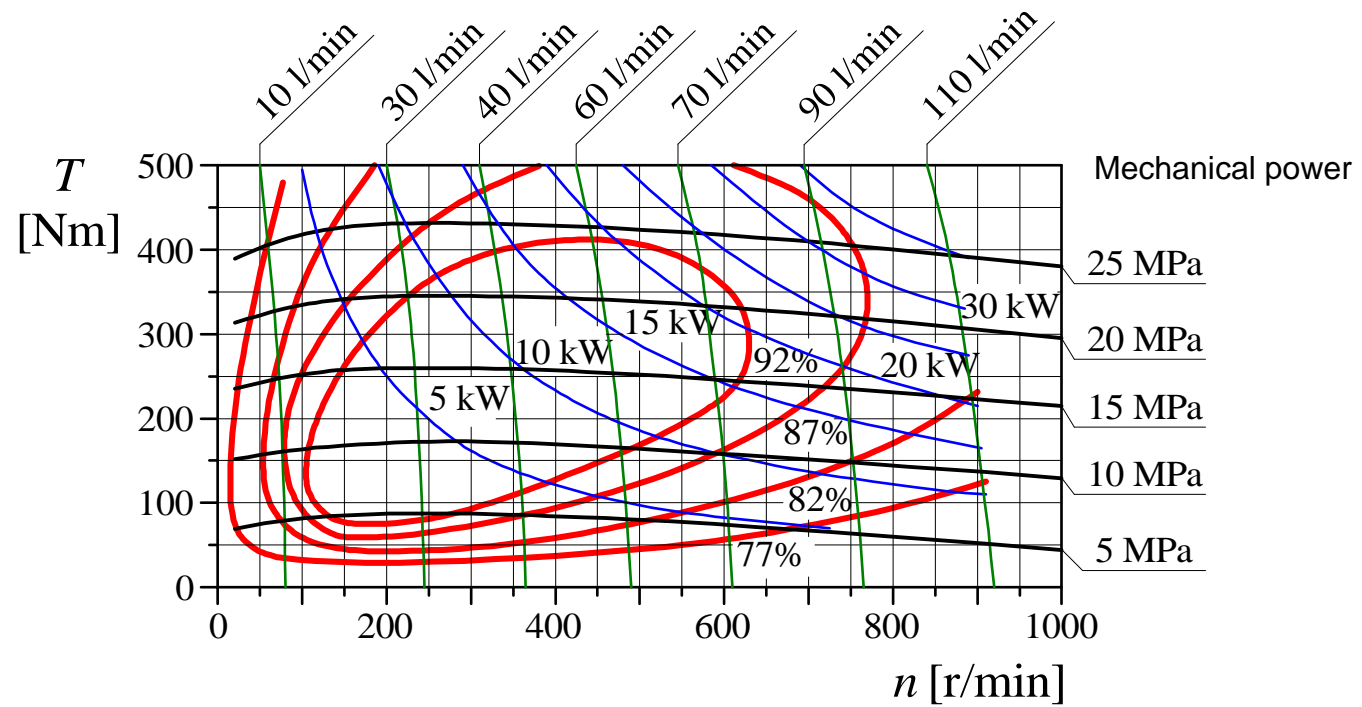


Power demand of load

$$P_{\text{mech}} = T \times \omega = 2 \times p \times n \times T$$



## Characteristic curves of motor



## Low speed high torque motors (LSHT)

Large swept volume

- large displacement area of working elements
- several work stages per one rotation of the axle

Radial piston motors

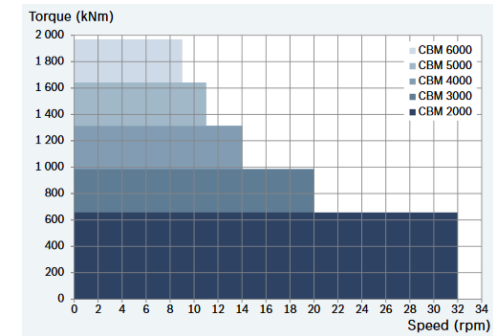
Vane motors with several chambers

Orbital motors

Total efficiency max.  $h_t \gg 0.8 - 0.92$

Rotational speed range  $n \gg 1 - 500 (-2400)$  r/min

Torque max.  $T \gg 1000 - 20000 (-125000)$  Nm



Maximum torque 1.97 MNm

Bosch - Rexroth Hägglunds

CBm radial piston motor

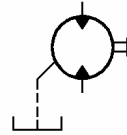
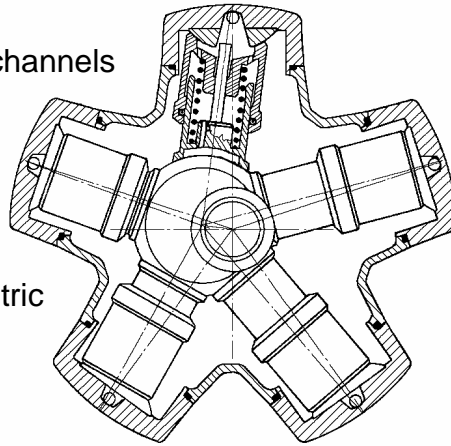
## Radial piston motors

- external flow channels
- internal flow channels

Hydrostatic bearings

External flow channels

Eccentric

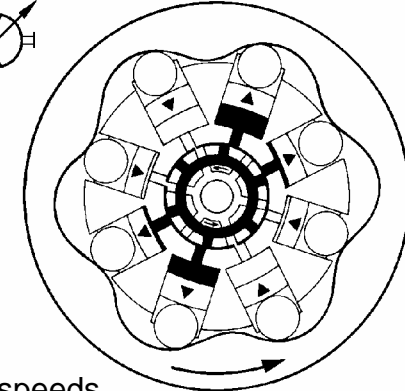
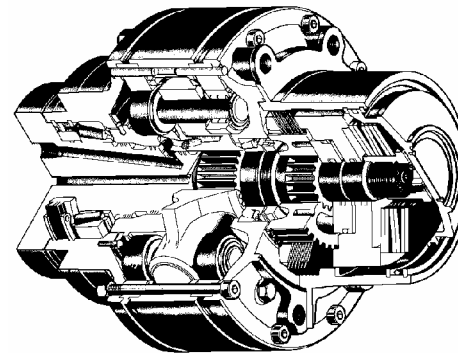


Case drain

Up to 420 bar



Internal flow channels

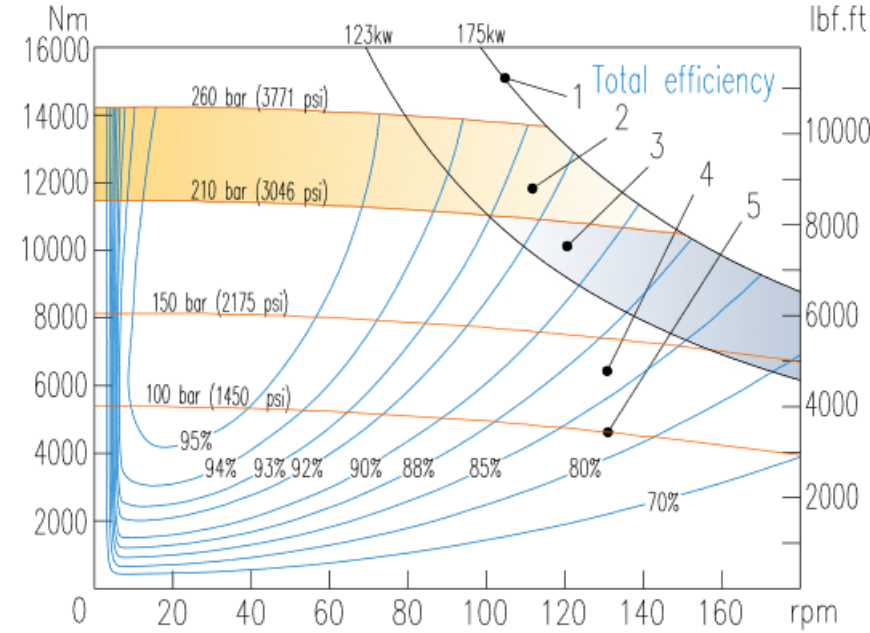


Cam mechanism, several cams for one revolution

Rotating housing

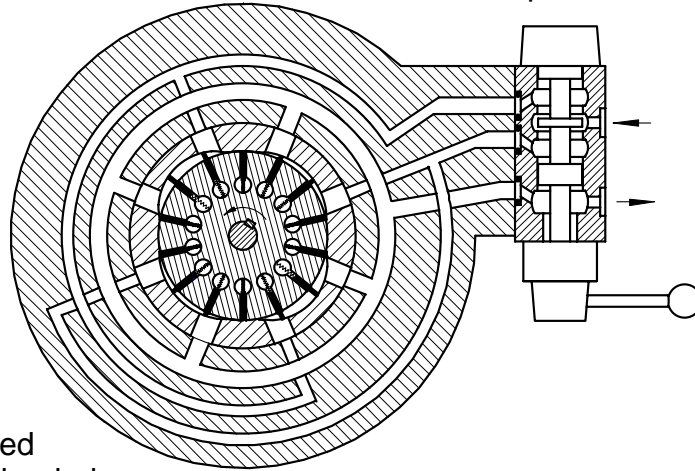
Opposite cylinder forces cancel internal bearing loadings

Can be freewheeled (springs) during on-road operation (trailer), 2 speeds



Stepwise change of displacement

Three displacements: 1, 2 and 1+2



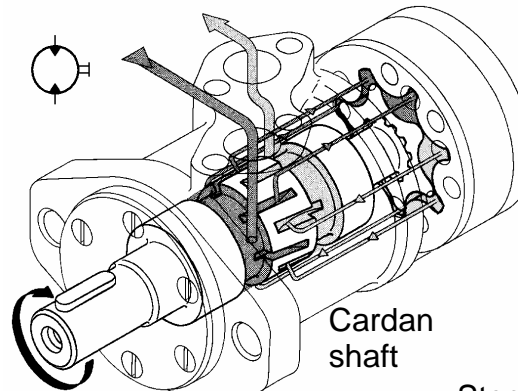
Multi chamber vane motor

<http://files.danfoss.com/documents/52010262.pdf>

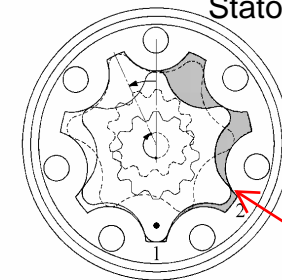
4 chamber model  
Radial forces cancelled  
Spring and pressure loaded vanes

Drum distributor valve (or disc valve)

