



Aalto-yliopisto
Sähkötekniikan
korkeakoulu

Pressure measurements

ELEC-E5710 Sensors and Measurement
Methods

Pressure

- Compressed gas or liquid aims to expand, this is called pressure.
- Defined as a ratio of force and surface area

$$p = \frac{F}{A}$$

- SI unit for pressure is Pascal,
 - Pa = N/m² = kg/m/s²
- After temperature, pressure is the second most measured process quantity.

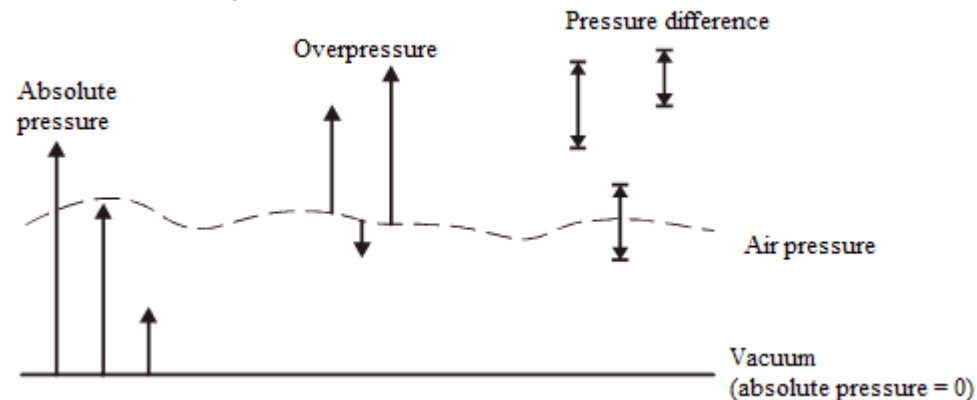


Units of pressure

	Pa	bar	psi	at	atm	Torr	mmHg	inHg	cmH ₂ O
1 Pa	1	10^{-5}	$1.45 \cdot 10^{-4}$	$1.02 \cdot 10^{-5}$	$9.87 \cdot 10^{-6}$	$7.5 \cdot 10^{-3}$	$7.5 \cdot 10^{-3}$	$2.96 \cdot 10^{-4}$	0.0102
1 bar	10^5	1	14.5	1.02	0.987	750	750	29.6	1020
1 psi	6890	689	1	0.070	0.068	51.7	51.7	2.04	70.3
1 at	$9.81 \cdot 10^4$	0.981	14.2	1	0.968	736	736	29	1000
1 atm	101325	1.01	14.7	1.03	1	760	760	30	1030
1 Torr	133	$1.33 \cdot 10^{-3}$	0.0193	$1.36 \cdot 10^{-3}$	$1.32 \cdot 10^{-3}$	1	~1	0.0395	1.36
1 mmHg	133	$1.33 \cdot 10^{-3}$	0.0193	$1.36 \cdot 10^{-3}$	$1.32 \cdot 10^{-3}$	~1	1	0.0395	1.36
1 inHg	3380	338	0.49	0.0344	0.033	25.3	25.3	1	34.4
1 cmH ₂ O	98.1	$9.81 \cdot 10^{-4}$	0.0142	0.001	$9.68 \cdot 10^{-4}$	0.736	0.736	0.029	1

Types of pressure

- Absolute pressure
 - Compared to vacuum, so pressure is always greater than zero
 - Meters for small absolute pressure are called vacuum gauges
- Current air pressure
 - Depends on circumstances, altitude etc.
 - Gauges are called barometers, absolute measurement
- Overpressure and underpressure
 - Reference pressure is the current air pressure
- Pressure difference measurement
 - Reference value is something else than vacuum or current air pressure



