

# Previous Topics

## Basic Amplifiers

- Biasing schemes

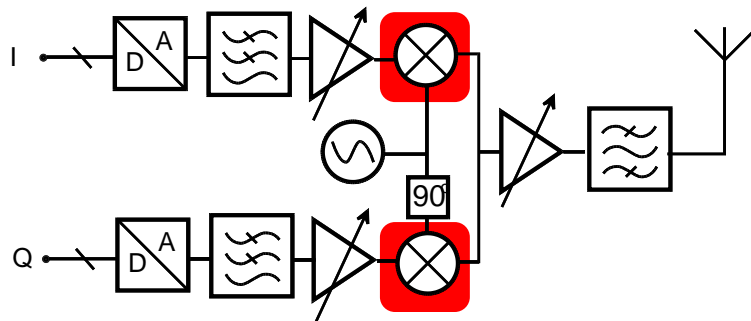
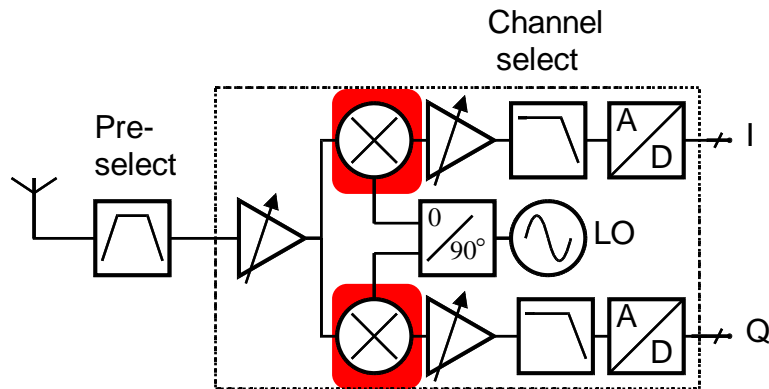
## Low-Noise Amplifiers

- Concepts
- Resistively terminated
- Parallel feed-back
- Common gate
- Inductively degenerated
- Wide bandwidth - - low noise ?? → Noise cancelling

## Power Amplifiers

- Concepts
- Current mode: A, B, C
- Switch mode: D, E, F

# Mixers



Focus on specific RF IC mixers

- Down-conversion (RX)
- Up-conversion (TX)

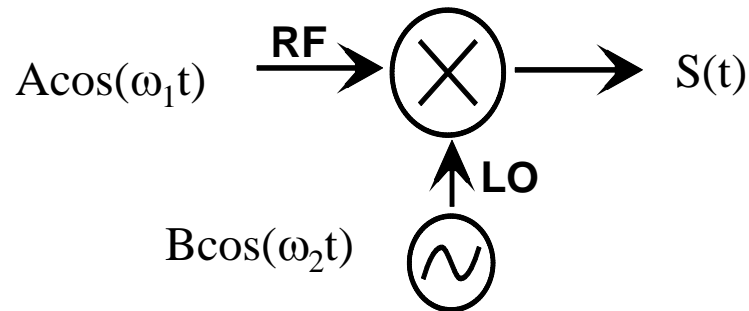
TX and RX mixers are quite similar  
→ RX only for simplicity

- Active mixers (Gilbert cell)
- Passive mixers
- Advanced cases / examples

Exercises & Homework

- Self-access learning material
- CAD-exercise
- Homeworks

# Ideal Multiplier / Mixer

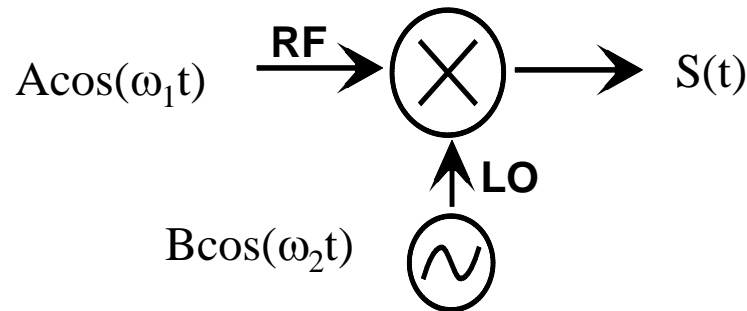


$$S(t) = A \cos(\omega_1 t) B \cos(\omega_2 t) = \frac{AB}{2} (\cos(\omega_1 - \omega_2)t + \cos(\omega_1 + \omega_2)t)$$

up-conversion

down-conversion

# Ideal Multiplier / Mixer



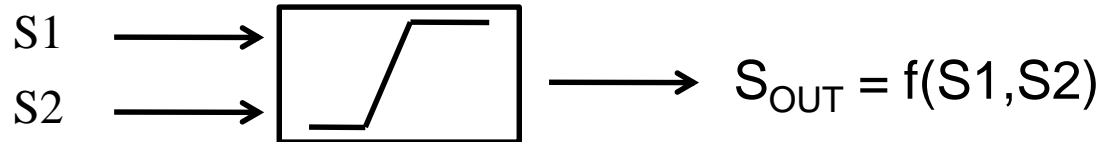
$$S(t) = A \cos(\omega_1 t) B \cos(\omega_2 t) = \frac{AB}{2} (\cos(\omega_1 - \omega_2)t + \cos(\omega_1 + \omega_2)t)$$

up-conversion

down-conversion

”mixing” = multiplication in time-domain = frequency shift in frequency domain

Any nonlinear element can act as a mixer



## Reminder: IIP3 Analysis

- Nonlinear circuit with 2<sup>nd</sup> and 3<sup>rd</sup> order nonlinearity

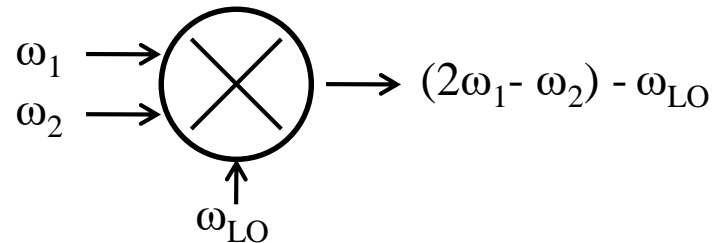
$$y(t) = \alpha_1 x(t) + \alpha_2 x^2(t) + \alpha_3 x^3(t)$$

- Inputs:  $A_1 \cos(\omega_1 t) + A_2 \cos(\omega_2 t) \rightarrow$  Output

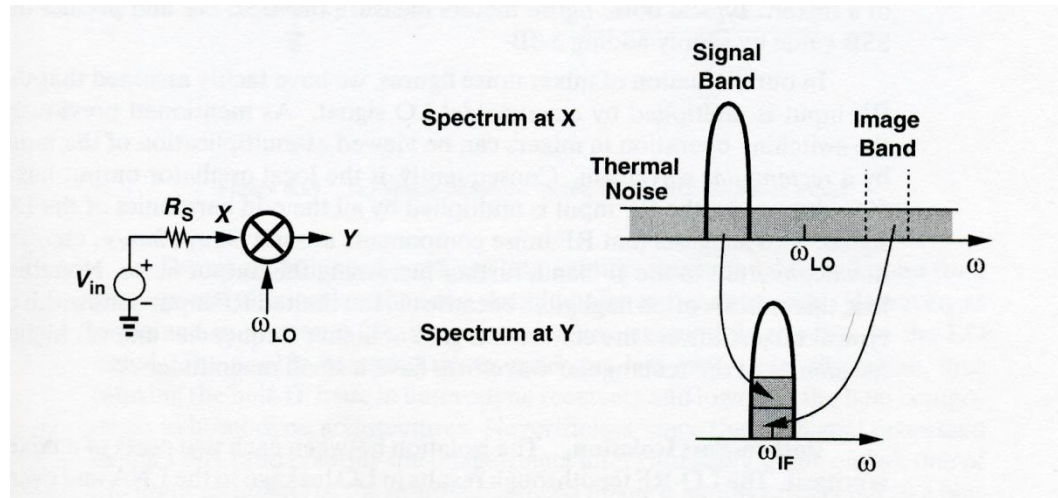
$$\begin{aligned} v_{out}(t) = & \frac{1}{2} \alpha_2 (A_1^2 + A_2^2) + \left( \alpha_1 A_1 + \alpha_3 \frac{3A_1^3 + 6A_1 A_2^2}{4} \right) \cos(\omega_1 t) + \left( \alpha_1 A_2 + \alpha_3 \frac{3A_2^3 + 6A_1^2 A_2}{4} \right) \cos(\omega_2 t) \\ & + \frac{1}{2} \alpha_2 A_1^2 \cos(2\omega_1 t) + \frac{1}{2} \alpha_2 A_2^2 \cos(2\omega_2 t) + \frac{1}{4} \alpha_3 A_1^3 \cos(3\omega_1 t) + \frac{1}{4} \alpha_3 A_2^3 \cos(3\omega_2 t) \\ & + \alpha_2 A_1 A_2 [\cos(\omega_1 t - \omega_2 t) + \cos(\omega_1 t + \omega_2 t)] + \frac{3}{4} \alpha_3 A_1^2 A_2 \cos(2\omega_1 t + \omega_2 t) + \frac{3}{4} \alpha_3 A_1 A_2^2 \cos(\omega_1 t + 2\omega_2 t) \\ & + \frac{3}{4} \alpha_3 A_1^2 A_2 \cos(2\omega_1 t - \omega_2 t) + \frac{3}{4} \alpha_3 A_1 A_2^2 \cos(2\omega_2 t - \omega_1 t) \end{aligned}$$

# Concepts

- Conversion gain =  $V_{IF} / V_{RF}$
- Noise Figure
  - Single-sideband (SSB)
  - Double-sideband (DSB)
- Linearity
  - IIP2
  - IIP3; in-band / out-of-band
- Compression point (ICP)
- Port-to-port isolation