Orbital motor ®



External gear  
Stator, 7 cams



For one rotation 42 tooth volumes have to be filled

Rotor, 6 cams  
Internal gear

Models with rollers also

Stepwise displacement changes possible

## Middle speed range motors

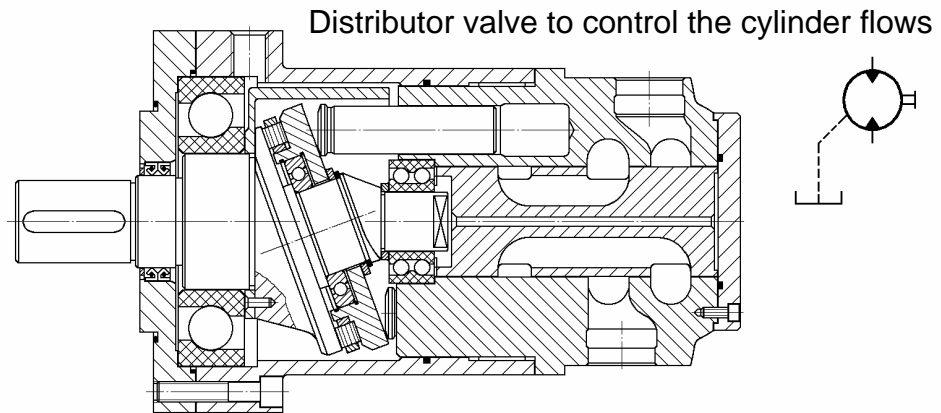
Gerotor motors (ring motors)

Wobble plate motors

Total efficiency max.  $h_t \gg 0.8 - 0.88$

Rotational speed range  $n \gg 200 - 1000 (-1500)$  r/min

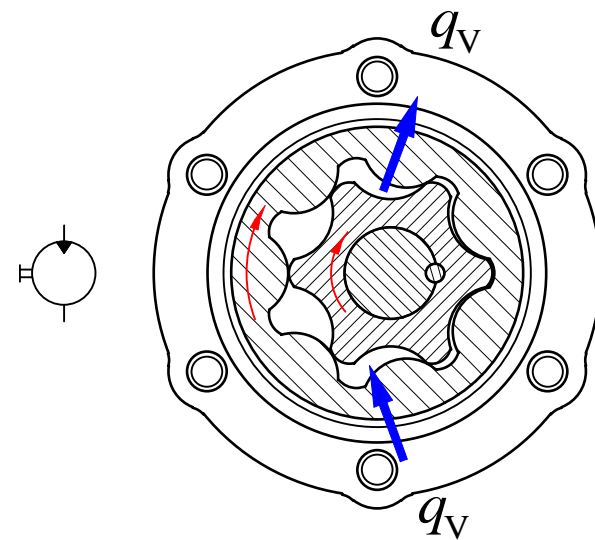
Torque max.  $T \gg 20 - 200 (-1200)$  Nm



Constant displacement  
 Medium speed because of rotor's mass imbalance

Gerotor motor (ring motor) ®

Wobble plate motors



## High speed range motors

External gear motors

Vane motors

Axial piston motors

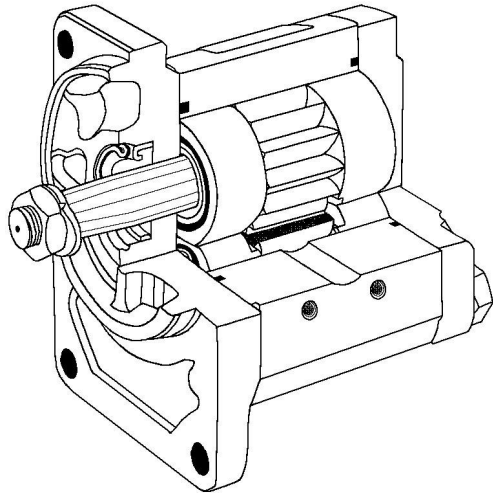
Total efficiency max.  $h_t \gg 0.82 - 0.9$

Rotational speed range  $n \gg 100 - 3000 (- 6000)$  r/min

Torque max.  $T \gg 10 - 700 (- 3000)$  Nm

Rotational speed may change frequently -> accelerations

Medium pressure (180 bar) unless radial compensation (250 bar)



External leakage connection needed if outlet flow is pressurized

→ External gear motor

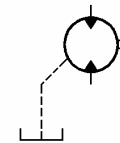
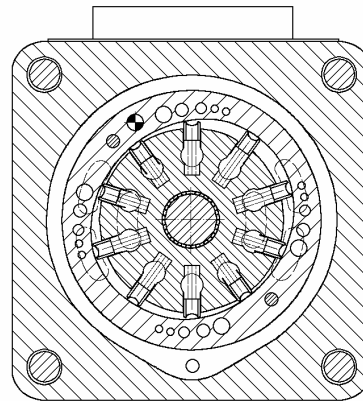


Some models with needle bearings for better performance at low speeds

Vane motor ®

Medium pressure (up to 210 bar)

Constant or variable displacement



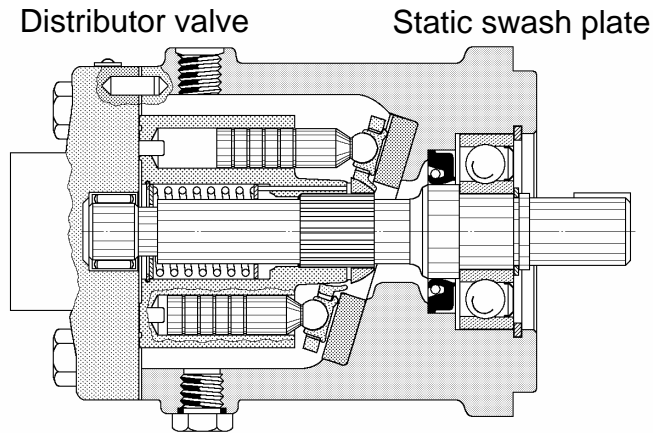
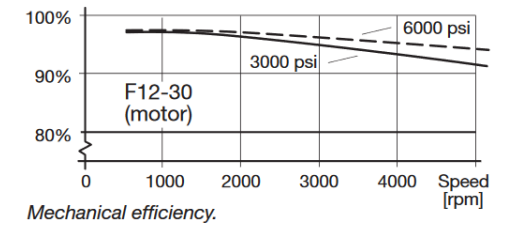
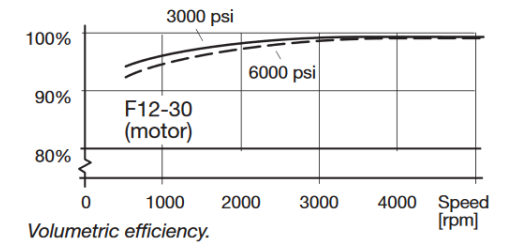
Hydraulic forces in balance

External leakage connection for pressurizing of both flow channels





Parker F12 bent axis motor



Up to 350 bar  
High efficiency

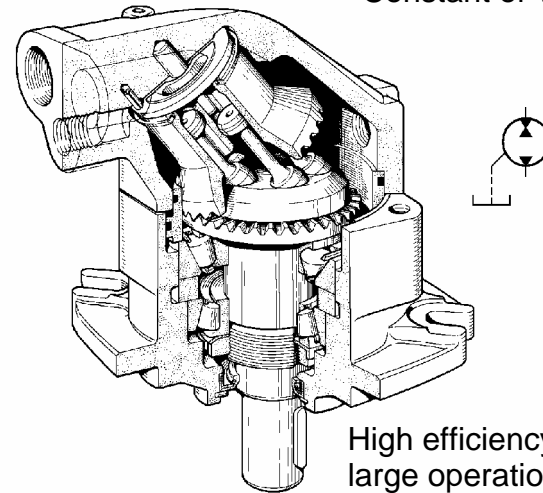
Constant or variable displacement  
In variable models typically 7°-18° control angle

Limited by radial forces (large) and and weakening of hydromechanical efficiency (small)

Bent axis <sup>®</sup>  
piston motor

Swash plate  
piston motor

Distributor valve Constant or variable displacement



In variable models typically large 8°-25° control angle (up to 40°)

Up to 400 bar

High efficiency at large operational area



# Hydraulic cylinders

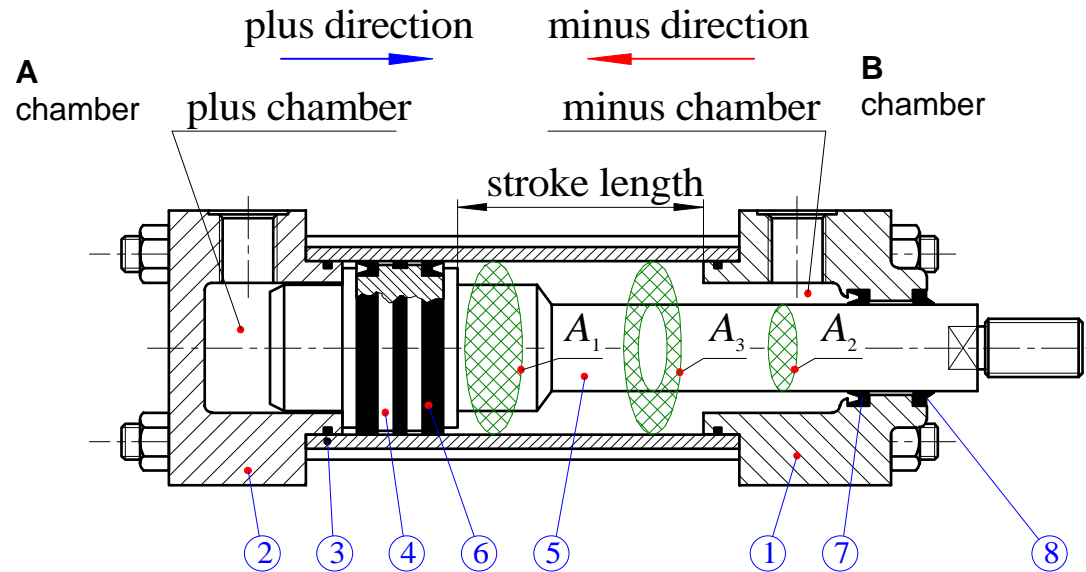
Convert hydraulic power into mechanical power

Construction types:

- single acting
- double acting

Both operate on positive displacement principle

# Terminology

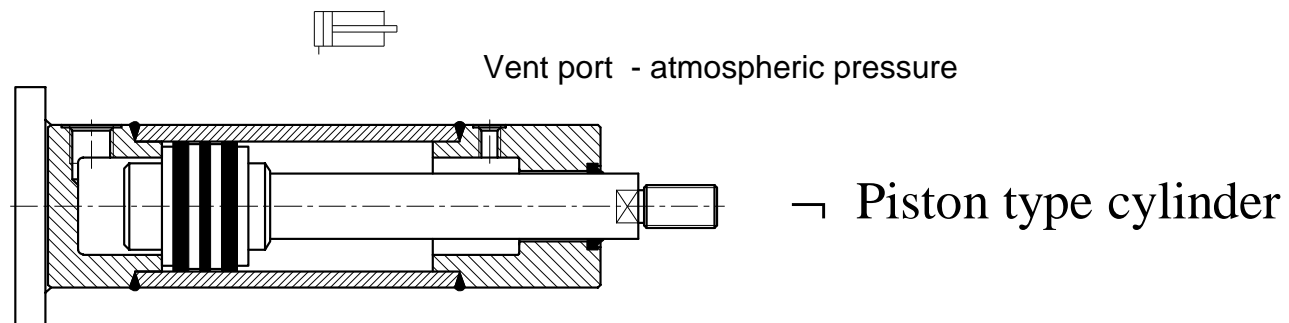


- |                    |                    |                          |
|--------------------|--------------------|--------------------------|
| 1. Head with inlet | 2. Cap with inlet  | 3. Cylinder tube         |
| 4. Piston          | 5. Piston rod      |                          |
| 6. Piston seals    | 7. Piston rod seal | 8. Piston rod wiper seal |