Static and dynamic pressure

- Static pressure: static pressure is measured when the fluid is at rest

$$p$$

- Dynamic pressure: caused by directional kinetic energy of matter

$$\frac{1}{2}\rho v^2$$

- Total pressure = static pressure + dynamic pressure

Hydrostatic pressure

- Pressure caused by the gravitational force of the liquid or gas:

$$p = \rho g \Delta h$$

ρ = fluid density ; g = gravitational acceleration; h = depth of fluid

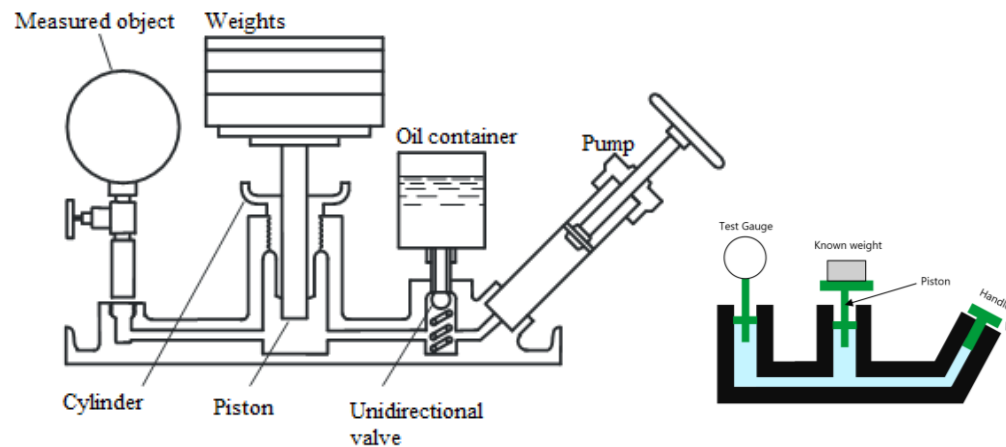
Measuring instruments

- Calibrating instruments are based on the definition of pressure
 - Dead weight testers
 - Manometers
- Field measuring instruments
 - Transitional and force sensors
 - For special applications e.g. thermic and ionization measuring instruments



Dead weight tester

- Typical calibrating device for meters
- Transforms the mass of weights to liquid or gas pressure with the help of a cylinder and a piston
- High accuracy is obtained by dimensional measurements (the diameter of the piston)