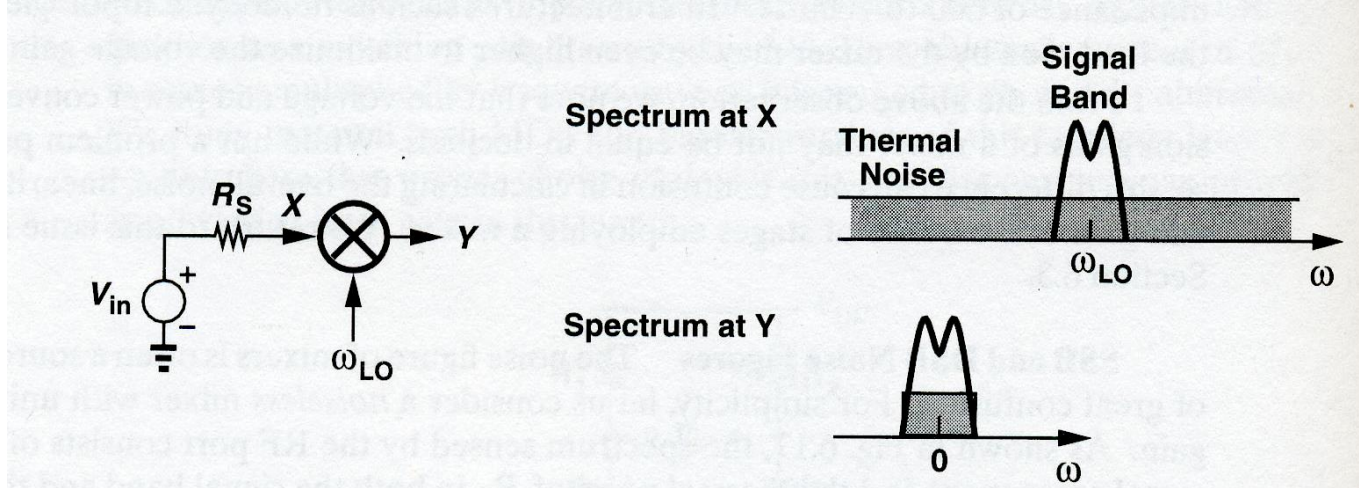
# Mixer Noise Figure; SSB



- In single-sideband mixer ( $f_{RF} \neq f_{LO}$ )
  - Noise is on both sidebands
  - Signal is on ONE sideband
- The NF of "noiseless SSB mixer" is 3 dB
- Heterodyne receivers: image filter before mixer



# Mixer Noise Figure; DSB



- In double-sideband mixer
  - Noise is on both sidebands
  - Signal is on both sideband
- The NF of "noiseless DSB mixer" is 0 dB
- Valid parameter for **direct-conversion receivers**

# Simple Mixer Example: MOSFET Drain Current

MOSFET drain current with two input signals:

$$I_{DS} = \frac{K'_n W}{2L} (V_{GS0} - V_T + v_{RF} + v_{LO})^2$$
$$= \frac{K'_n W}{2L} \left[ (V_{GS0} - V_T)^2 - 2(V_{GS0} - V_T)(v_{RF} + v_{LO}) + v_{RF}^2 + v_{LO}^2 + 2v_{RF}v_{LO} \right]$$

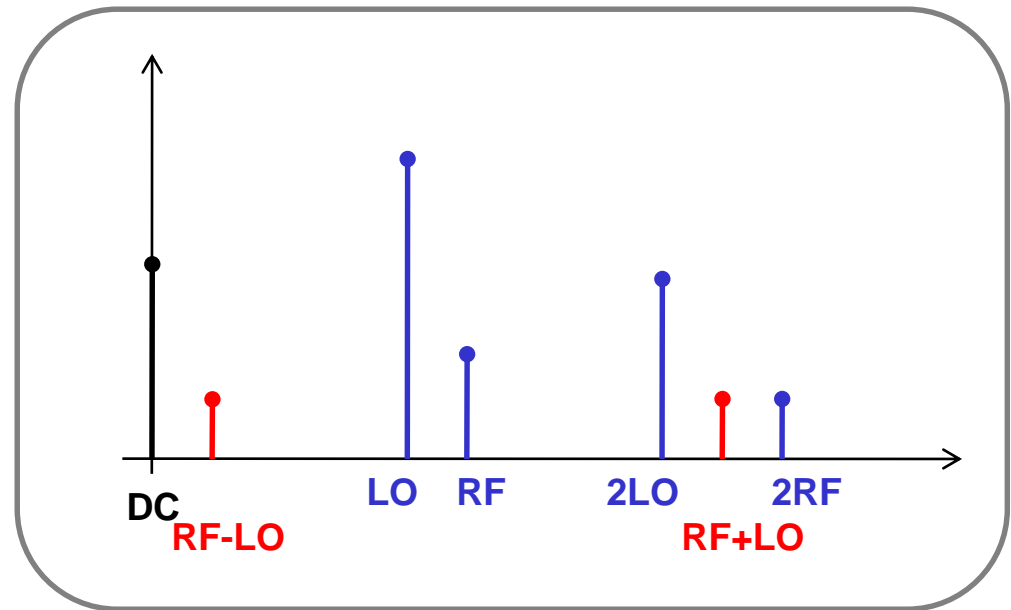
# Simple Mixer Example: MOSFET Drain Current

MOSFET drain current with two input signals:

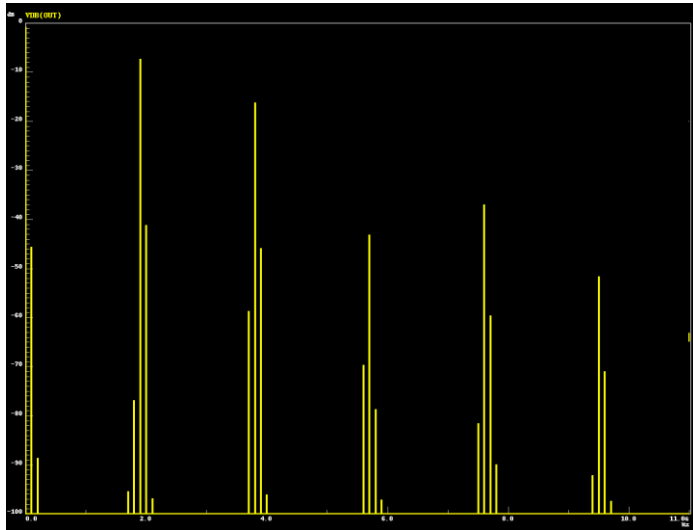
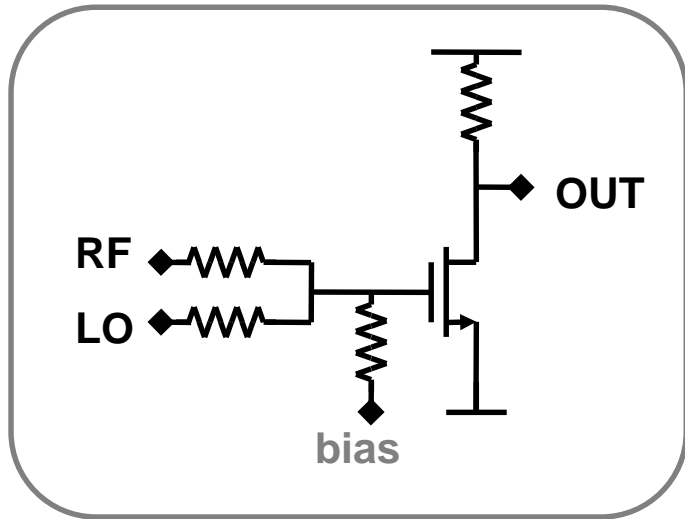
$$I_{DS} = \frac{K'_n W}{2L} (V_{GS0} - V_T + v_{RF} + v_{LO})^2$$
$$= \frac{K'_n W}{2L} \left[ (V_{GS0} - V_T)^2 - 2(V_{GS0} - V_T)(v_{RF} + v_{LO}) + v_{RF}^2 + v_{LO}^2 + 2v_{RF}v_{LO} \right]$$

The output includes

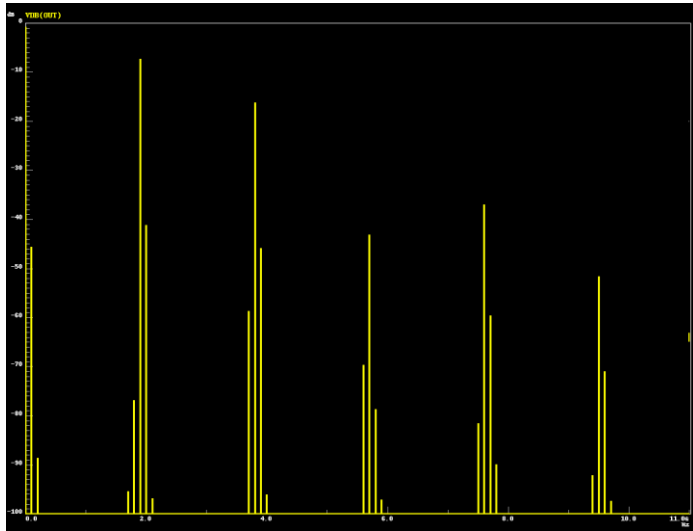
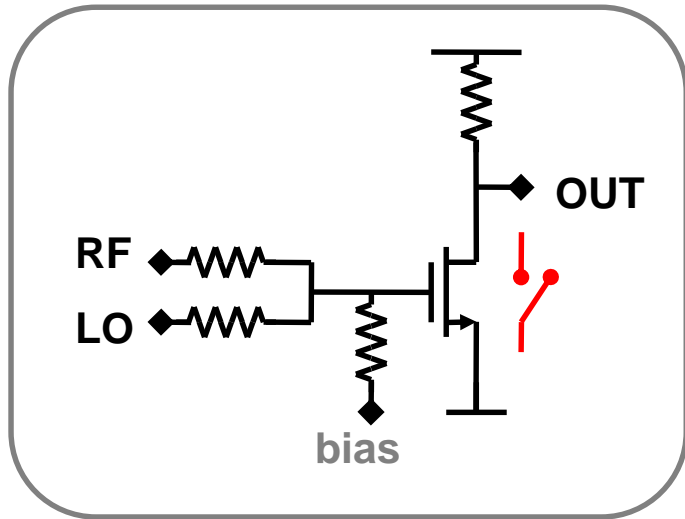
- DC component
- Feedthrough components
- Distortion components
- Mixing product components