Plunger cylinder integrated in reach truck's mast

## Single acting cylinders

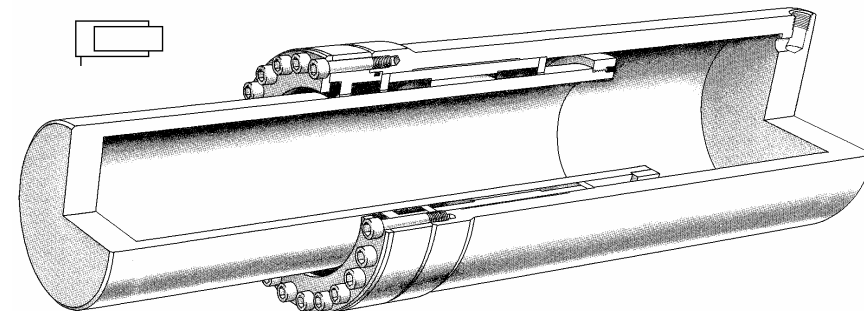
Operate hydraulically to only one direction



<http://www.rocla.com/en/products/roclas-humanic2-reach-trucks>



Plunger cylinder ®



These models are single acting

## Telescopic cylinder

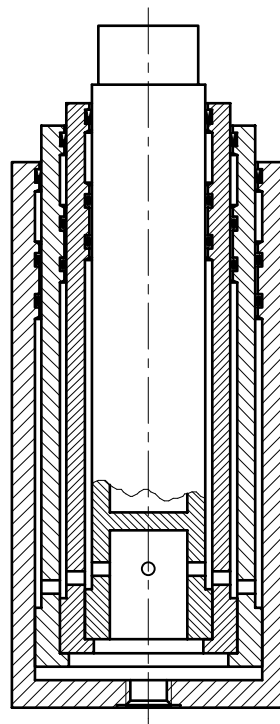
Variable speed

- the largest piston starts (the least pressure need)
- the smallest piston is the last (the highest pressure need)

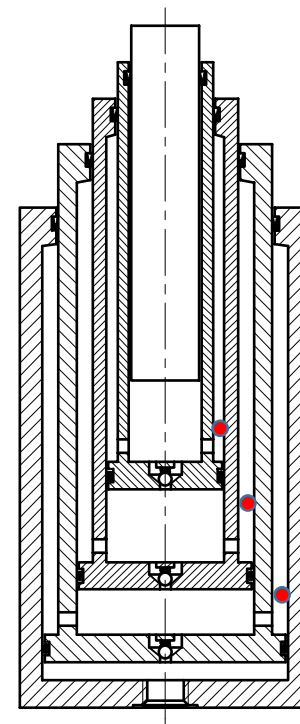
Used in dump trailers etc.



a



b

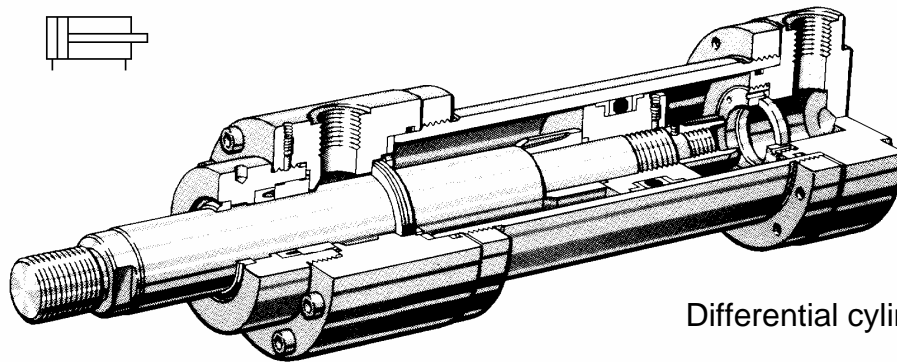


Constant speed telescopic cylinder  
All the pistons move at the same time

The movement of a piston forces the fluid from the space between the adjacent cylinders out to lift the next piston

[http://www.nurmihydro.fi/products\\_akipt.html](http://www.nurmihydro.fi/products_akipt.html)

## Double acting cylinders



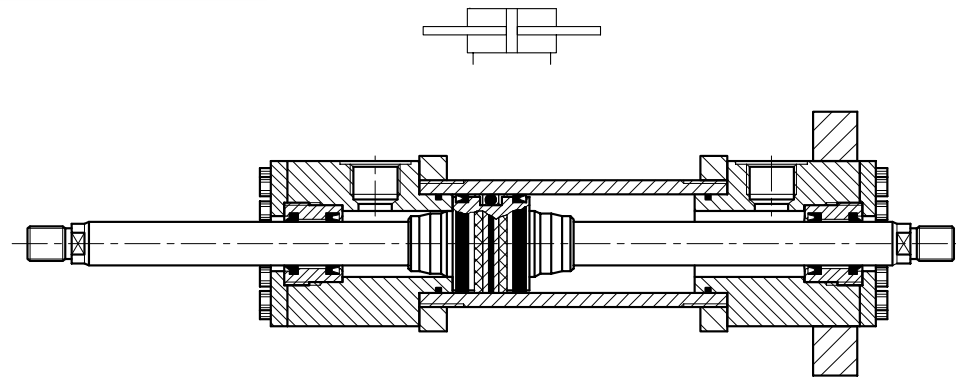
Differential cylinder



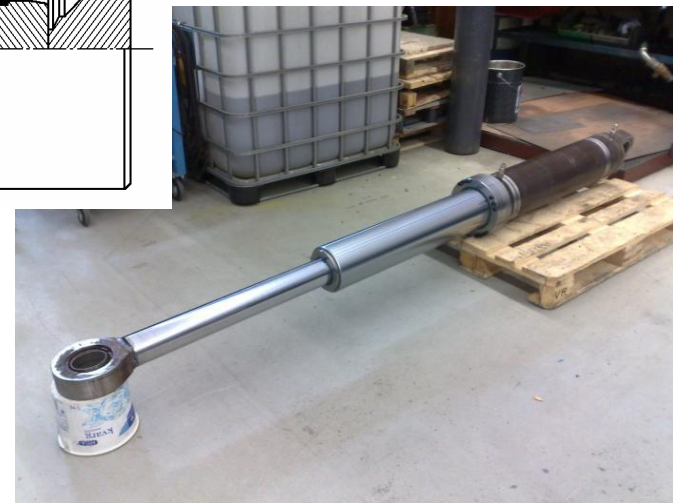
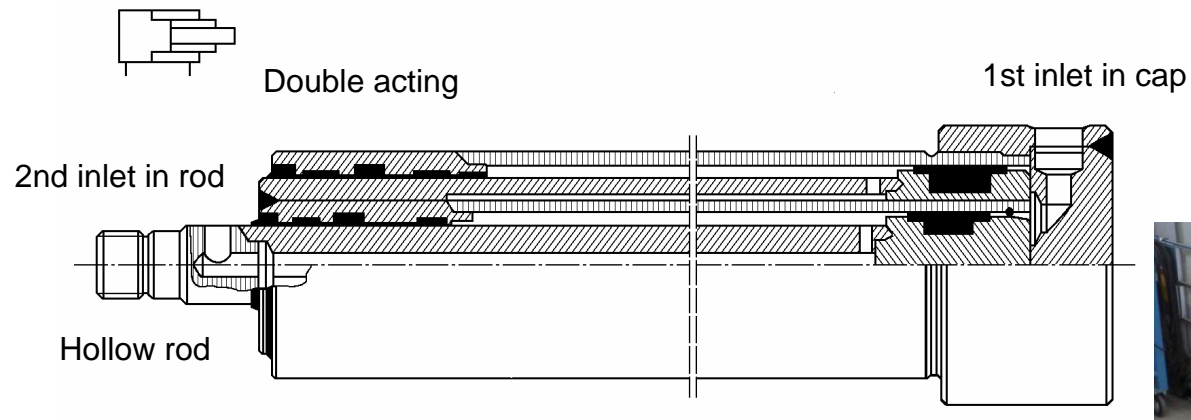
Single piston rod



Double piston rod  
Symmetric cylinder



# Telescopic cylinder



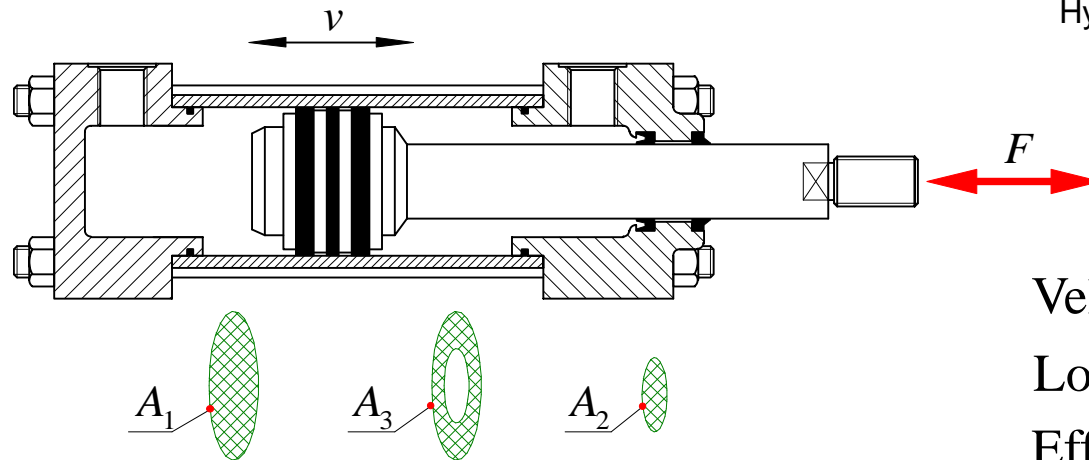
hydraulicpower.fi

## Characteristics of cylinders

Theoretic pressure demand  $p_{\text{theor, in}} \times A_{\text{in}} = F + p_{\text{out}} \times A_{\text{out}}$

Theoretic flow demand  $q_{V, \text{in, theor}} = A_{\text{in}} \times v$

Quasi-static process  
Hydraulic variables do not change



Velocity  $v$  [m/s]