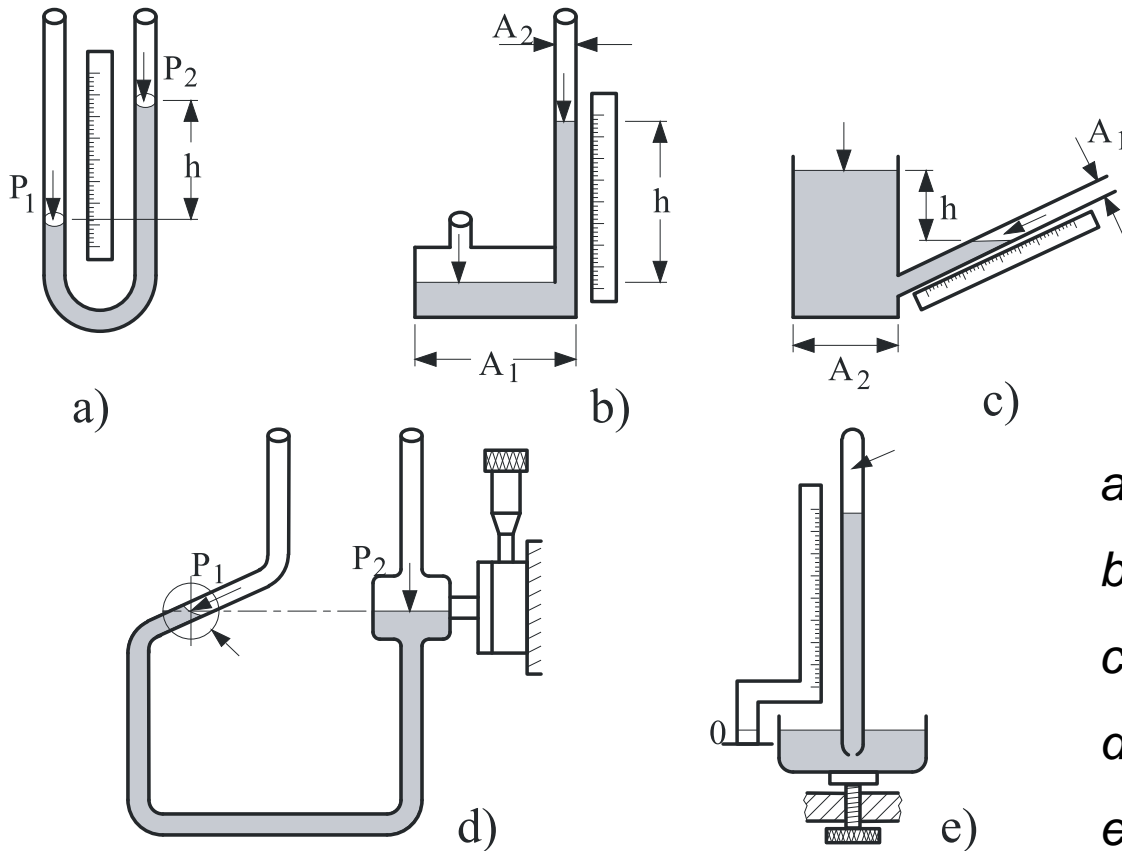


Schematic diagram: Dead Weight Tester

Dead weight tester

- Air or nitrogen as a medium when the pressure is low (1kPa – 5 MPa) and oil or water with higher pressure (5 MPa – 2,5 GPa)
- Problems
 - Small pressure: friction
 - High pressure: elastic deformation of the cylinder-piston combination
- Important during calibration
 - Determination of the effective area of the cylinder piston
 - Determination of the mass of the weights

Manometer



- a) *U-tube manometer,*
- b) *Well type manometer,*
- c) *Inclined tube manometer,*
- d) *Micro manometer*
- e) *Barometer*

Manometer

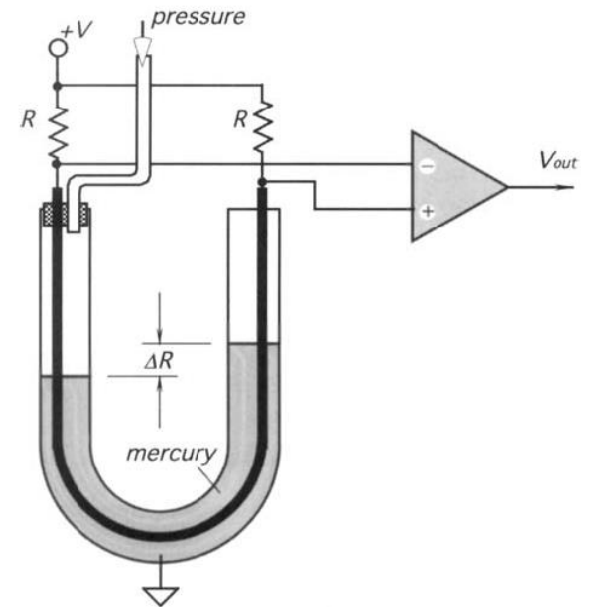
- Filled with water, mercury or e.g. butyl alcohol
- Pressure difference $p_1 - p_2$ can be calculated from the altitude difference of the columns

$$p_1 - p_2 = \rho gh, A_2 = A_1$$

$$p_1 - p_2 = \rho gh \left(1 + \frac{A_2}{A_1} \right), A_2 \neq A_1$$

Manometer (example)

- U-shaped resistive wire in mercury which short circuit the wire
- Measuring with a bridge connection
 - Equilibrium when the pressure difference of the tube is zero
 - When the other side is exposed to pressure, the bridge connection is not in equilibrium and there is an output signal
- When the pressure increases on the left side, the resistance also increases. On the other side, the resistance decreases
- The output voltage is proportional to the resistance difference