# Example: MOSFET Drain Current

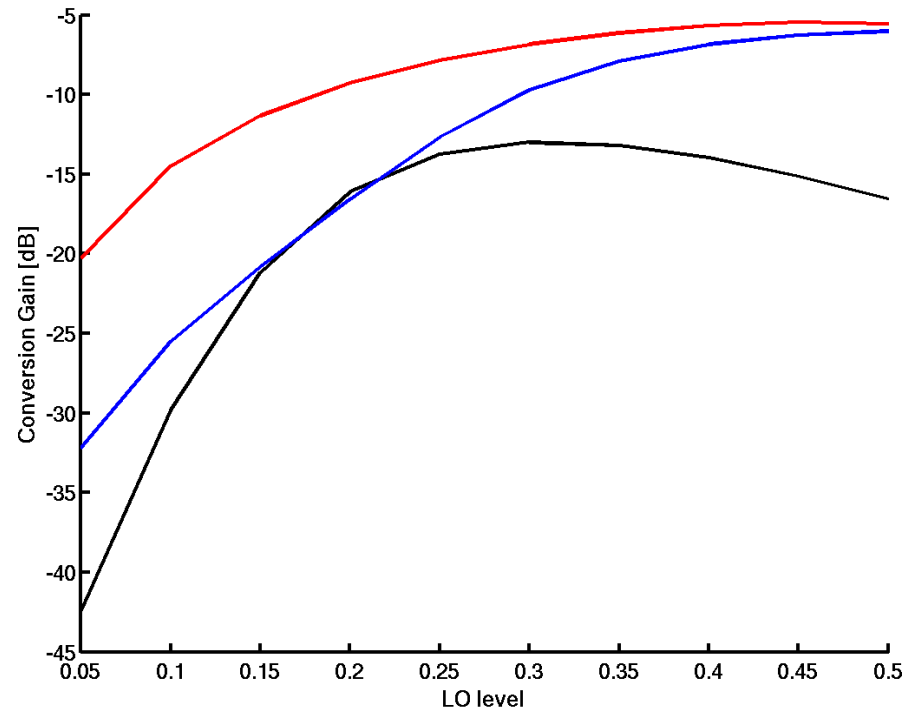


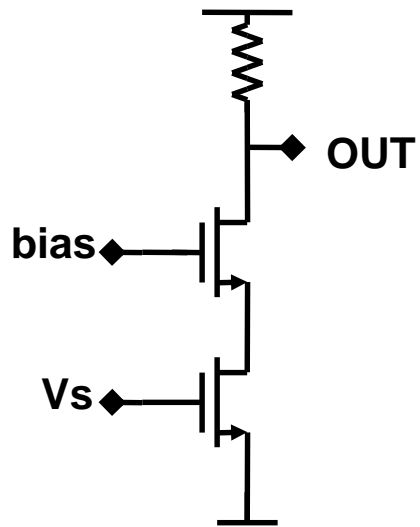
# Example: MOSFET Drain Current



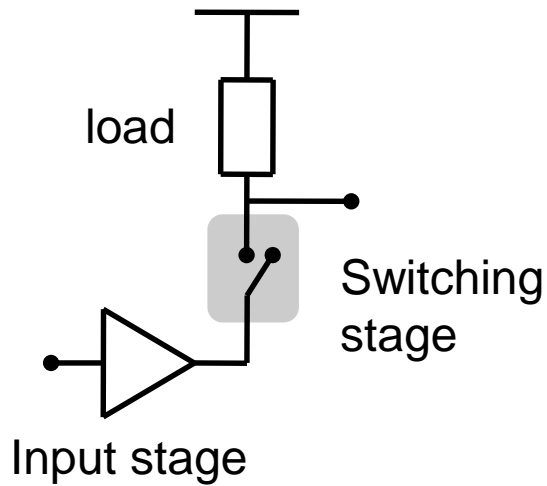
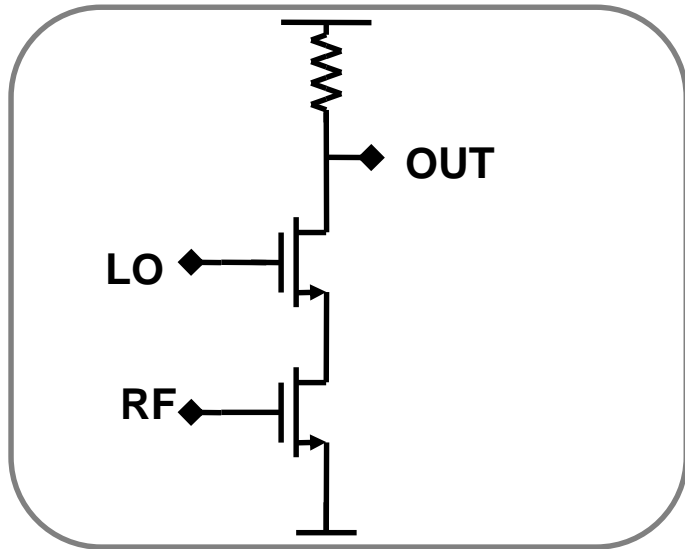
Three "modes"

- Good amplifier, bias=0.6V
- **Switch, "class-C", bias=0.4V**
- **Resistive mixer, bias=0.8V**

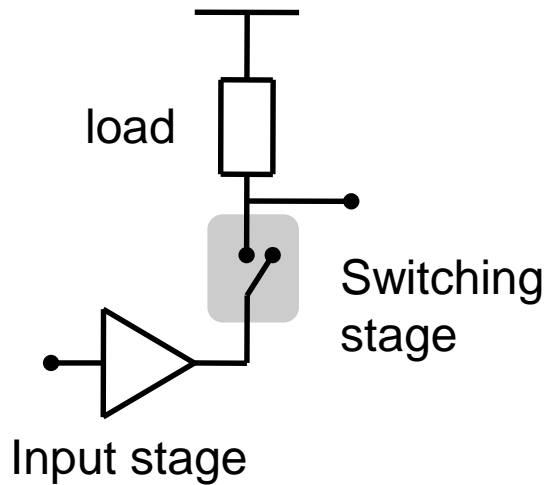
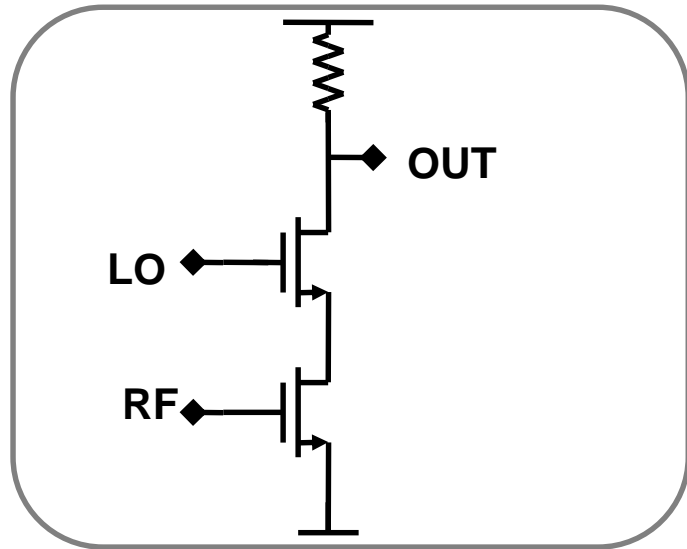




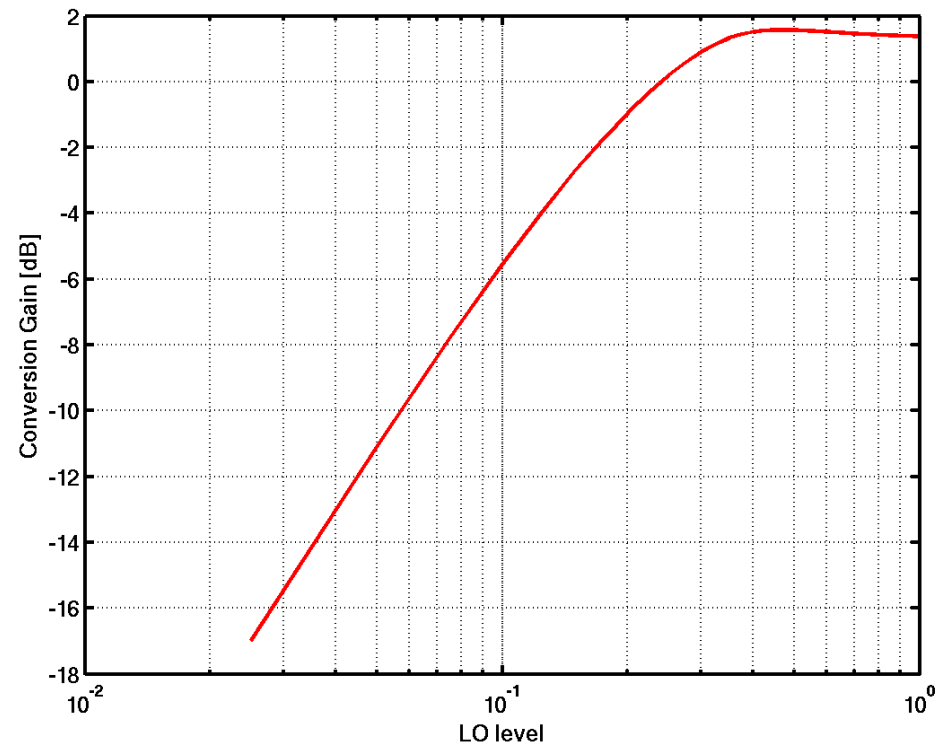
# Cascode Amplifier → Mixer



# Cascode Amplifier → Mixer

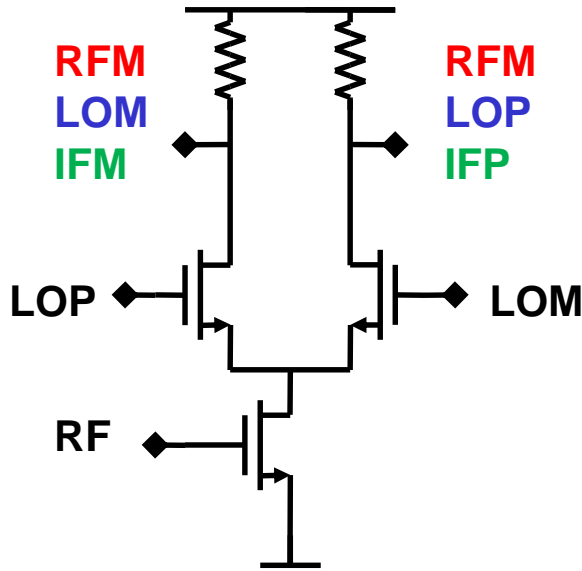


- Active mixer = conversion gain  $> 0$
- Poor port-to-port isolation  
→ *What to do ?*