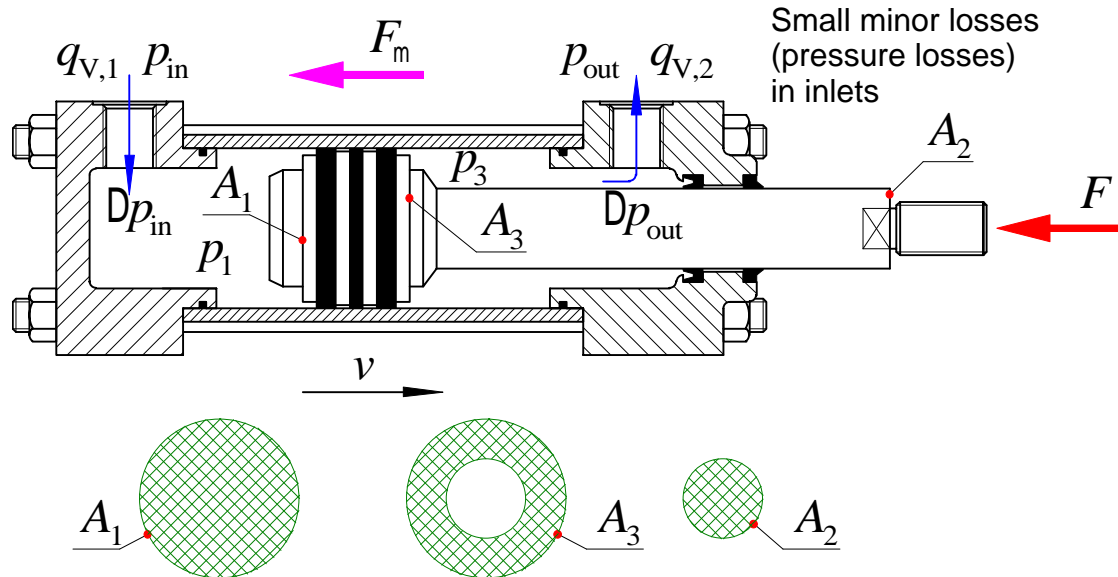
Load force  $F$  [N]

Effective piston area  $A$  [m<sup>2</sup>]



## Reality

Small minor losses  
(pressure losses)  
in inlets



Small minor losses  
(pressure losses)  
in inlets

Example case:  
plus-direction movement,  
opposing force

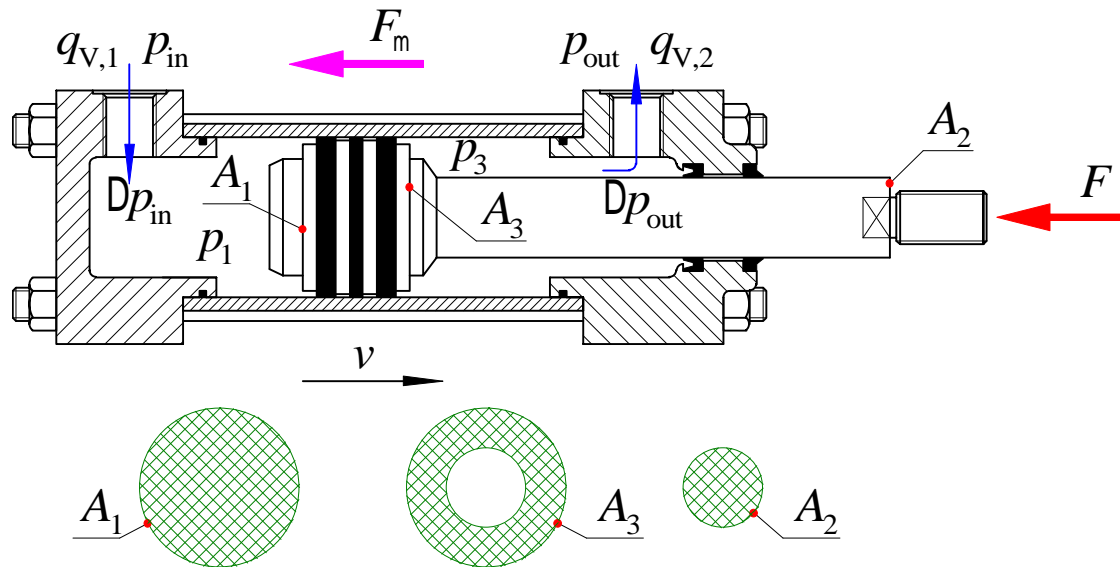
Friction – hydromechanical efficiency  $h_{hm}$

Leakage – volumetric efficiency  $h_v$

Efficiencies in cylinder case are quite unclear  
It would be better to use in calculations  
- Friction forces  
- Leakage flow rates  
instead

# Pressure

Example case:  
plus-direction movement,  
opposing force



Actual A chamber pressure  $\Rightarrow$  force      Actual B chamber pressure  $\Rightarrow$  force

Force equation 
$$p_{in} \times A_1 - Dp_{in} \times A_1 = p_{out} \times A_3 + Dp_{out} \times A_3 + F + F_{\mu}$$

Friction force (opposing movement)  
 Load force

Force equation in general form

Flow OUT increases the actual chamber pressure because of minor loss

$$p_{\text{real, in}} \times A_{\text{in}} - Dp_{\text{in}} \times A_{\text{in}} = F + F_{\mu} + p_{\text{out}} \times A_{\text{out}} + Dp_{\text{out}} \times A_{\text{out}}$$

Flow IN decreases the actual chamber pressure because of minor loss

Actual pressure demand

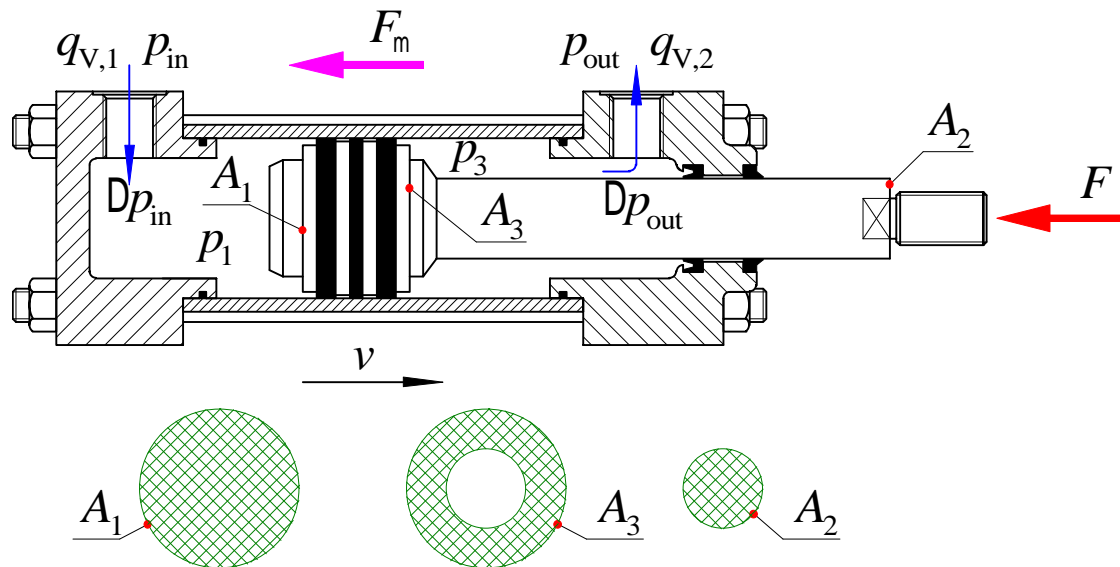
$$p_{\text{real, in}} = \frac{F + F_{\mu} + p_{\text{out}} \times A_{\text{out}} + Dp_{\text{out}} \times A_{\text{out}} + Dp_{\text{in}} \times A_{\text{in}}}{A_{\text{in}}}$$

In efficiency form

$$p_{\text{real, in}} = \frac{F}{A_{\text{in}} \times \eta_{\text{hm}}} + p_{\text{out}} \times \frac{A_{\text{out}}}{A_{\text{in}}}$$

Correct or not?  
Hydromechanical efficiency  
depends on what?

Flow

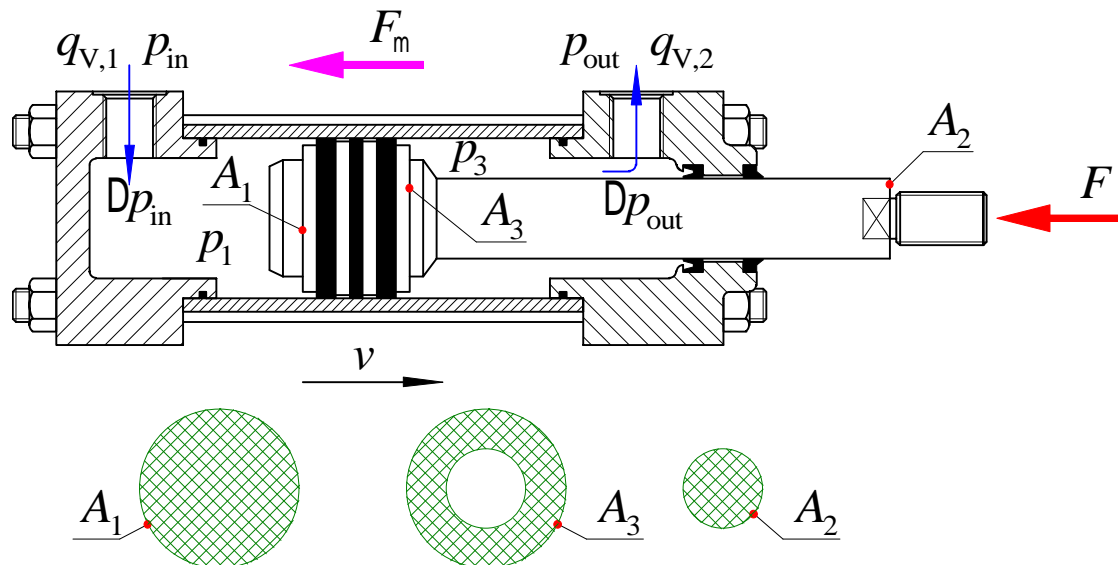


Example case:  
plus-direction movement,  
opposing force

Actual flow demand  $q_{V,in,real} = \frac{A_{in} > v}{h_v}$

Volumetric efficiency depends on the leakages  
What if pressure  $p_3$  is higher than  $p_1$ ?  
Unclear!