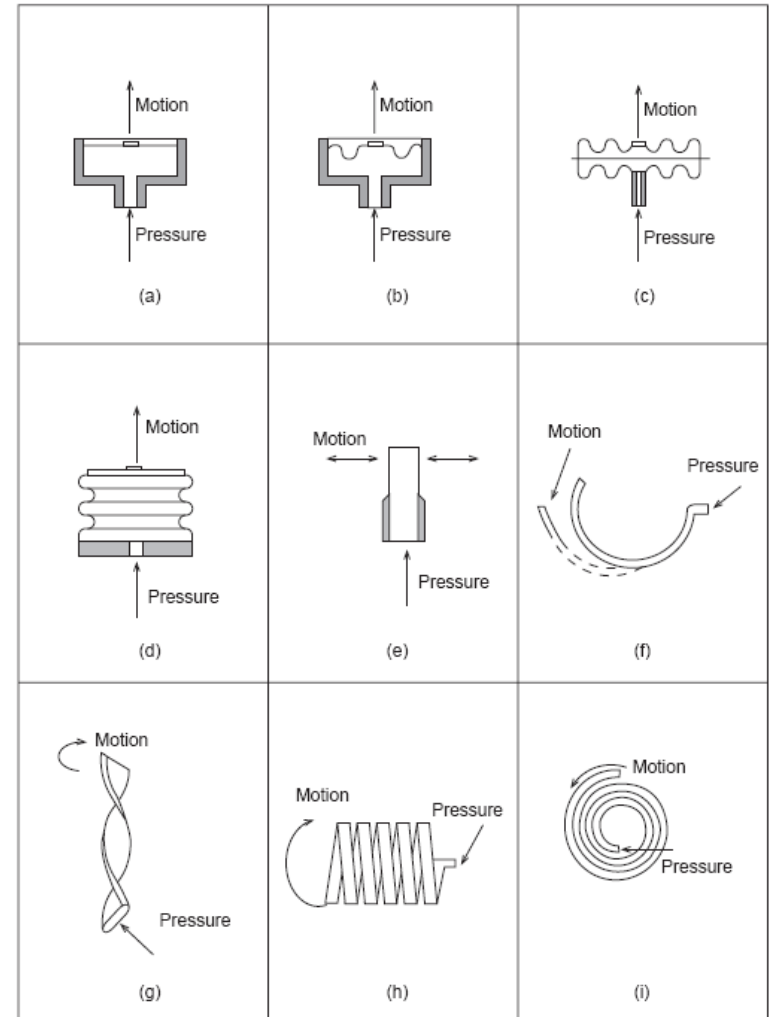
Manometer (example)

- Pros:
 - Simple and reliable instrument to measure gas pressure
 - Inexpensive
- Cons:
 - Low time constant
 - Sensitivity to vibrations
 - Large
 - Mercury contaminates the gas

Mechanical pressure sensors (no fluid)

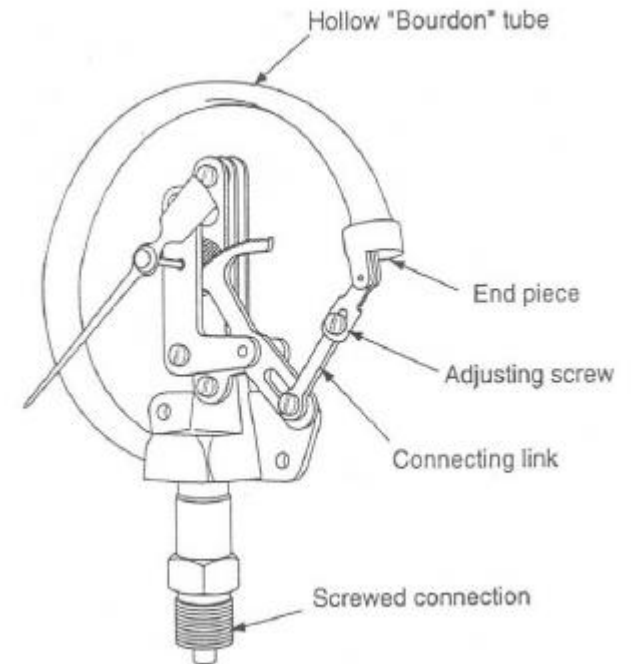
- transition pressure sensors

- (a) Flat film
- (b) Waved film
- (c) Capsule
- (d) Bellows
- (e) Straight tube
- (f) C-shaped bourdon tube
- (g) Bent bourdon tube
- (h) Twisted bourdon tube
- (i) Spiral bourdon tube