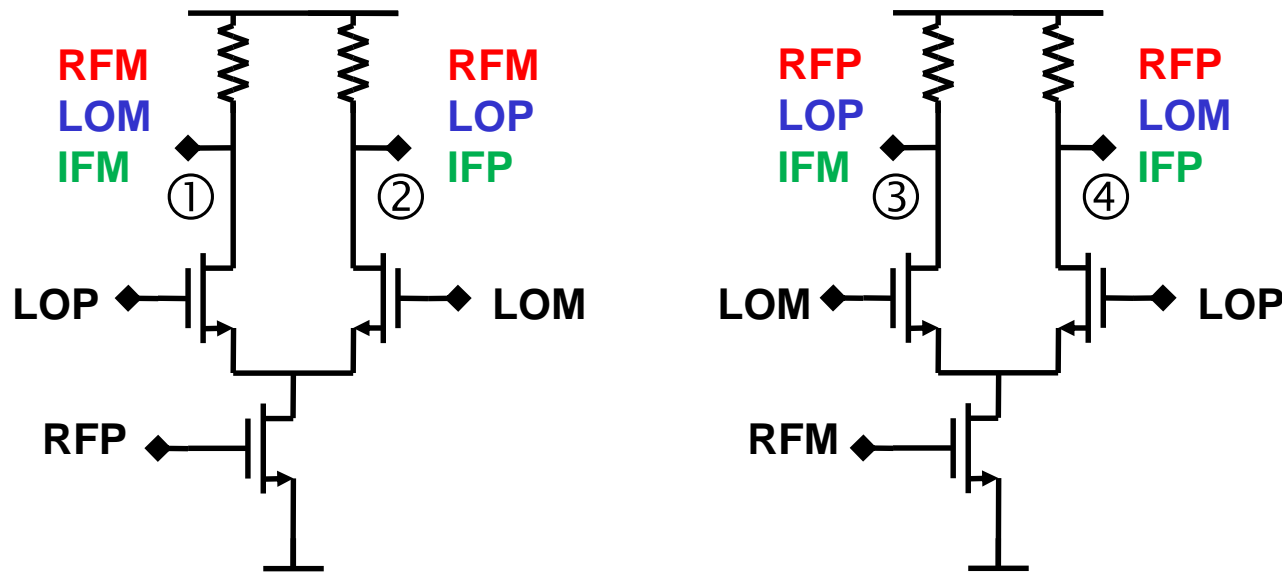


# Single-Balanced Mixer



- Differential LO signal  $\rightarrow$  differential output w/o RF
- Rest of performance essentially same as previously
- Differential LO cancels out RF; how to cancel LO leakage ?

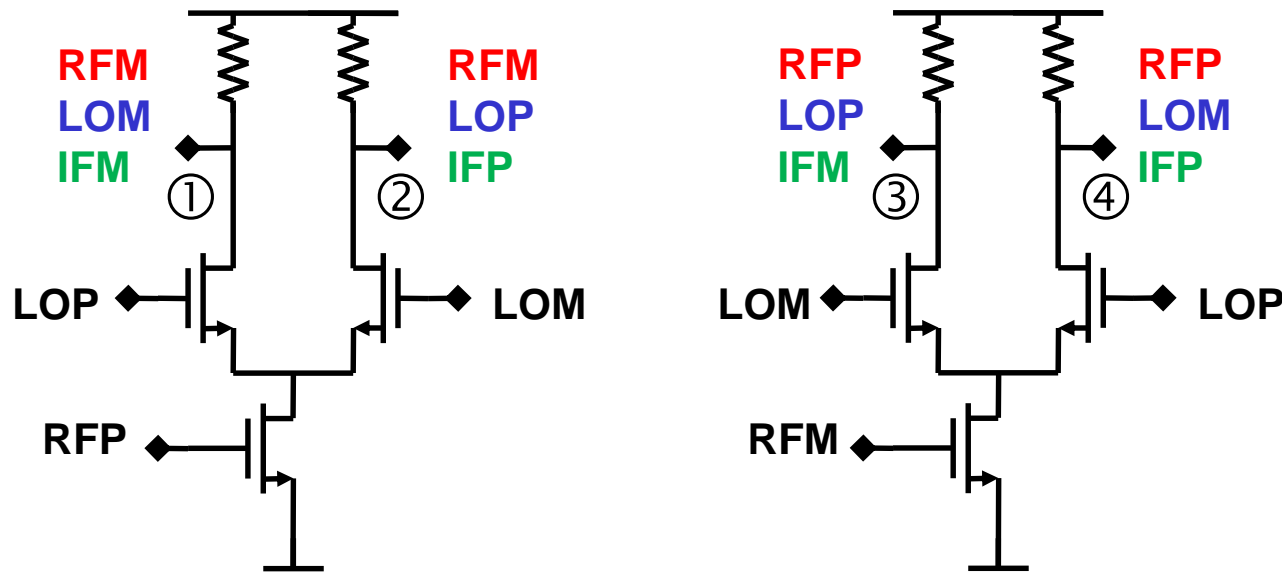
# Double-Balanced Mixer (derivation)



- Differential LO signal → differential output w/o RF
- Differential RF signal → differential output w/o LO

How to combine ① ② ③ ④ ?

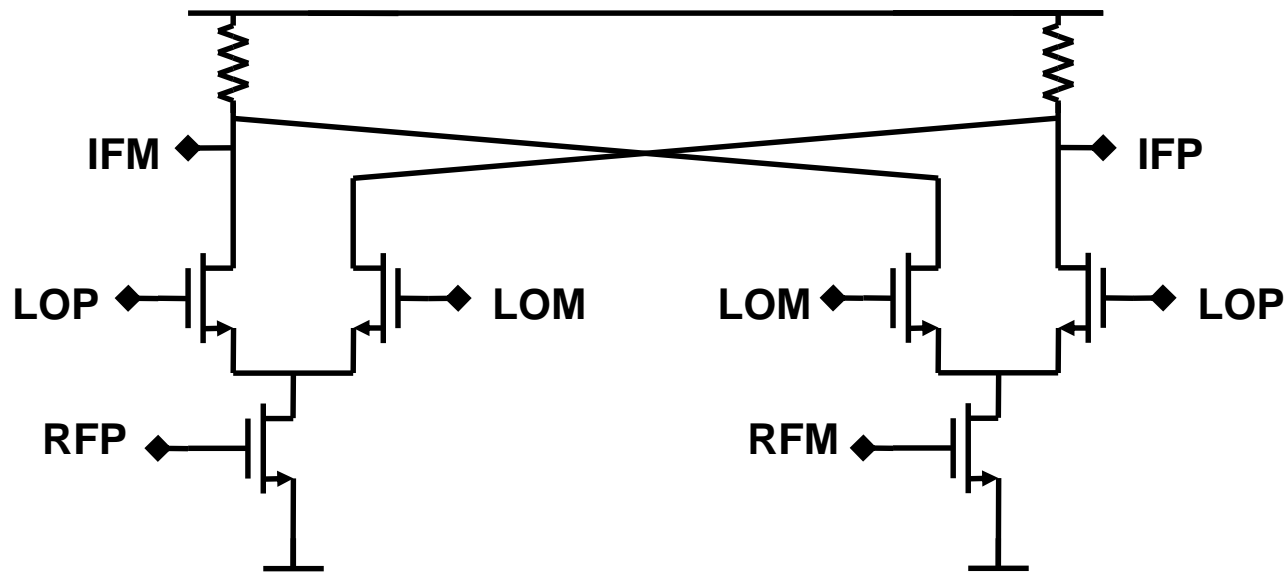
# Double-Balanced Mixer (derivation)



- Differential LO signal → differential output w/o RF
- Differential RF signal → differential output w/o LO

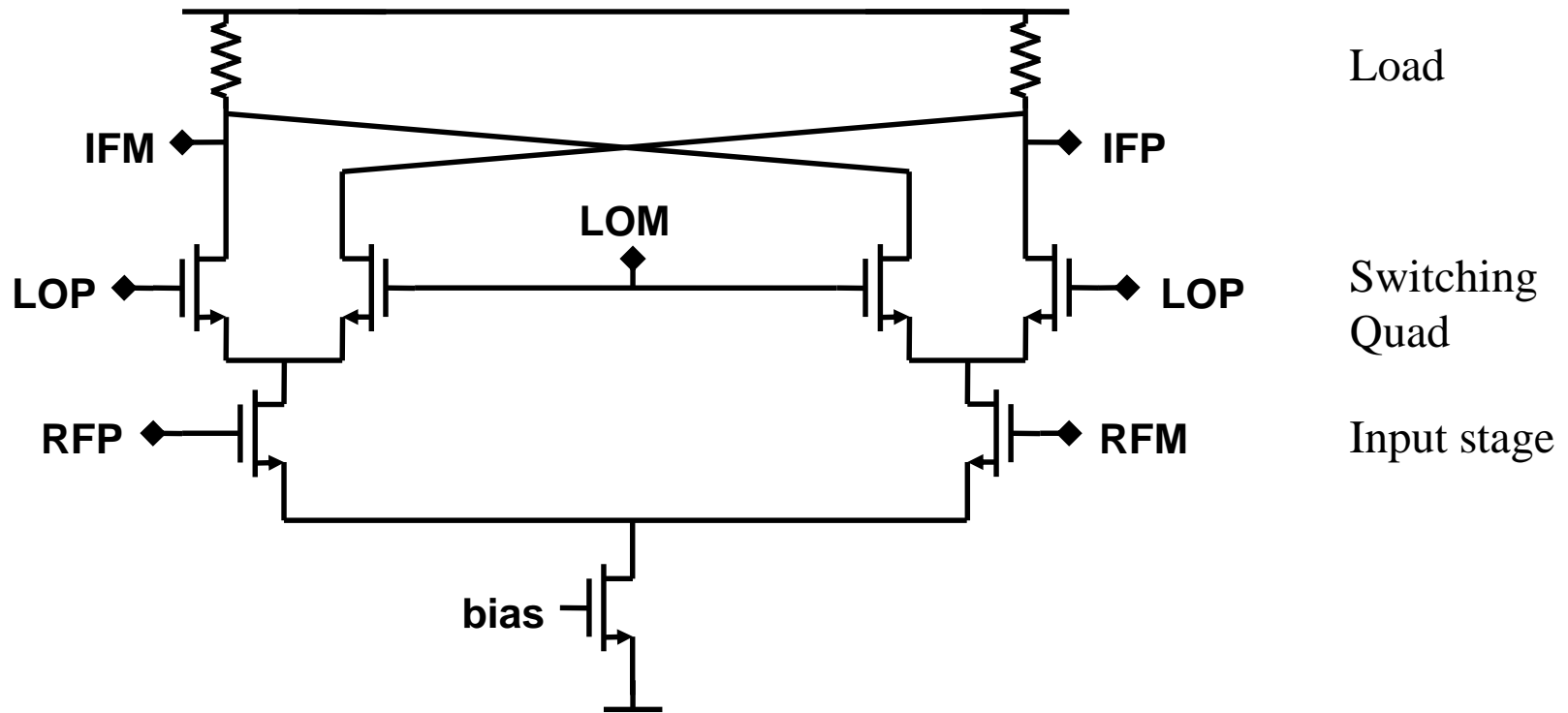
How to combine ① ② ③ ④ ?  $\rightarrow (\textcircled{1} + \textcircled{3}) - (\textcircled{2} + \textcircled{4})$