## Power



Example case:  
plus-direction movement,  
opposing force

Power demand of external force  $P_{\text{mech}} = F \cdot v$

## Theoretic power demand

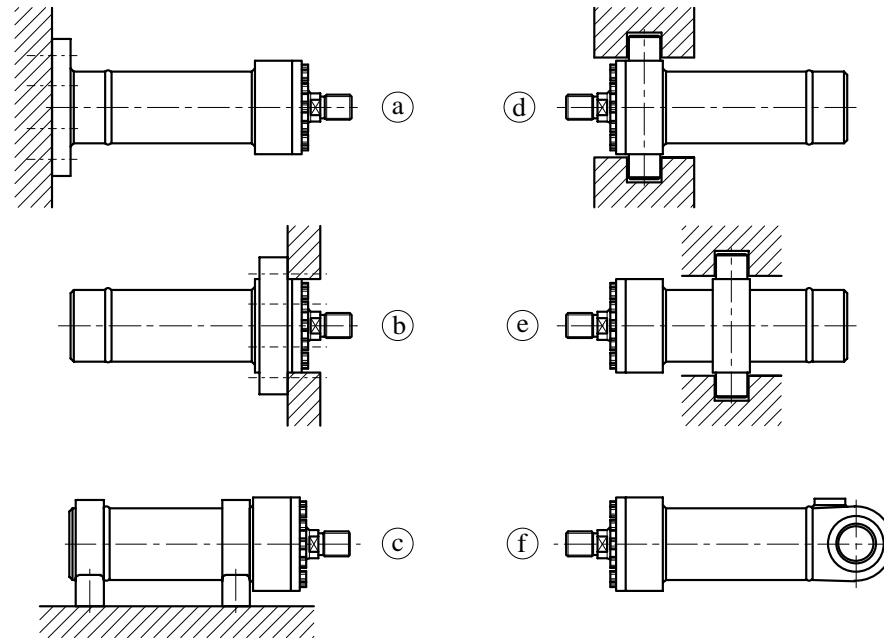
$$P_{\text{theor}} = q_{V,\text{in}} \times c_p \times p_{\text{in}} - \frac{A_{\text{out}}}{A_{\text{in}}} \times p_{\text{out}} \frac{\dot{V}}{\dot{V}} = F \times v$$

## Actual power demand

$$P_{\text{real}} = q_{V,\text{in}} \times c_p \times p_{\text{in}} - \frac{A_{\text{out}}}{A_{\text{in}}} \times p_{\text{out}} \frac{\dot{V}}{\dot{V}} = \frac{F \times v}{h_t}$$

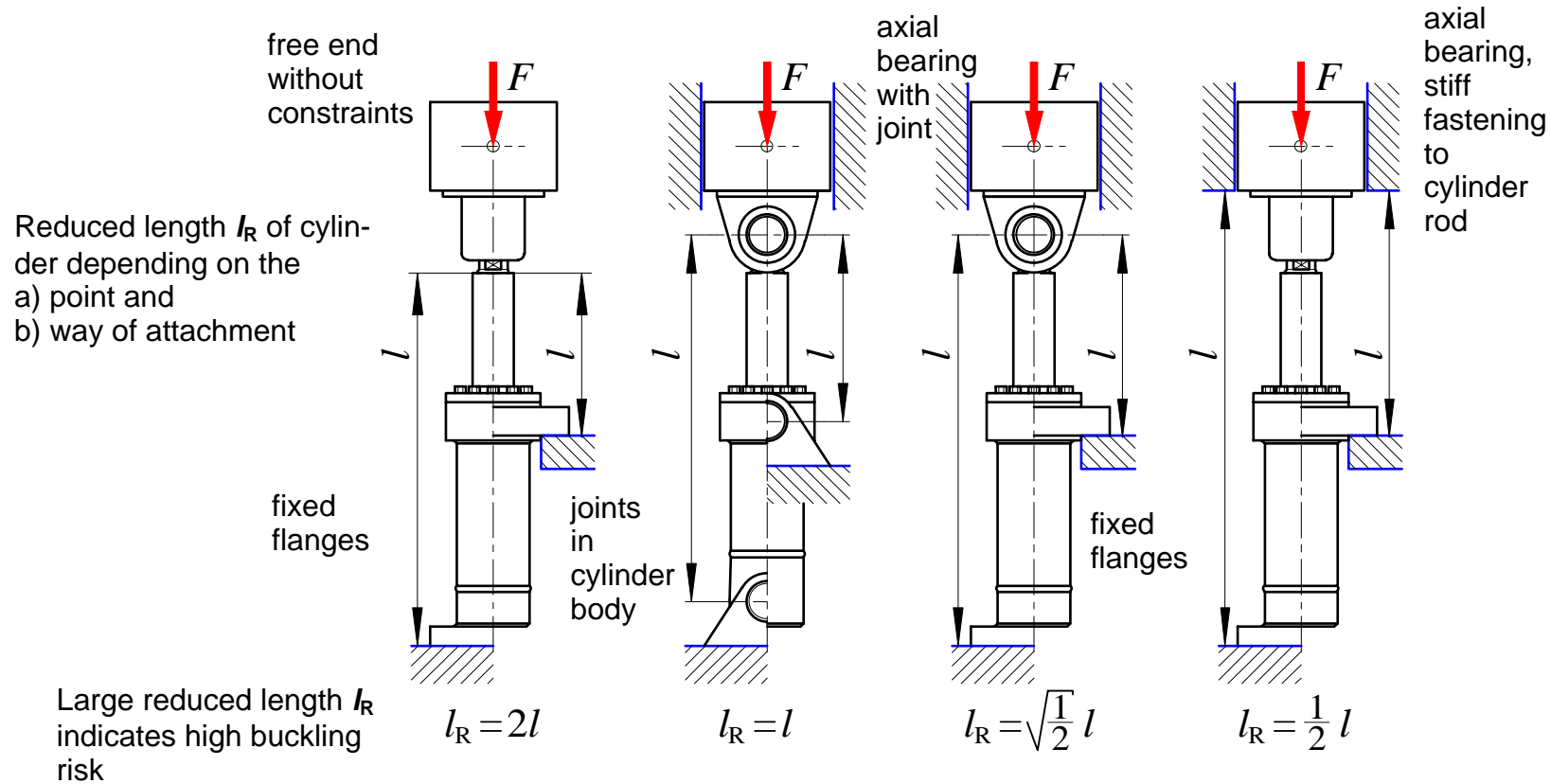
If there is meaningful leakage, both the volumetric efficiency and total efficiency depend heavily on the velocity.  
Normally leakage is very small and total efficiency depends merely on seal friction(s) and minor losses.

## Loading and buckling of cylinders



Loading only in parallel to the piston rod!

## Mounting and buckling length





## Buckling diagram

Safety factor typically 4

$$F = \frac{p^2 \times E_m \times I}{C_n \times l_R^2}$$

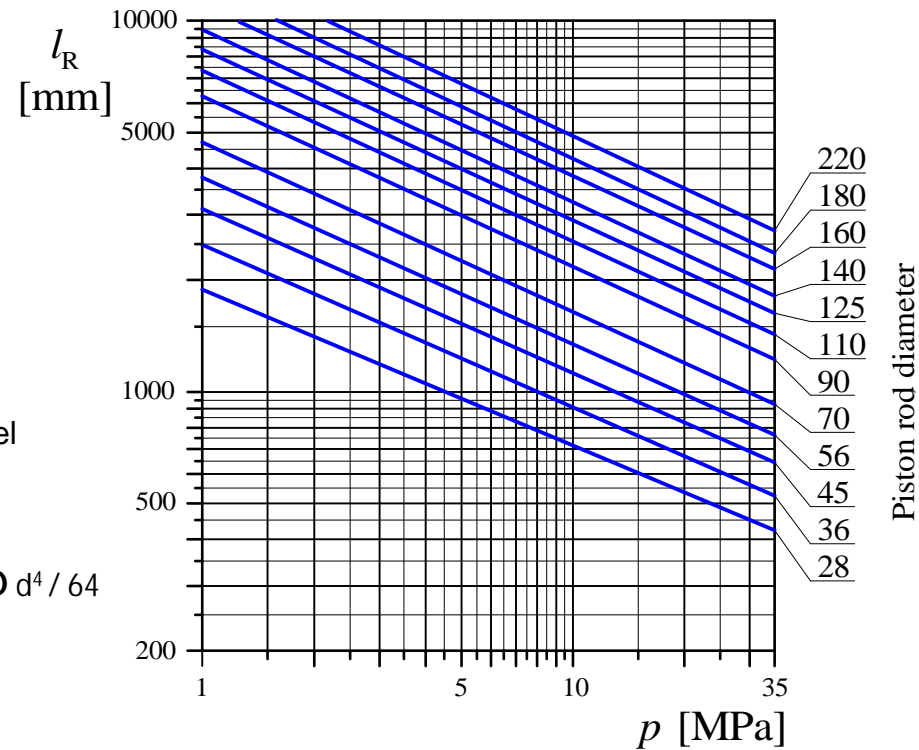
Young's modulus  $\sim 210$  GPa for steel

$E_m$  modulus of elasticity

$I$  area moment of inertia  $p d^4 / 64$

$C_n$  safety factor

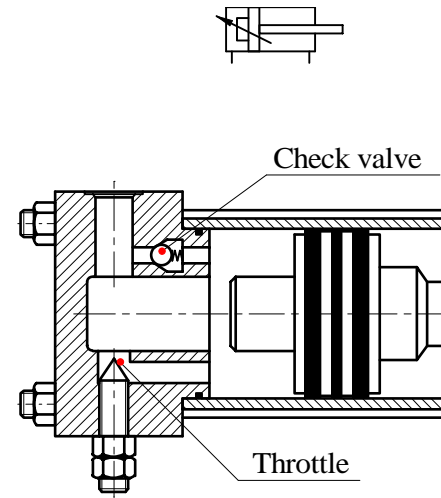
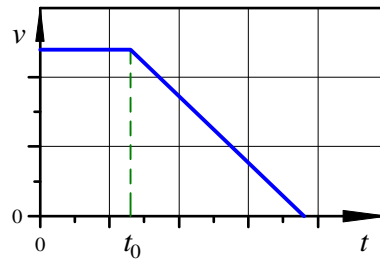
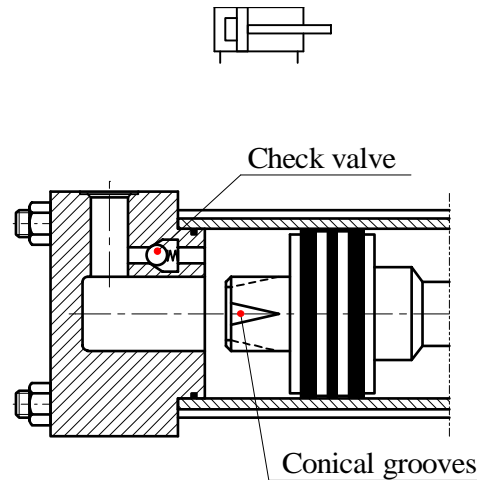
$l_R$  effective length



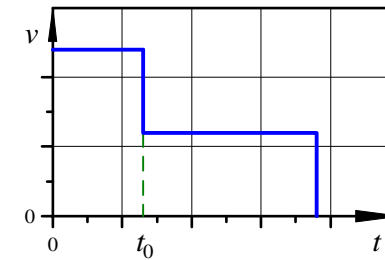
## End cushioning of cylinders

At velocities  
 $> 0.1 \text{ m/s}$

Flow area diminishes  
 flow resistance  
 increases the deeper  
 the rod end is in the  
 flow channel



Flow area and flow  
 resistance remain the  
 same as the rod end gets  
 into the flow channel  
 Flow resistance is ad-  
 justable



# Torque motors

Convert hydraulic power into mechanical power

Rotation angle restricted, generally  $< 360^\circ$

Construction types:

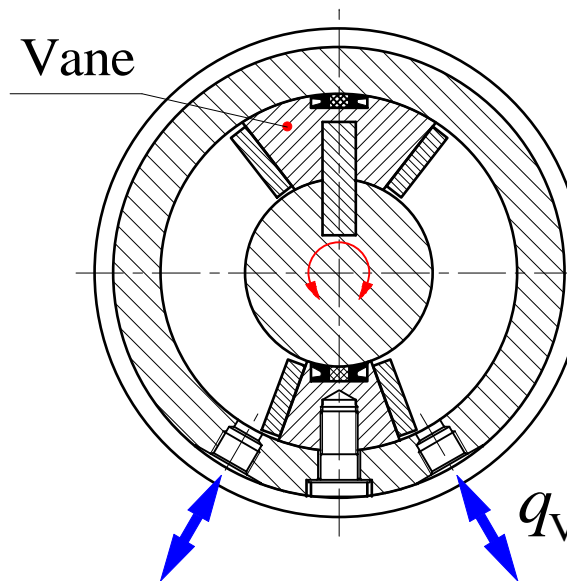
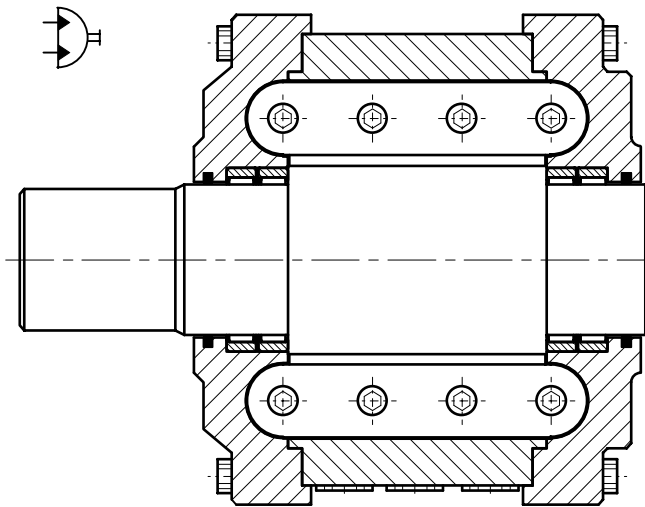
- vane
- piston

Both operate on positive displacement principle

Total efficiency max.  $h_t \gg 0.6 - 0.86$

Torque max.  $T \gg 10000 - 20000 (- 300000) \text{ Nm}$

# Vane type



Maximum rotation angle  $\sim 320^\circ$

With end cushioning  $\sim 240^\circ$

Uneven pressure distribution causes high bearing loads

With 2 vane structure higher torques and pressure forces can be compensated  $\Rightarrow$

smaller turning angle  $\sim 170^\circ$

Constant torque

Leakage reduces total efficiency

Maximum  $\sim 72\%$

## **Piston type**

Gear type:

Screw gear

Crank mechanism

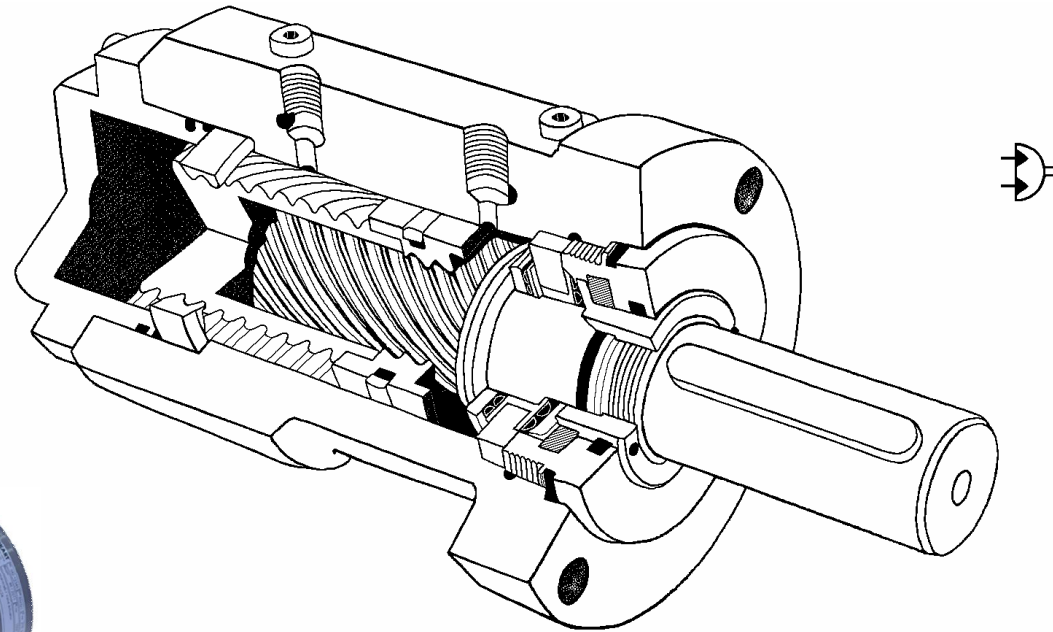
Cogwheel gear

Linear movement produced by piston is transformed into rotational by using two (2) screw gear mechanisms

- On the outer surface of piston
- On the inner surface of piston

The rotation angle can be up to 720°

Maximum pressure is about 100 bars  
Efficiency is limited by leakages and friction in the gear  
Constant torque  
Maximum efficiency is about 62%

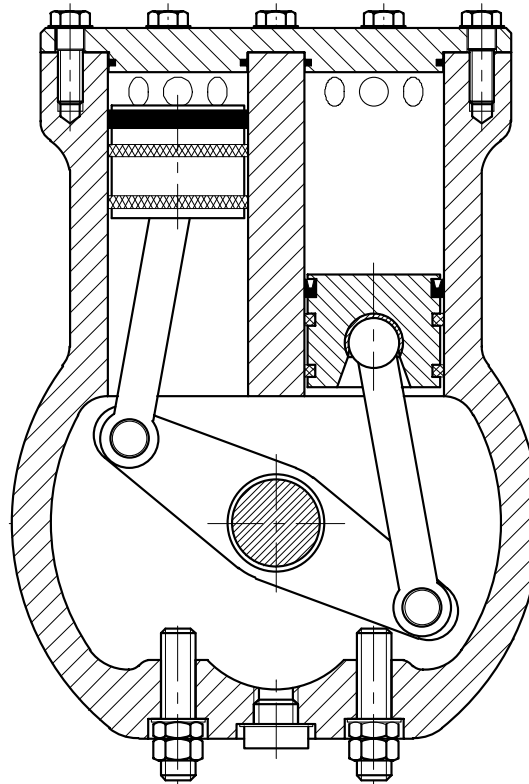


Screw gear  
Crank mechanism  
Cogwheel gear

Two pistons in parallel to have operation in two directions  
Torque is not constant  
- maximum in the middle  
- only about 2/3 of the maximum near the ends

Turning angle about 100°

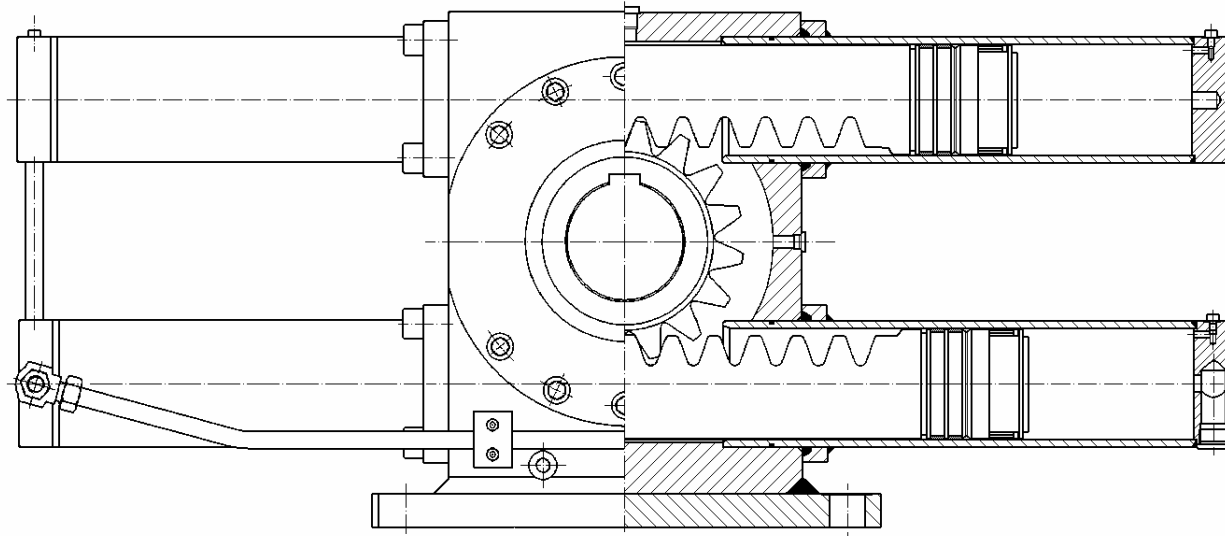
Maximum pressures 100 - 150 bar



Torque motors

Screw gear  
Crank mechanism  
Cogwheel gear

Linear movement is converted into rotational with cogwheel mechanism  
The rotation angles are typically  $90^\circ$  -  $720^\circ$   
Maximum pressure typically 160 bar  
Efficiency can be about 86%



Rack and pinion structure



Torque motors



<https://www.fiellberg.fi/products/torque-motor/>

Screw gear  
Crank mechanism  
Cogwheel gear



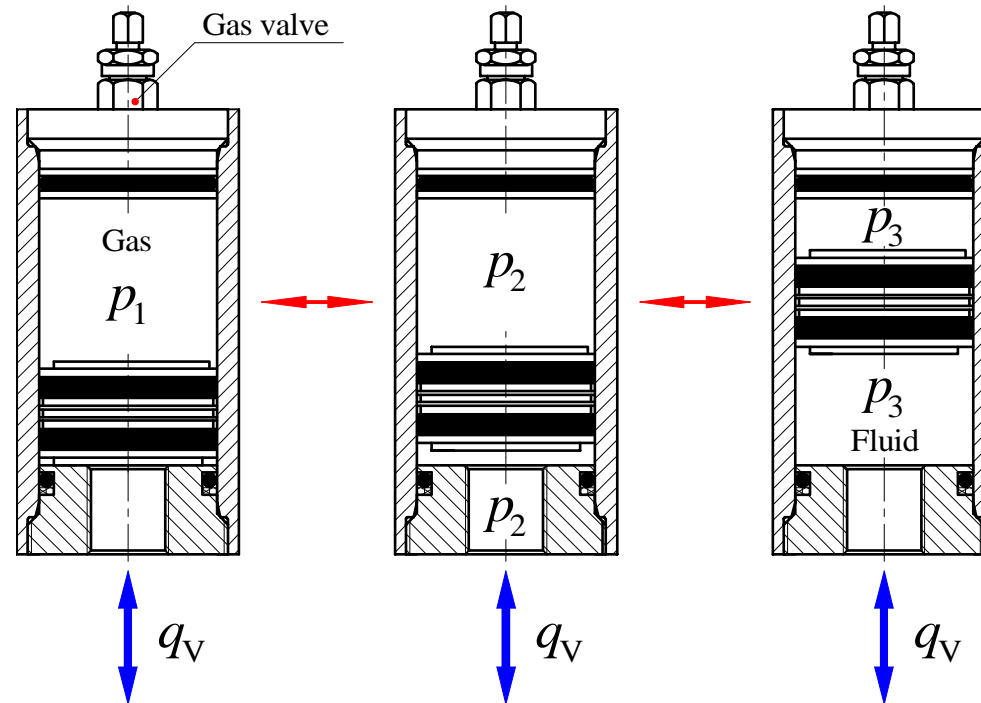
Accumulators are superior **power sources**