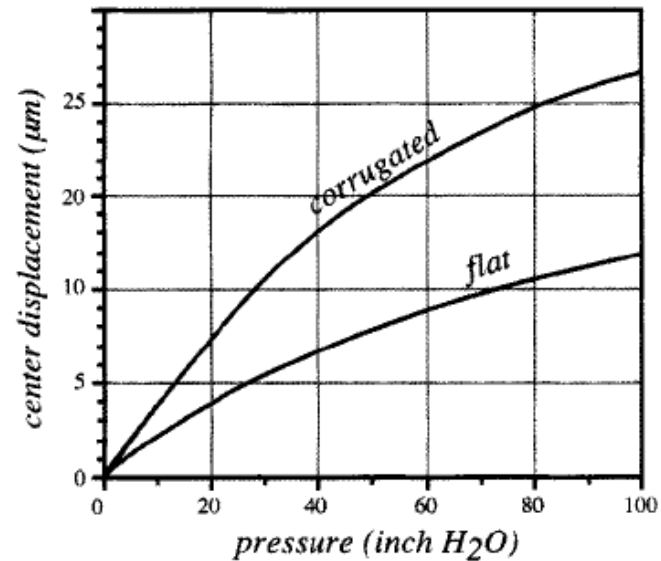
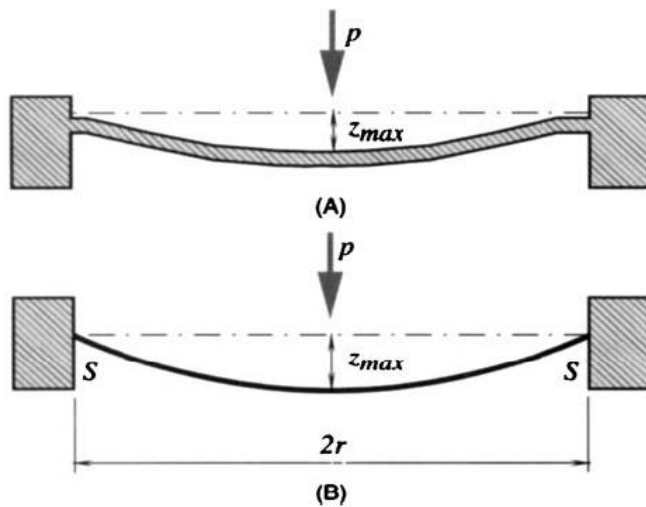
Bourdon tube

- Flat tube made of brass or steel
- Functioning based on springback factor
- Inexpensive, reasonable overall accuracy in pressure gauges
- Absolute pressure up to 6 MPa and overpressure up to 700 MPa



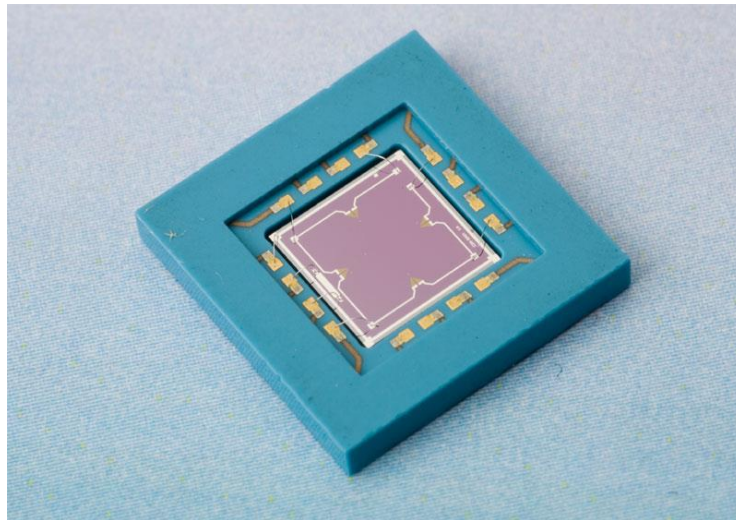
Flexible film

- Sensitivity can be enhanced by corrugating the film
 - Releases tension in the film
 - Enhanced sensitivity and linearity