## Double-balanced Mixer (derivation 2)



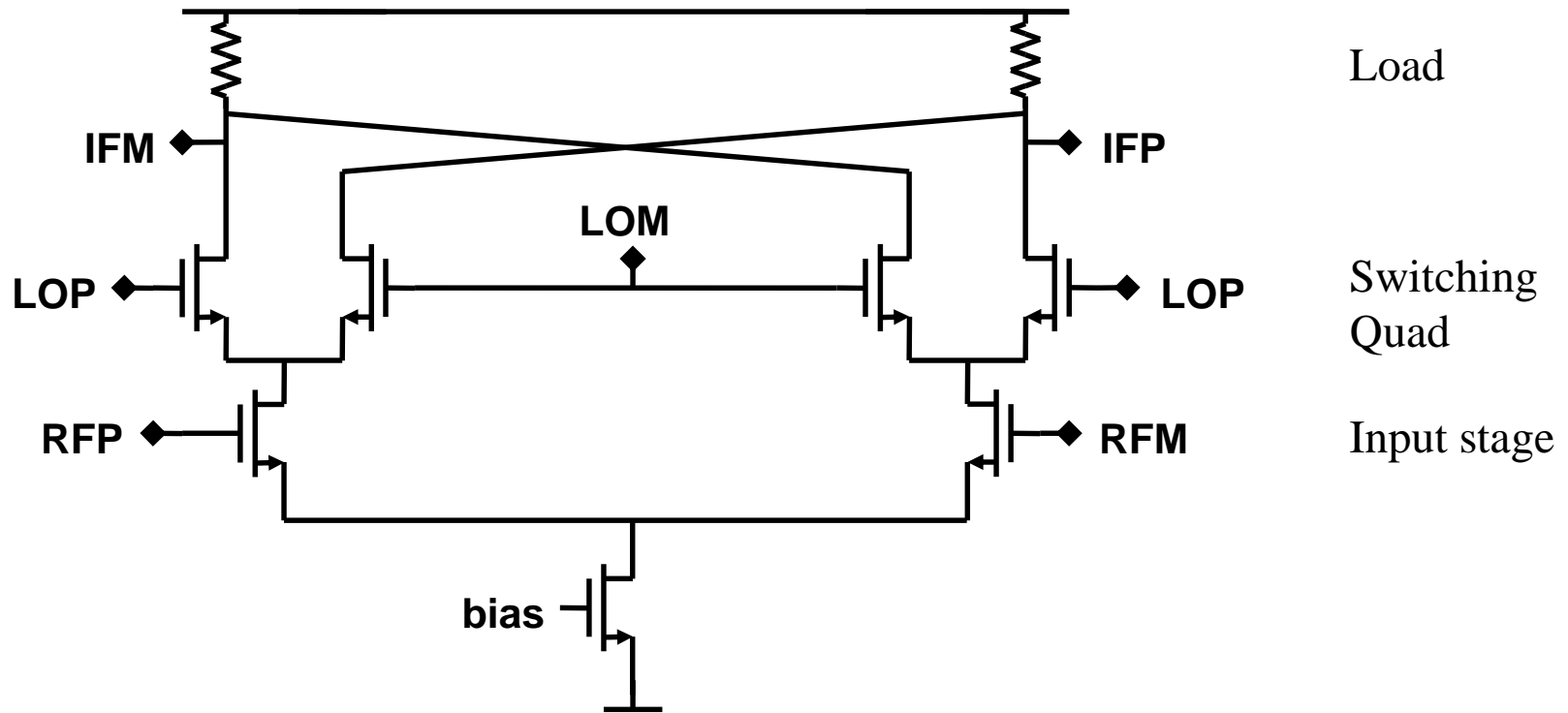
- Independent RF transistors have poor matching  
→ Differential pair helps

# Gilbert Cell Mixer



Gilbert cell mixer was the work horse of RF IC transceivers.  
It dominated until some problems appeared ...

# Gilbert Cell Mixer

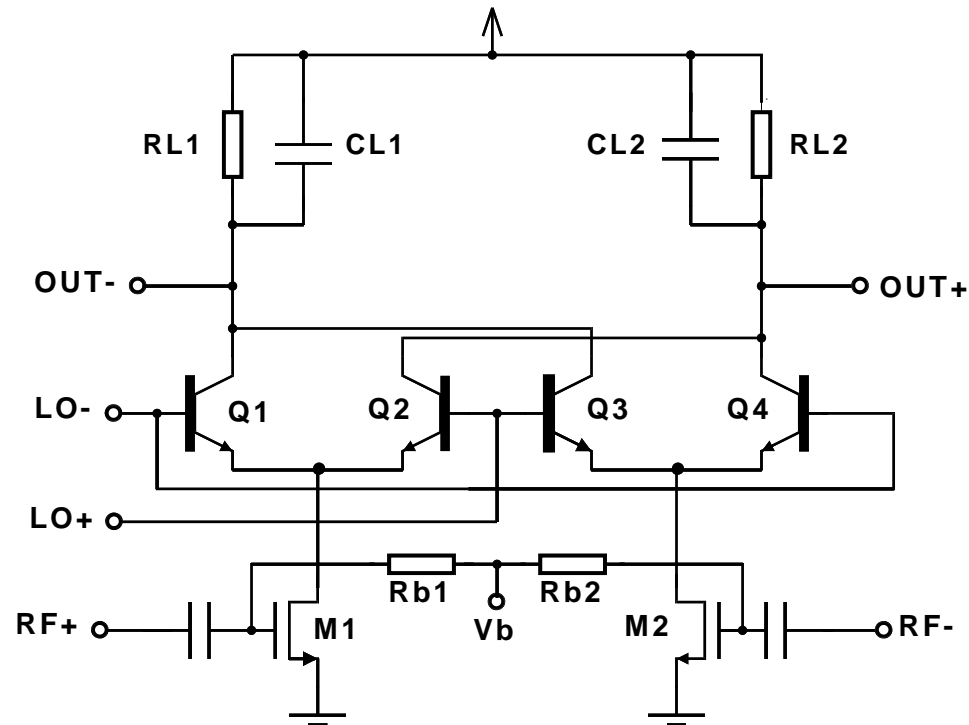


Gilbert cell mixer was the work horse of RF IC transceivers.  
It dominated until some problems appeared ...