# Pressure accumulators

Store hydraulic energy  
by utilizing the  
compressibility of gas  
(nitrogen)      Piston accumulator

To activate the accumulator the system  
pressure has to exceed accumulator's  
precharge pressure ( $p_1$  in the figure))

Nitrogen gas  $N_2$



## Construction and characteristics

Construction types:

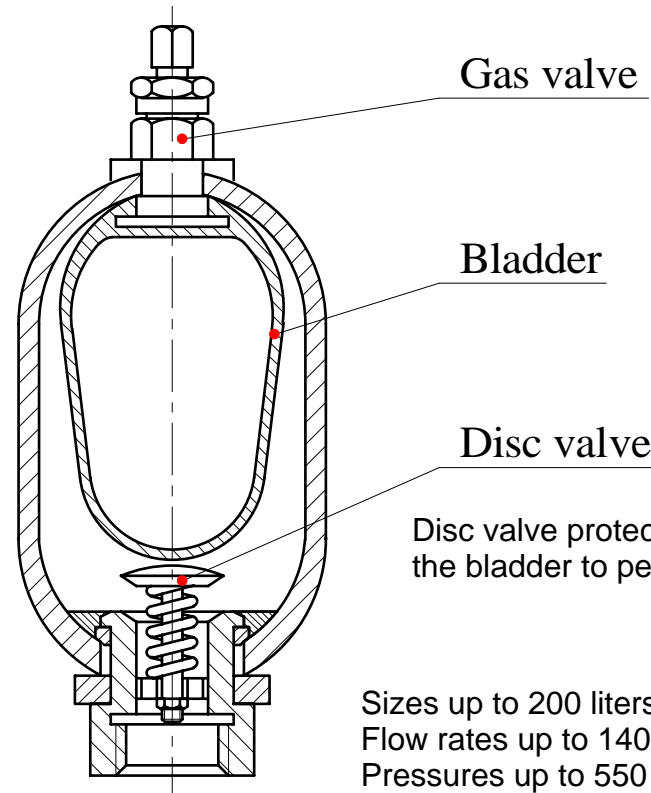
- bladder
- diaphragm
- piston

Nominal volumes  $V \gg 0.1 - 600 \times 10^{-3} \text{ m}^3$

Charging and de-charging flows max.  $q_V \gg 120 - 140 \times 10^{-3} \text{ m}^3/\text{s}$



Gas inside the bladder  
Fluid outside



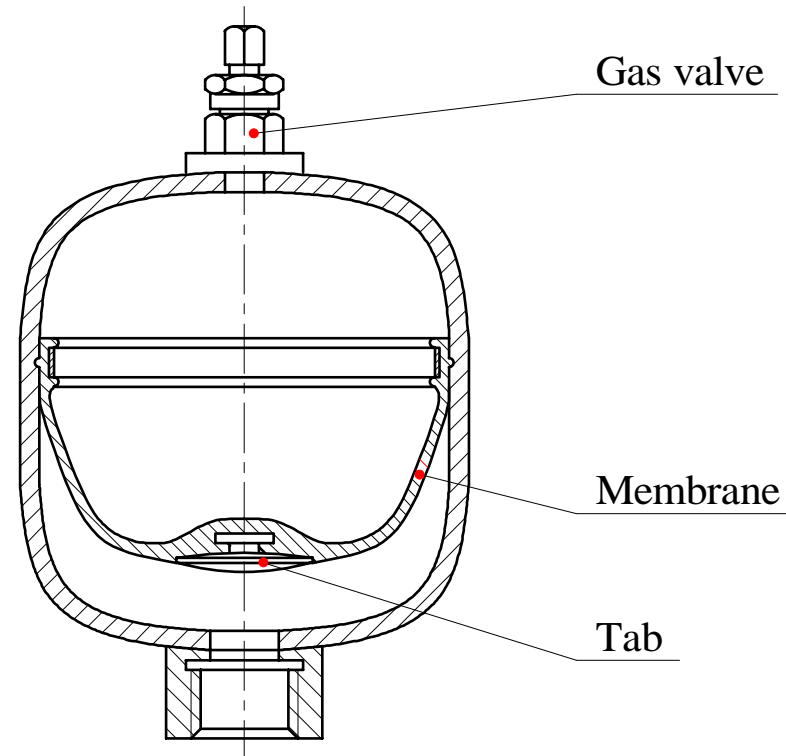
Disc valve protects the bladder and prevents the bladder to penetrate out

Sizes up to 200 liters  
Flow rates up to 140 l/s (!)  
Pressures up to 550 bar

Bladder  
Diaphragm  
Piston



Membrane accumulators are often used for damping of hydraulic oscillations  
Sizes up to 5 liters  
Flow rates up to 140 l/s (!)  
Pressures up to 500 bar

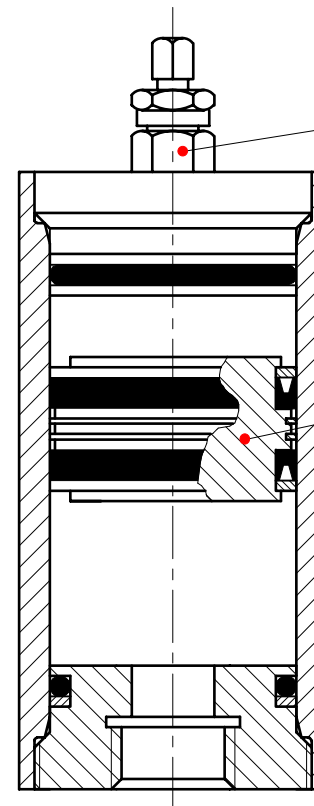


Bladder  
Diaphragm (aka Membrane)  
Piston



<https://www.hydrroll.com/fi/>

Bladder  
Diaphragm  
Piston



Gas valve

Piston

Sizes up to 600 liters  
Flow rates up to 120 l/s (!)  
Pressures up to 400 bar

Seal friction may decrease the efficiency (at low pressures)

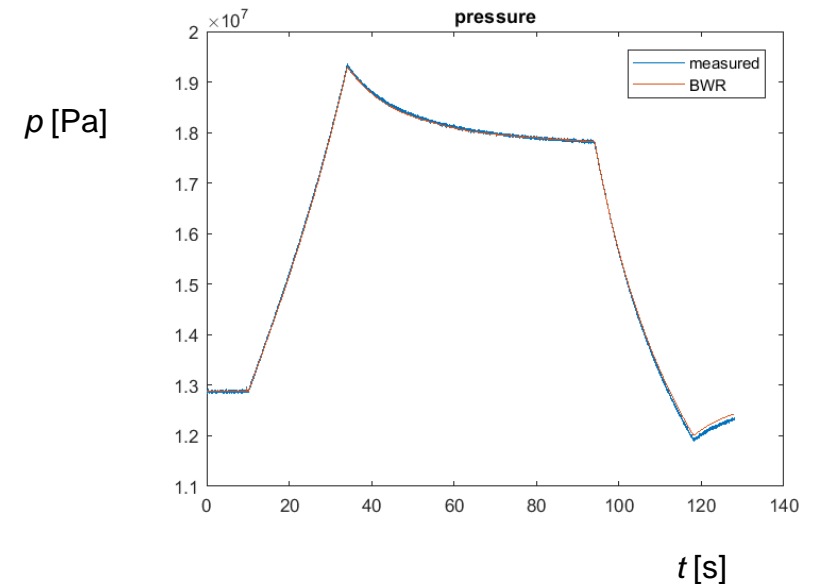
Gas volume can be increased by connecting additional gas bottles to accumulators

## Application examples

- Flow source
- Upkeep of pressure
- Levelling of flow fluctuation
- Suppression of pressure shocks
- Energy storage for exceptional situations
- Storing of external energy
- Levelling of volume changes
- Levelling of shock-like loadings of actuators

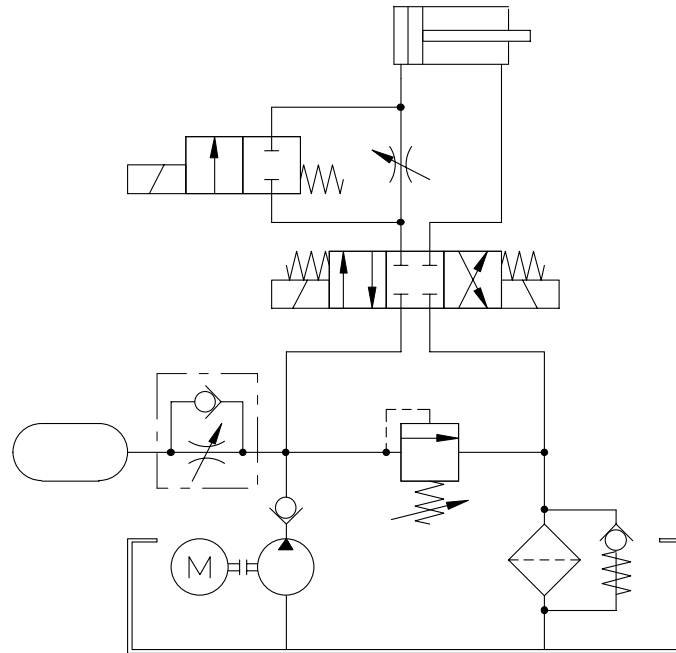
Equation of state for ideal gas can be used for simple calculations  
Real gas equations for accurate results (especially at high pressures)

compression - storage (1 minute) - expansion

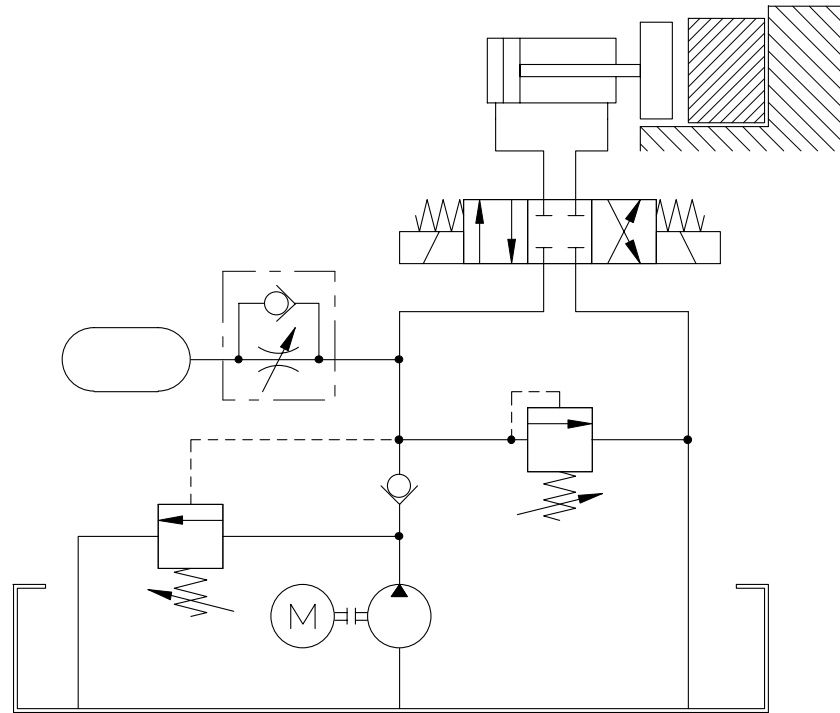


Measured and simulated pressure response indicates the effects of thermal losses especially during storage phase