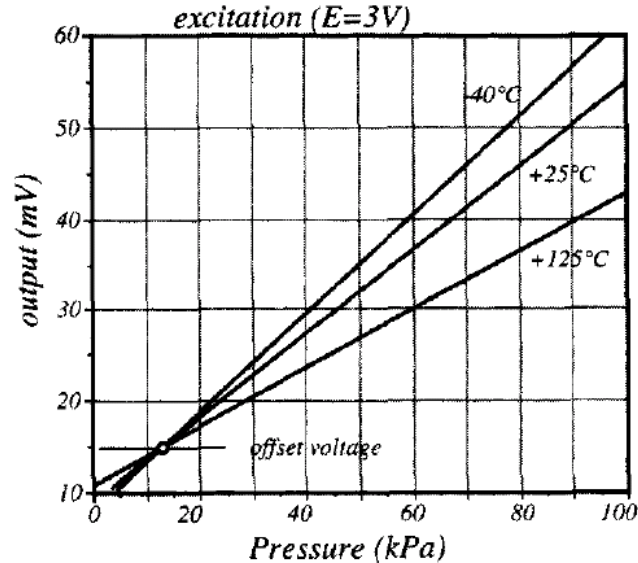
Piezoresistive pressure sensor

- The most common type,
 - To all applications
- Typically a semiconductor stretch slip attached to a flexible film
- Measurement with a Wheatstone bridge



Temperature dependency of a piezo pressure sensor

- The temperature coefficient of a piezo sensor's sensitivity is negative and rather big
- Temperature compensation is required
 - Often with bridge connections



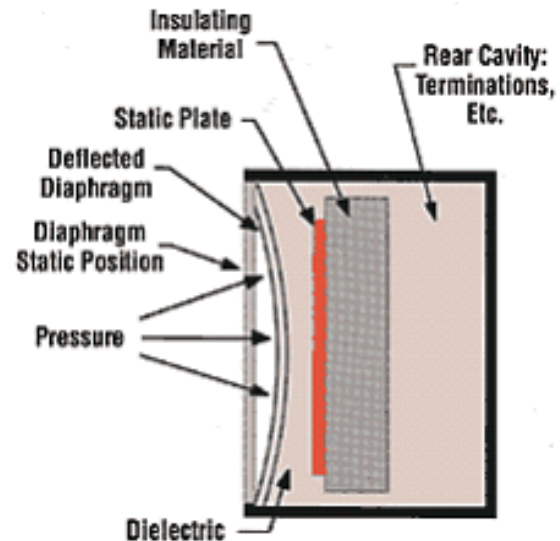
Strain gauge pressure sensor

- Electrical resistance of a strain gauge changes when material deforms.
- When a material comes longer and narrower, its resistance changes.



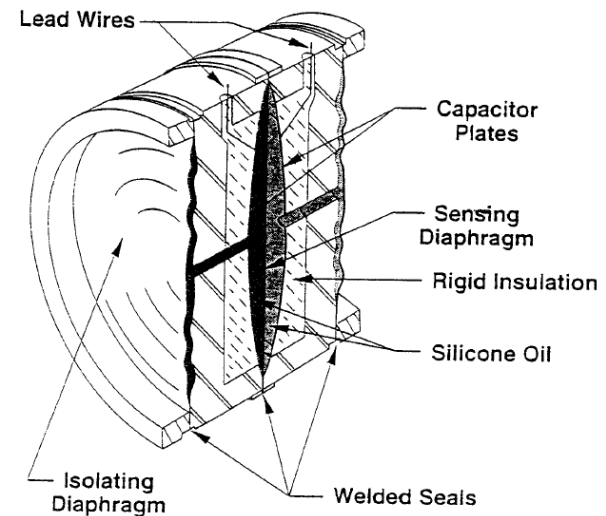
Capacitive pressure sensor

- Other electrode (e.g. silicon) functions a pressure-displacement transformer while the other one is fixed
- As pressure increases the distance between the electrodes decreases
 - Capacitance increases
- In differential version, the capacitance of the other one increases and the other one's decreases
- Linearity and stability are good but the measuring electronics is more complicated



Capacitive pressure sensor in practice

- 2 insulator films made of special metal compound
 - Also to measure corrosive materials
- Pressure difference to sensor film via oil
 - Desired permittivity to capacitor
 - Absorbs shocks and vibrations