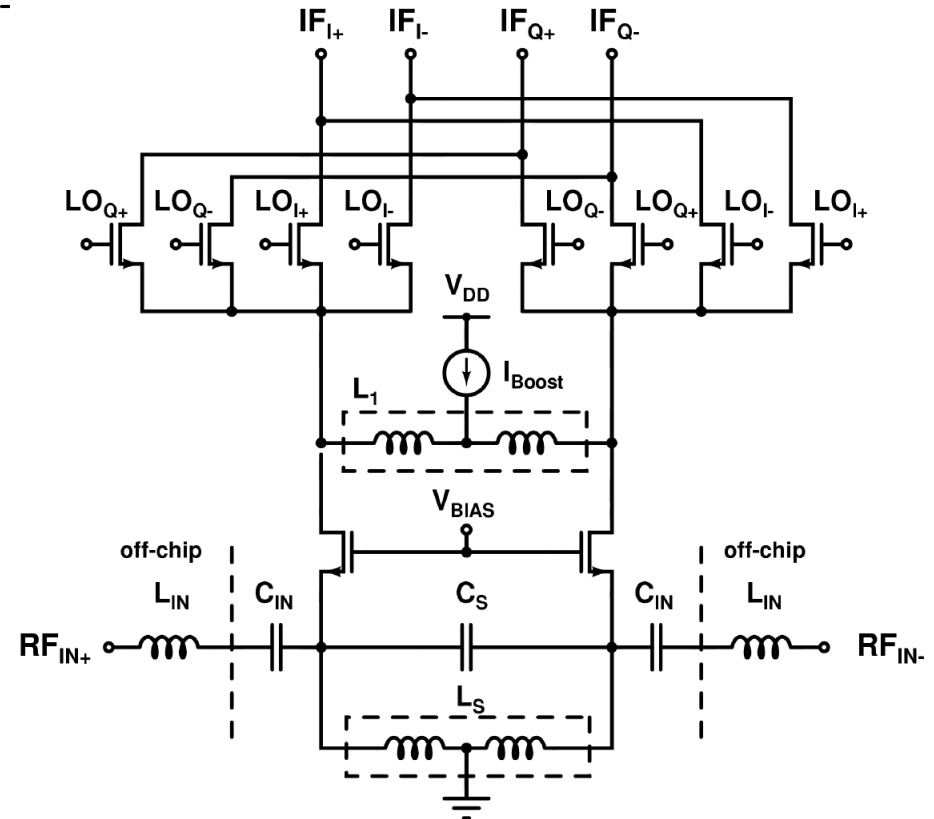
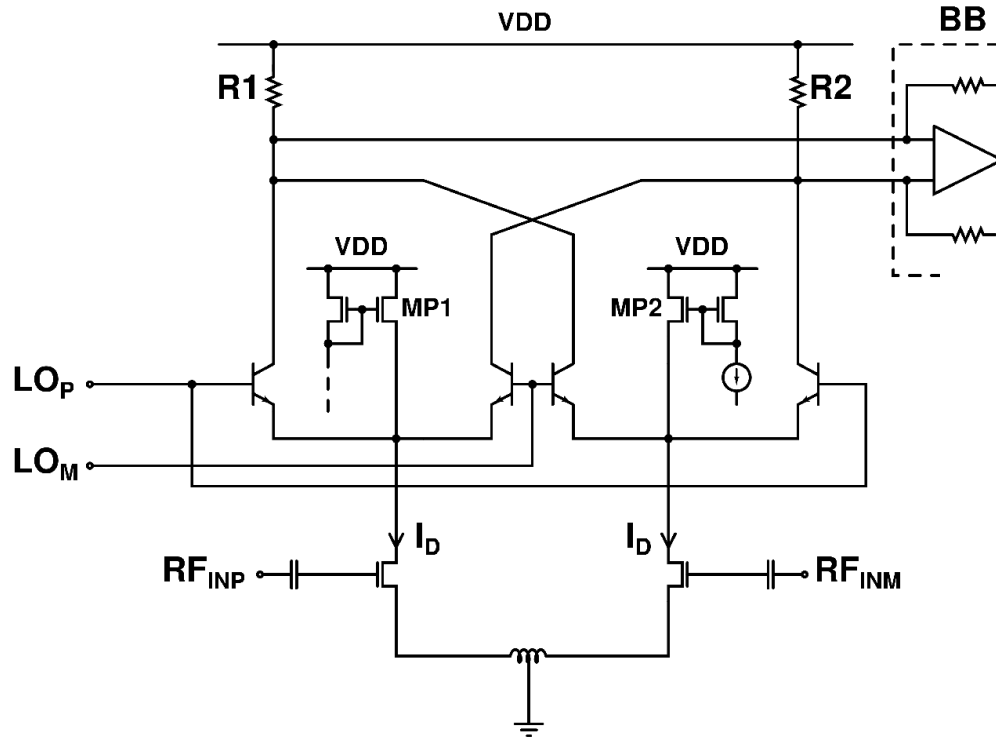
This circuit needs a high supply voltage.

Low-voltage versions have poor characteristics.

# Gilbert Mixer, Examples



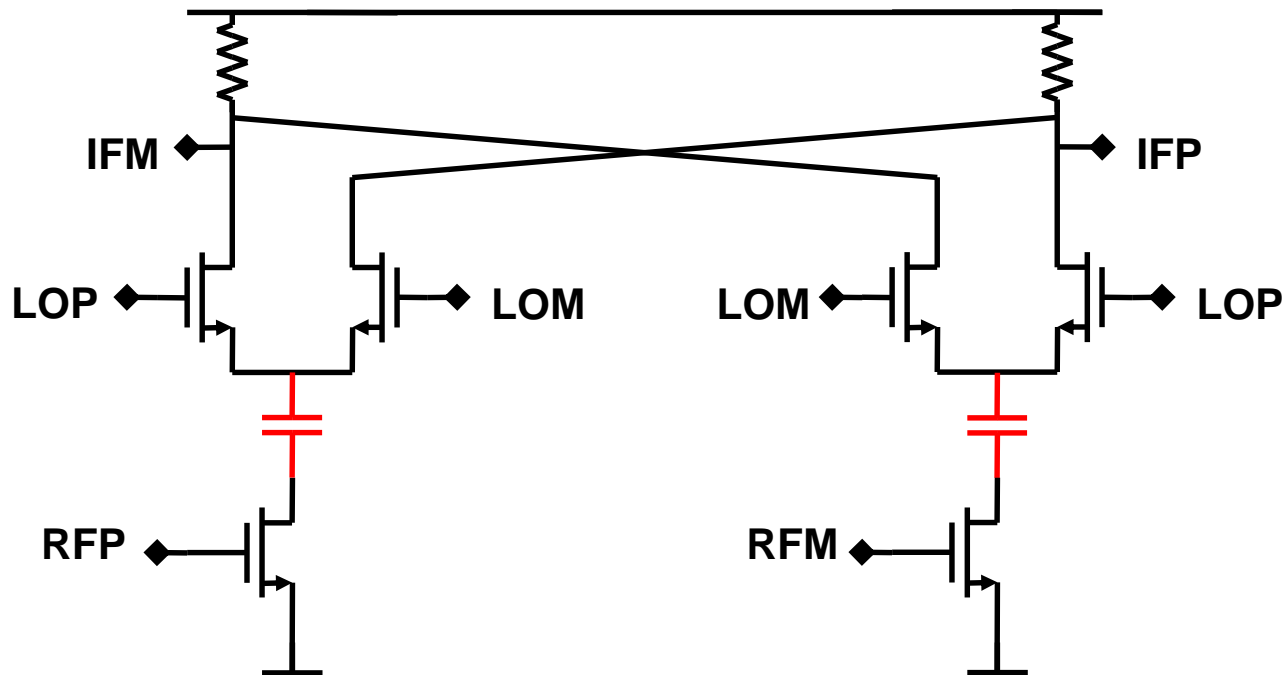
# Gilbert Mixer, Examples





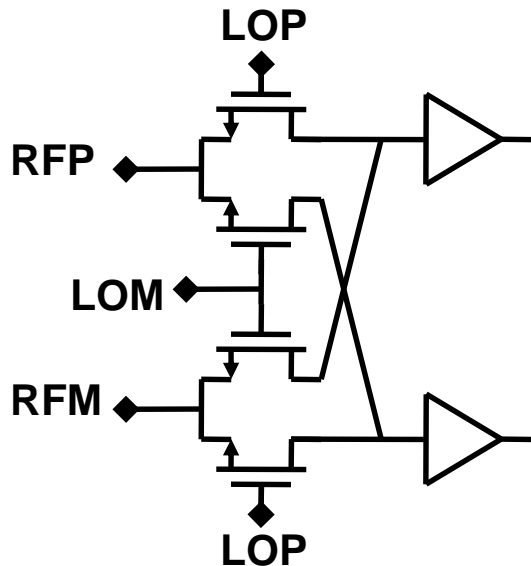
# Passive Mixers

WHY ? Demand for **low supply voltage** and high linearity  
→ Gilbert cell and its variants do not work well

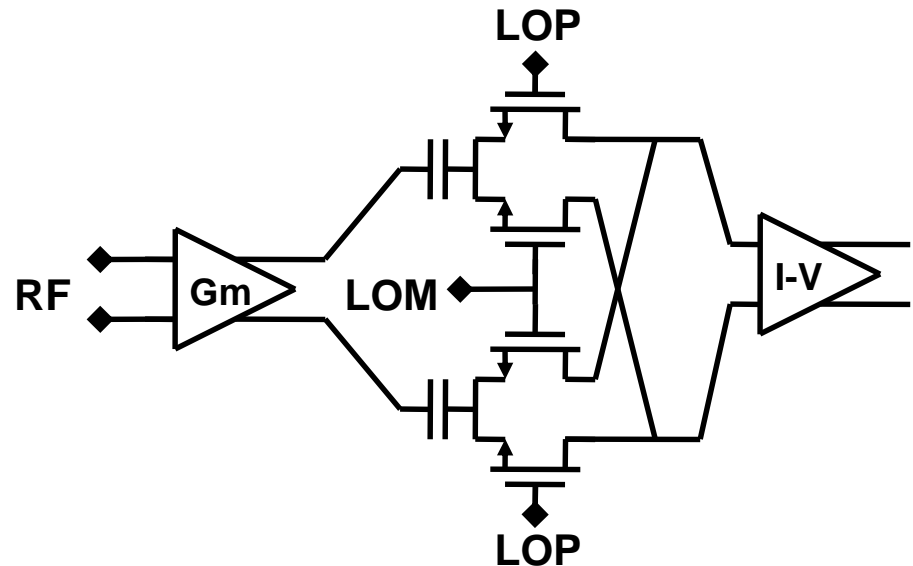


If we ignore DC bias matters, would this work ?

# Voltage-Mode / Current-Mode Passive Mixer



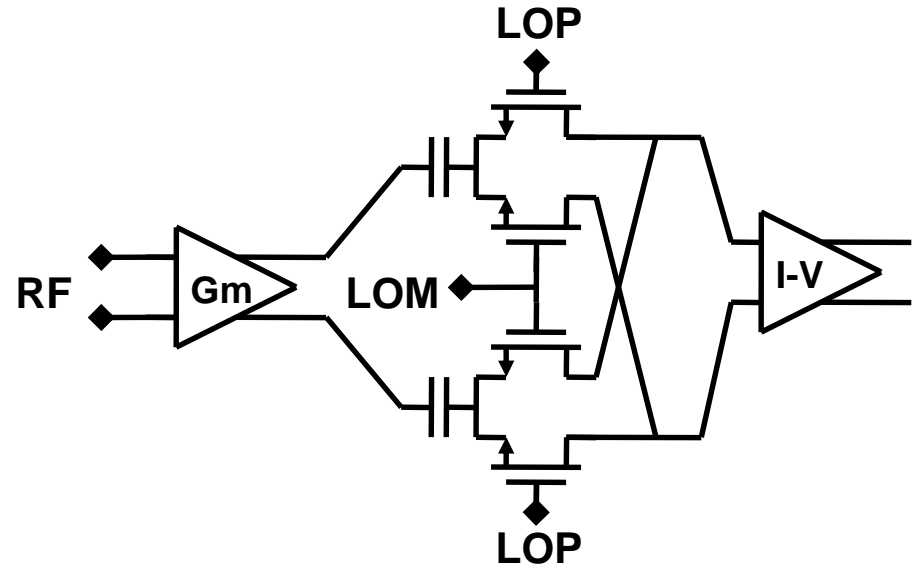
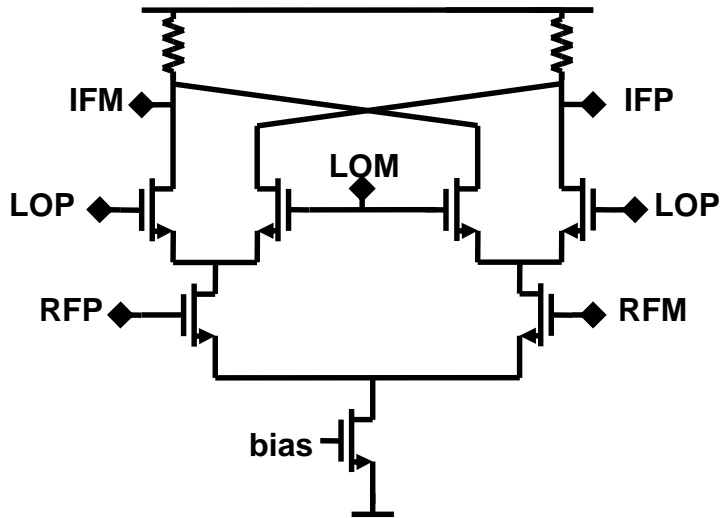
- Input  $V_{in} \rightarrow$  output  $V_{out}$
- $R_{DS(ON)} \ll Z_{in}$   
 $\rightarrow$  high imp output buffer