# Flow source

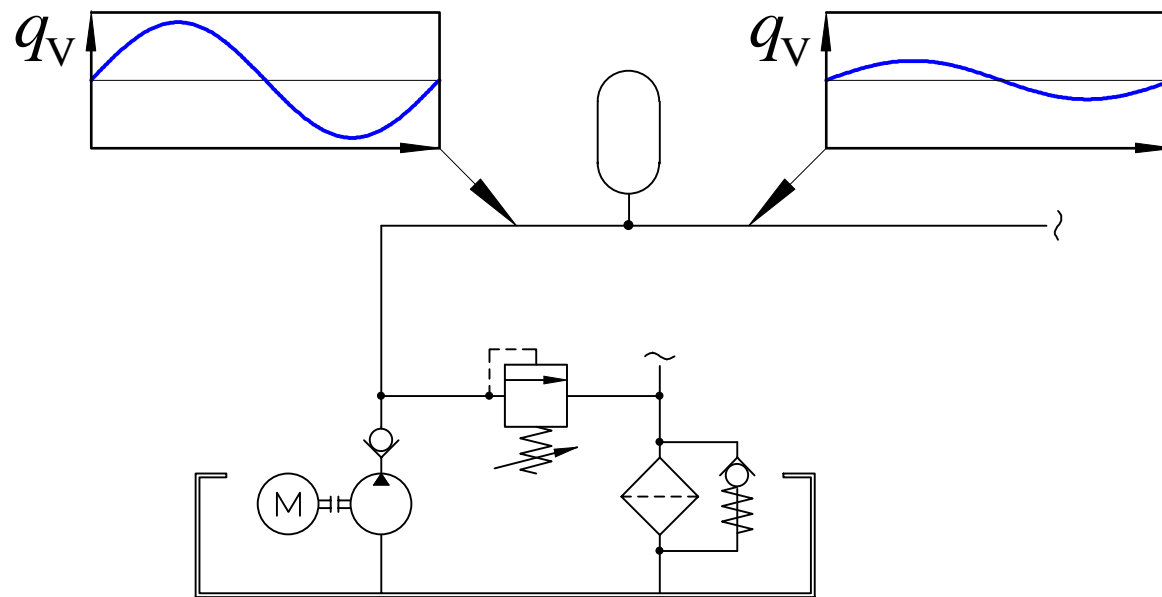


## Upkeep of pressure

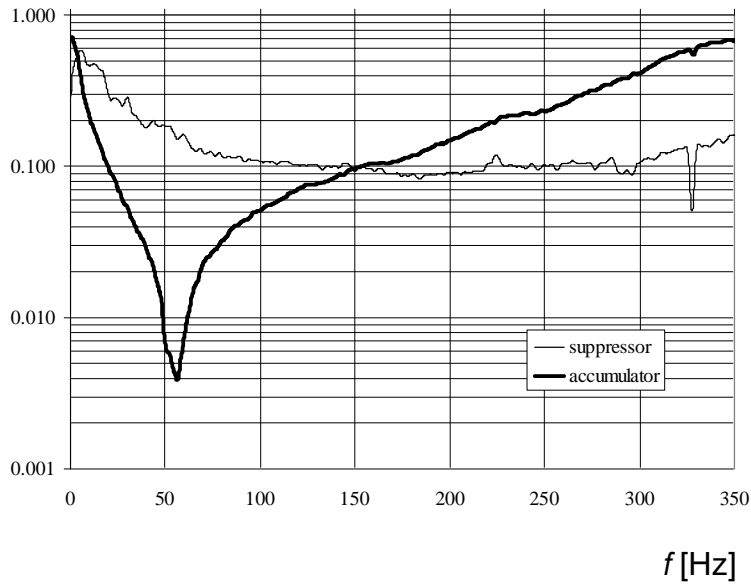




## Levelling of flow fluctuation

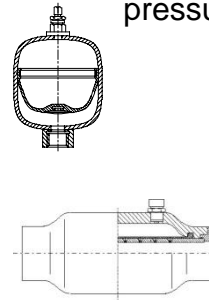


Pressure pulsation amplitude as function of frequency



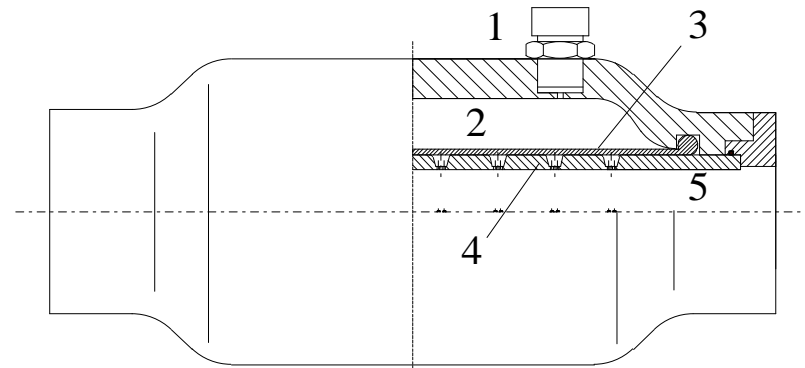
Inline suppressor ®

Membrane accumulator's  
 a) elastic gas volume (hydraulic capacitance) and  
 b) inlet throat  
 form together a hydraulic resonator capable of damping  
 pressure oscillations at frequencies 0 - 100 - 300 Hz



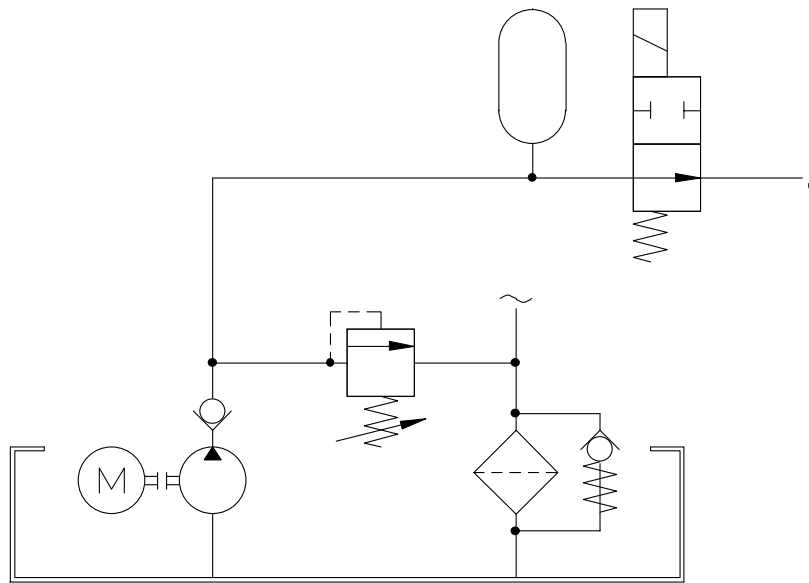
Example:  
 Levelling of  
 flow fluctuation

Special accumulators "pulsation and noise dampers" or "inline suppressors" have wider frequency range

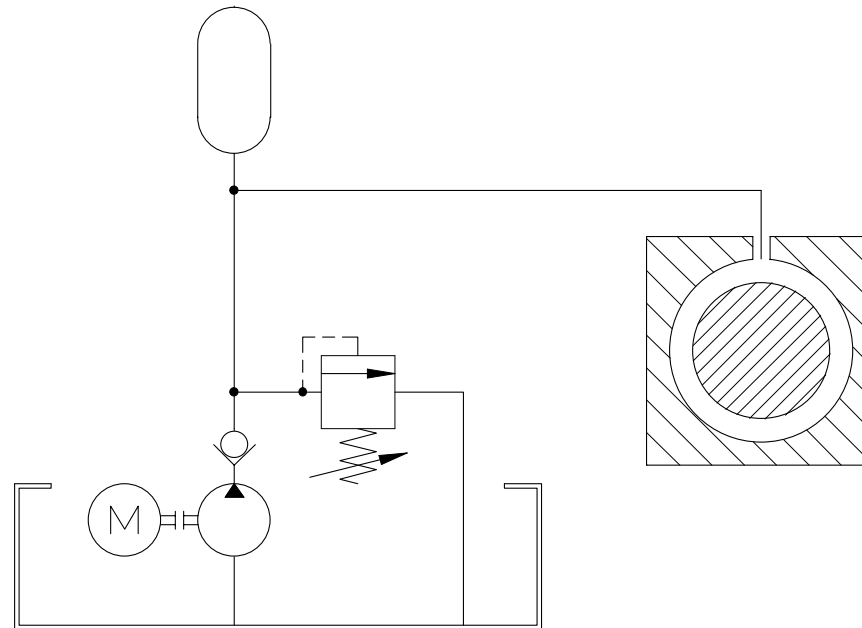


<http://www.saip.it/EN/Products/Standard%20accumulators/with%20bladder/SPM%20type>

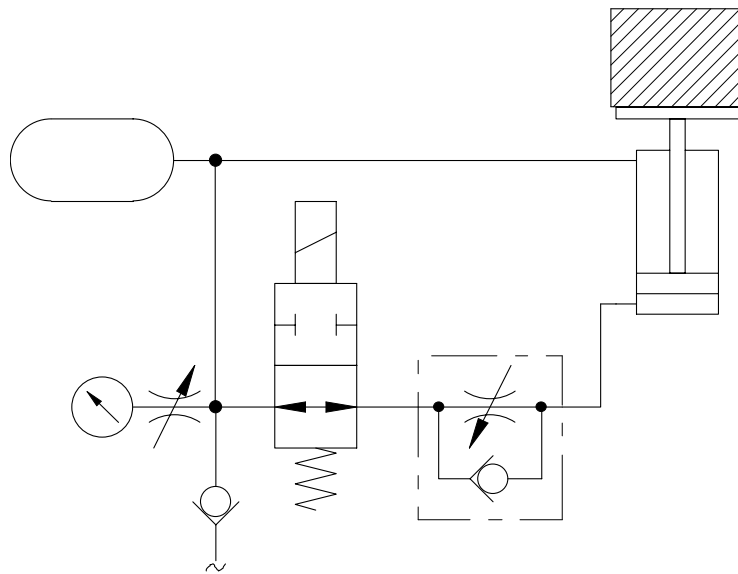
## Suppression of pressure shocks



## Energy storage for exceptional situations



## Storing of external energy



# Lecture themes - Recap

Pump's task in hydraulic system?

Converting hydraulic power into

- rotational movement?

- linear movement?

Operation principle of hydrostatic power converters?

Utilization possibilities of pressure accumulators?