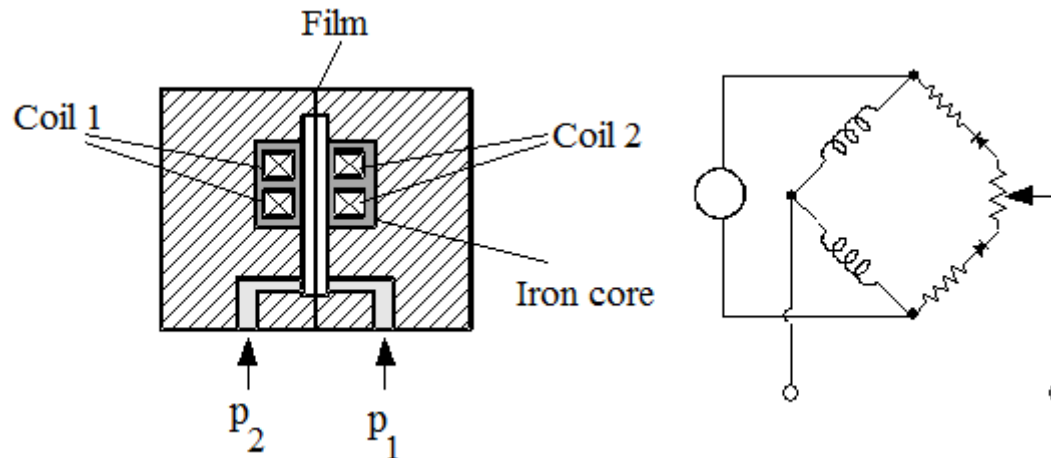


Piezo sensor vs. capacitive sensor

- Films can be protected against overpressure with a mechanical support
 - Movement of a capacitive film is bigger than in piezo sensors (better support is possible)
 - In film based sensors, meter breaks down at pressures 10 times (piezo) and 1000 times (capacitive) higher than the upper limit of the measurement range
- Flatness of the film is important for capacitive sensors
 - Displacements are often smaller than thicknesses
- Capacitive sensors have better relative sensitivity
- Stray capacitance can easily be as big as nominal capacitances (Measuring circuits must be close to sensors!)
- Both have low hysteresis

Inductive (reluctance) pressure sensor

- Change in pressure bends magnetic film
 - Air gap between the iron core and the film changes and, thus, the reluctance also changes
 - Inductance of the coil changes
- Measurements with small displacements (< 30 mm)
 - Small pressures



Reluctance sensor

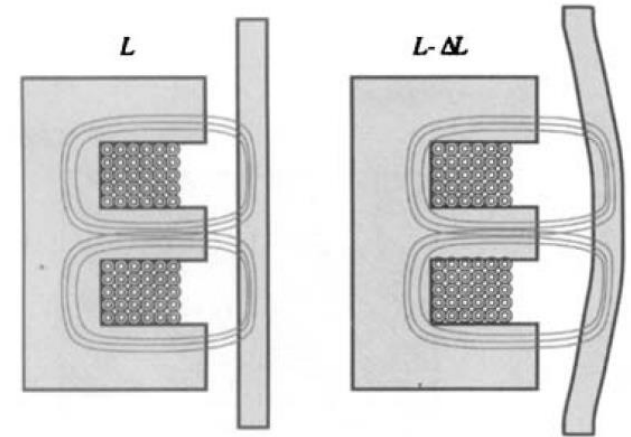
Material i causes a reluctance $R_i = \frac{l_i}{\mu_i A_i}$