- Input  $I_{in} \rightarrow$  output  $I_{out}$
- Requires I-V converter (TIA)  
 $\rightarrow$  low imp output buffer

Identification of voltage or current-mode mixer may be difficult and even unnecessary; Main feature is that **no DC current flows** in the mixing FETs

# Active / Passive Mixer

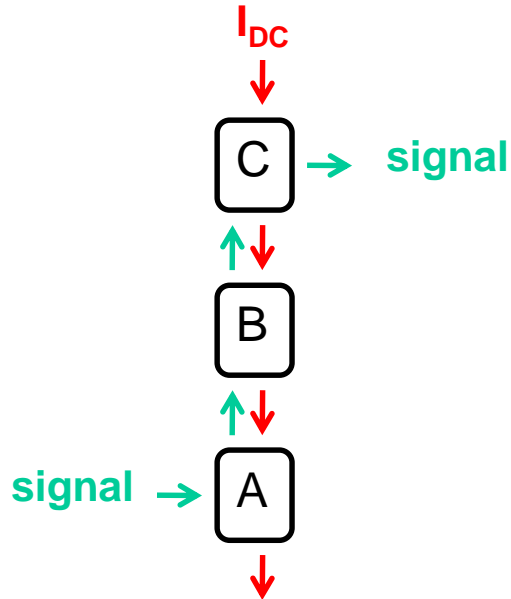


Passive mixer is just a "folded" version of active mixer

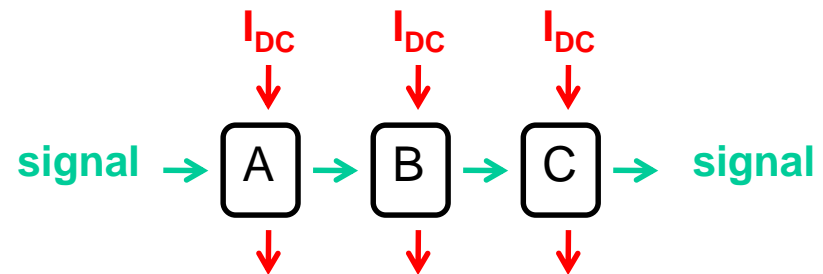
- In an active mixer DC current flows through the switching quad  
→ CG FETs provide gain but also contribute to noise

# Principles

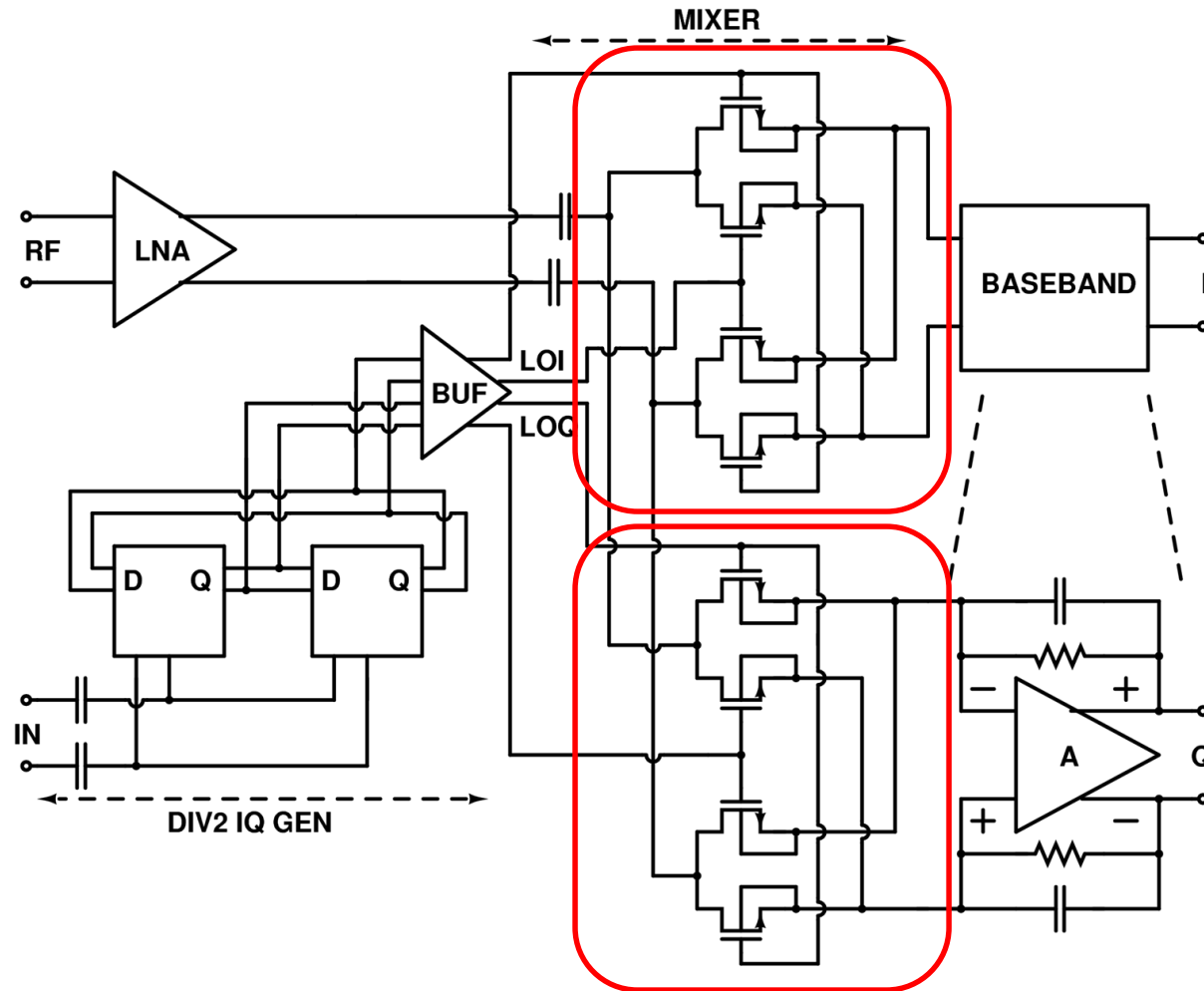
”current re-use”



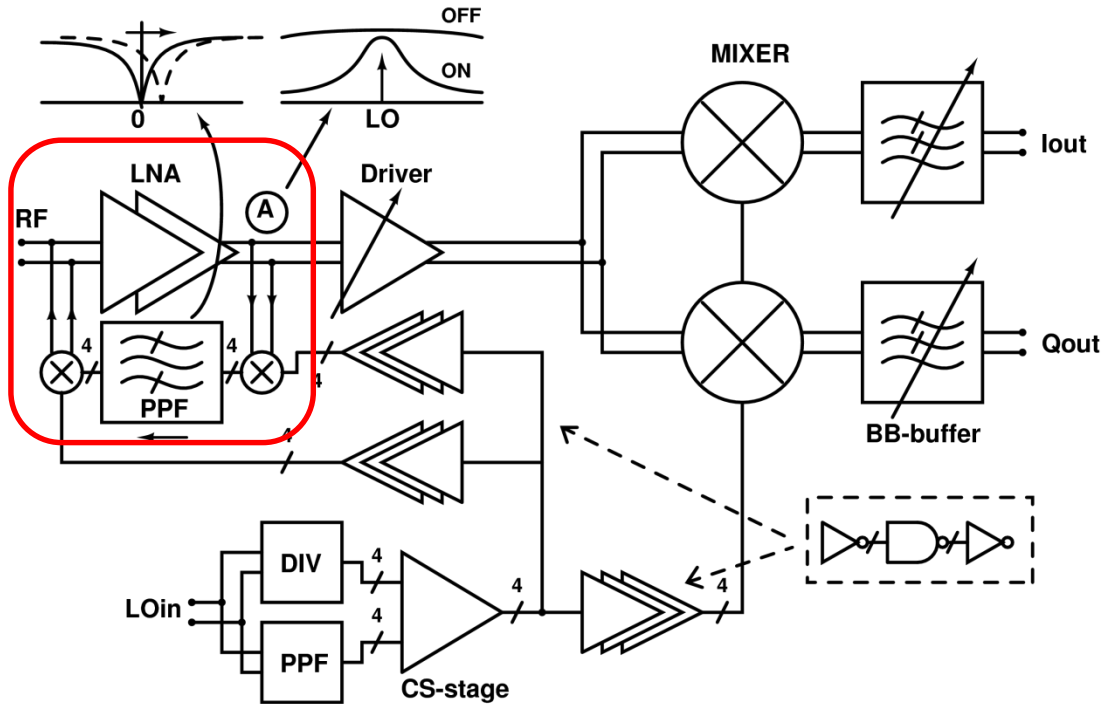
”low voltage”