l_i = distance experienced by flux in material

μ_i = permeability of the material

A_i = area in material which is perpendicular to direction of propagation

Inductance of a coil, which contains N turns $L = \frac{N^2}{\sum_{i=0}^M R_i}$

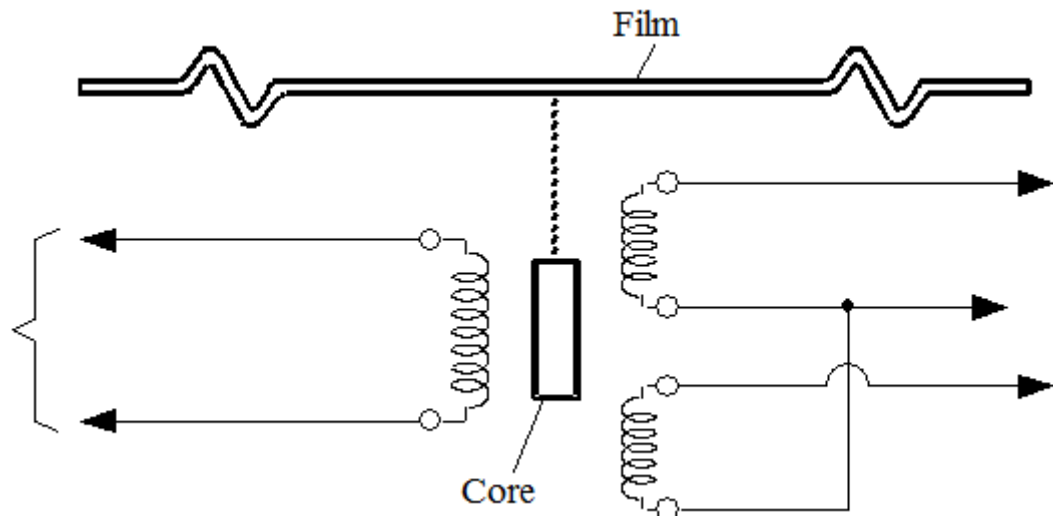


Pros of reluctance sensor

- Low temperature dependency
- Very small pressure difference measurements
- Due to small pressure cavity, there is good endurance to overpressure ('short circuit' of the magnetic parts does not disturb)
 - In practice, it almost never breaks down

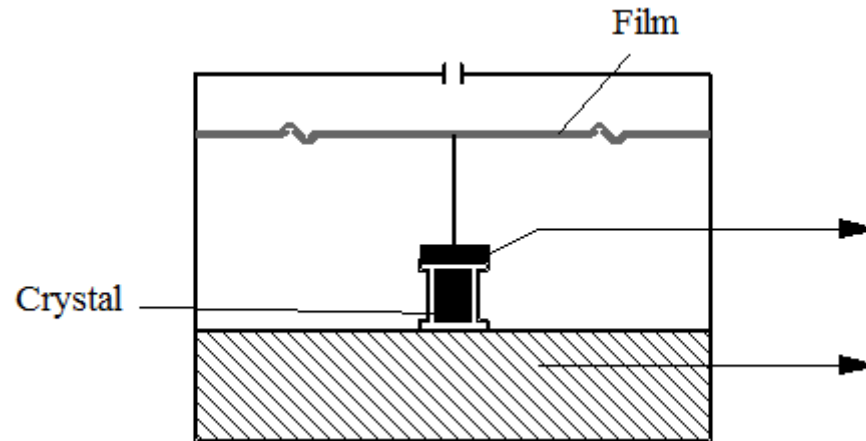
Inductive pressure sensor, Linear Variable Differential Transformer (LVDT)

- Moving iron core changes the transformer ratio



Piezoelectric pressure sensor

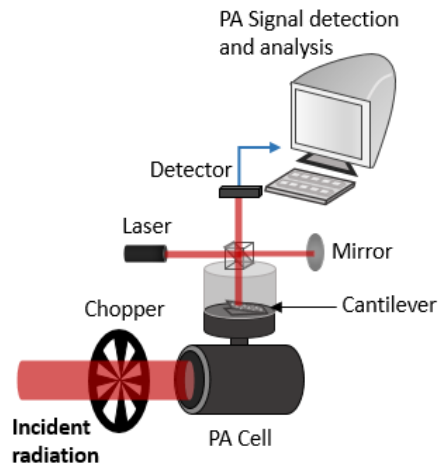
- Electric charge of the crystal surfaces change when the surface is strained
- Leakage currents compensate the charges on the crystal surfaces
 - Not suitable to measure static pressure



Piezoelectric pressure sensor

- Pros
 - High output signal and specific frequency
 - Small size, durable
- Cons
 - High output impedance and temperature sensitivity
 - Requires an amplifier
 - Only dynamic measurement

Cantilever Pressure sensor



Schematic diagram of Photoacoustic radiation detection setup with cantilever pressure sensor.

Absorption of chopped radiation by radiation absorber



Periodic volume expansion of carrier gas due to heating



Gaseous pressure induced cantilever movement



Interferometric detection of cantilever displacement