# Passive Mixer, Use Case 1

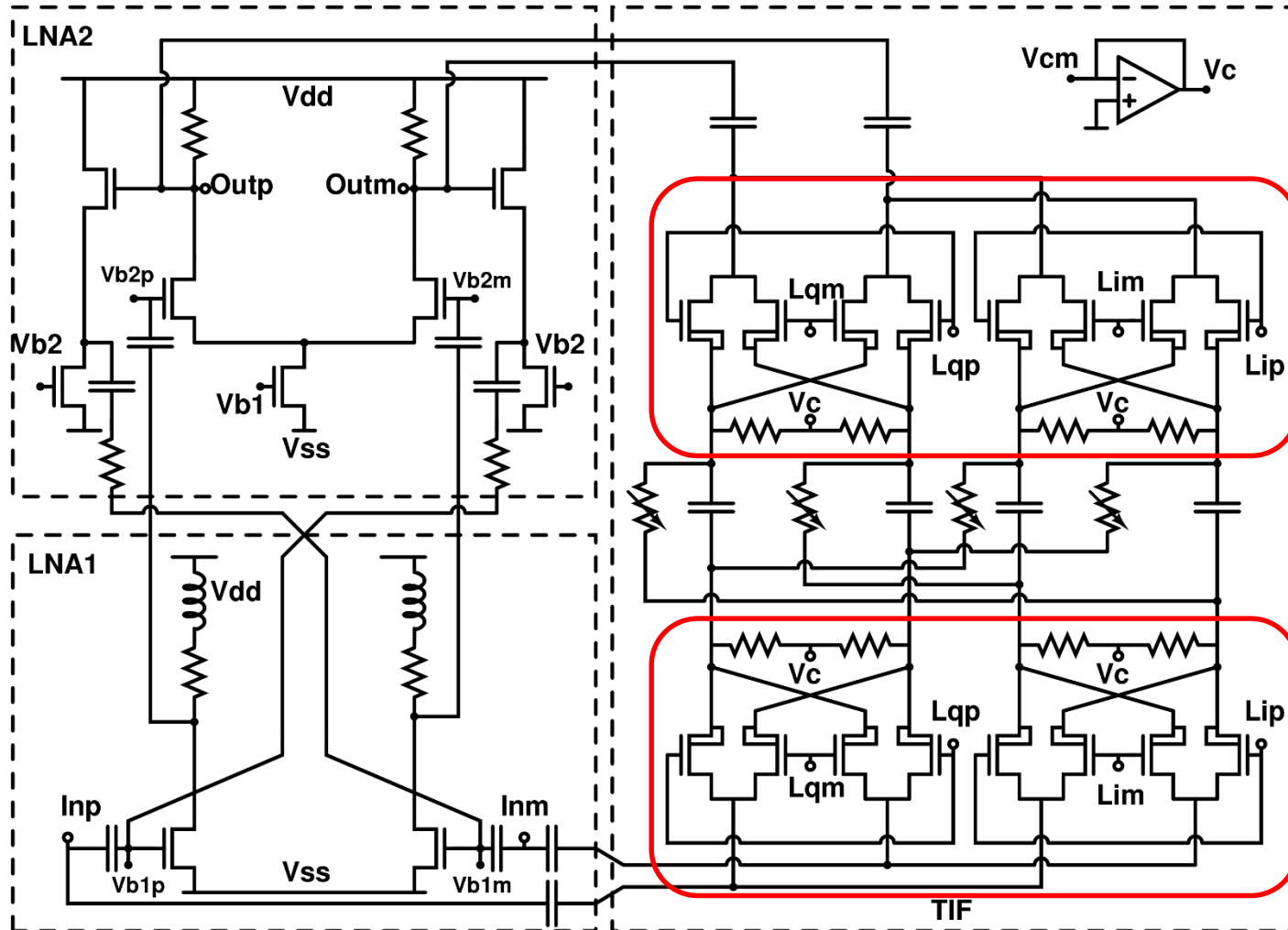


# Passive Mixer, Use Case 2

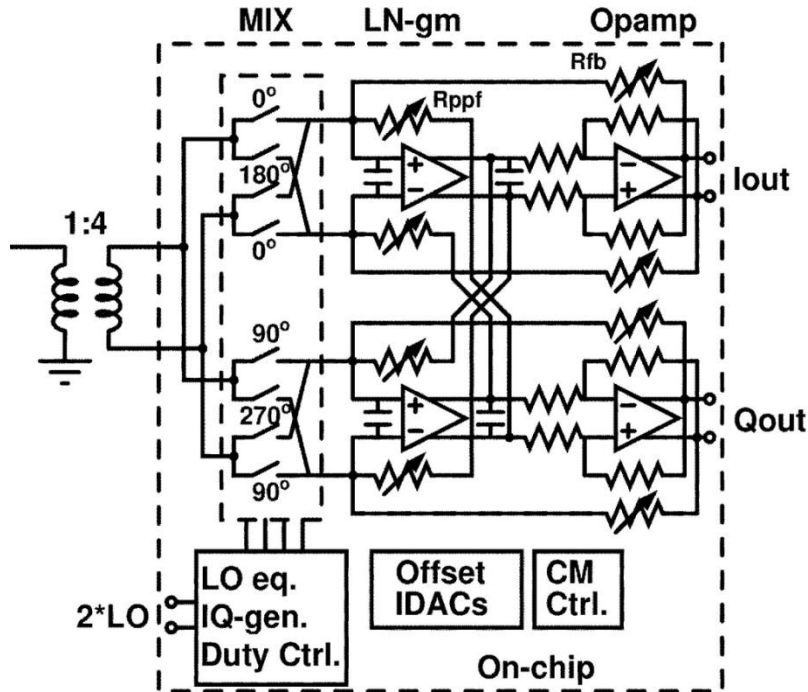


	TIF OFF/ON	TIF OFF/ON	TIF OFF/ON
LO Freq (GHz)	2.4	4.0	5.3
Gain (dB)	42/40	43/41	42/40
IIP3 (dBm)	-11/-5	-13/-5	-11/-7
Blocker ICP (dBm)	-20/-15	-23/-16	-23/-18
NF (dB)	4.3/5.8	3.2/5.7	3.9/5.9
S11 < -10dB (GHz)	2.5-5.5		
LO leak (dBm)	-85/-63	-56/-54	-58/-56
Idc (mA)	45/53	44/56	46/58
Gain Adjustment (dB)	15		
BB bandwidth (MHz)	5-50		
Active area (mm <sup>2</sup> )	0.25		
Technology	1.2V 65nm CMOS		

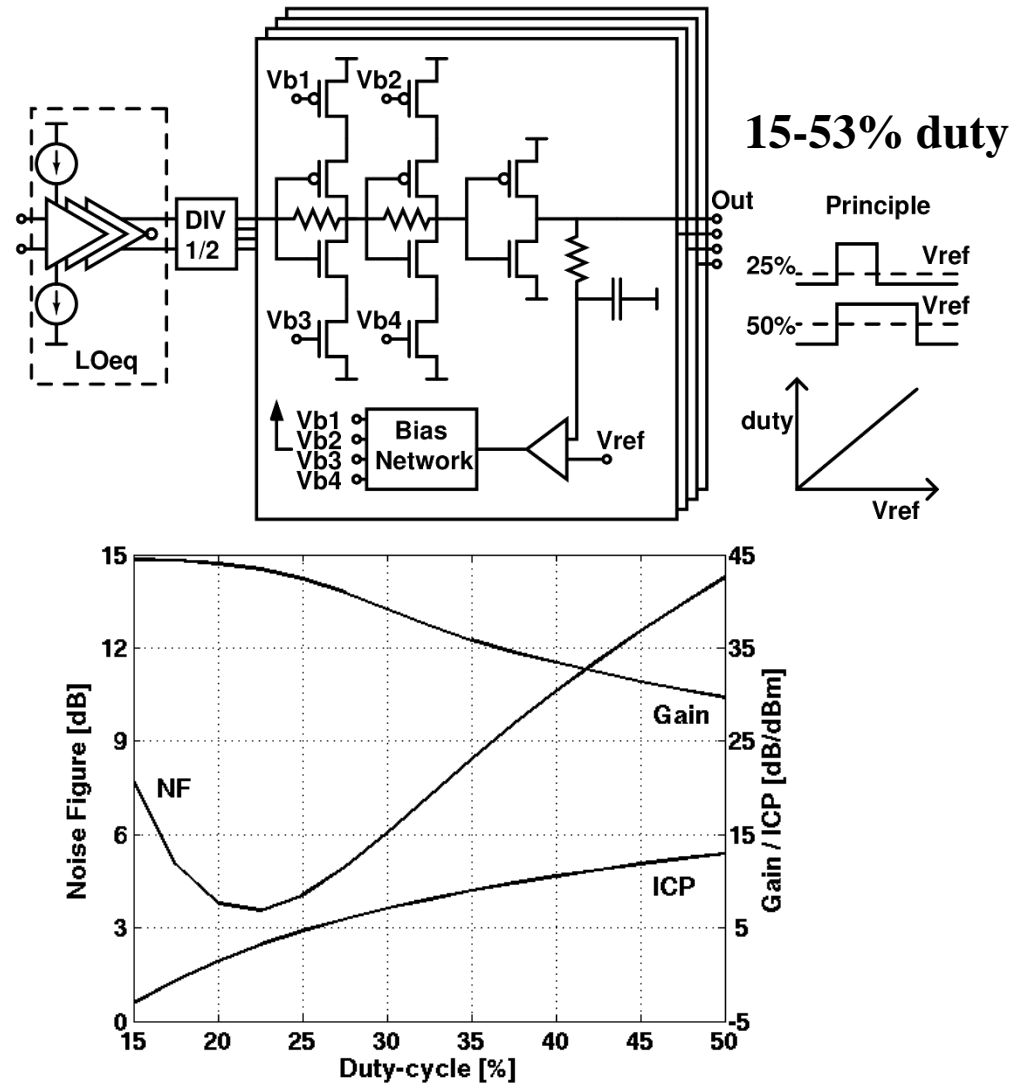
# Passive Mixer, Use Case 2



# Passive Mixer, Case 3



Measured results





# Self-Learning Assignment 4

Objective is to familiarize yourself with passive mixers.

Read three journal papers and write a reference essay.

You can find the assignment from

MyCourses / Assignments - SLA / Self-learning assignment 4

Return your answer as a pdf-file to Return Box in the same page

## Next Meeting Tuesday 3.5.

### Synthesizers

Topics will be

- concepts related to LO / CLK generation
- Synthesis methods
- Oscillators
- Frequency dividers
- IQ generation