Statistical language model (SLM)

- Content today:
 - SLM methods
 - SLM applications
 - Introduction to Neural LMs
- Presented by <u>Mikko Kurimo</u>
- Pics from Sami Virpioja, Kalle Palomäki, Bryan Pellom, Steve Renals, Dan Jurafsky and Tomas Mikolov – thanks!

Contents

- statistical language models and their applications
- maximum likelihood estimation of n-grams
- class-based n-grams
- the main smoothing methods for n-grams
- introduction to other statistical and neural language models

Goals of today

- 1. Learn how to model language by statistical methods
- 2. Learn basic idea of neural language modeling
- 3. Know some typical SLM methods and applications

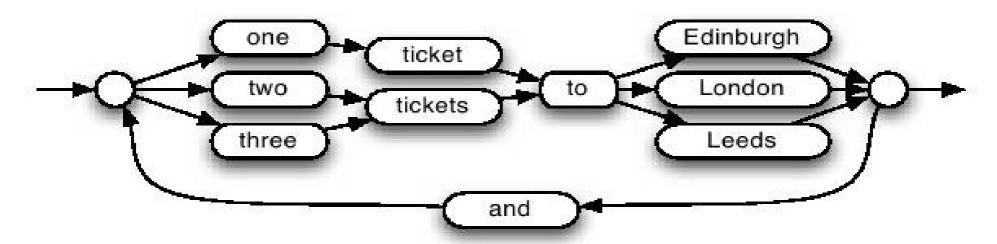
Statistical Language Model

- Model of a natural language that predicts the probability distribution of words and sentences in a text
- Often used to determine which is the most probable word or sentence in given conditions or context
- Estimated by counting word frequencies and dependencies in large text corpora
- Has to deal with: big data, noisy data, sparse data, computational efficiency

Some historical landmarks of SLMs

- Markov chains (Markov, 1913)
- N-grams (Shannon, 1948)
- Predicting unseen events (Good, 1953)
- Landmarks at Aalto University (Helsinki Univ. of Technology)
 - Dynamically expanding context (Kohonen, 1986)
 - Self-organizing semantic maps (Ritter and Kohonen, 1989)
 - WEBSOM for organizing text collections (Kohonen, 1996)
 - Morfessor for unsupervised analysis of words (Lagus. 2002)
 - Varigram LM for sequencies of words (Siivola, 2005)
 - Unlimited vocabulary LMs for speech recognition (Hirsimäki, 2006)
 - Class n-gram models for very large vocabulary speech recognition of Finnish and Estonian (Varjokallio, 2016)
 - An Extensible Toolkit for Neural Network LMs (Enarvi, 2016)

A simple statistical language model



- Limited domain models, constructed by hand
- Transition probabilities can be estimated statistically
- Only a very limited set of sentences are recognized

N-gram language model

- Stochastic model of the relations between words
 - Which words often occur close to each other?
- The model predicts the probability distribution of the next word given the previous ones
- A conditional probability of word given its context
- Estimated from a large text corpus (count the contexts!)
- Smoothing and pruning required to learn compact long-span models from sparse training data

N-gram models

- E.g. trigram = 3-gram:
- Word occurrence depends only on its immediate short context
- A conditional probability of word given its context
- Estimated from a large text corpus (count the contexts!)

```
the united states of ???
P(states | the united )
P(of | united states)
→ P(America | states of) =
 P(Belgium | states of) = ...
```

Estimation of N-gram model

$$P(w_i \mid w_j) = \frac{c(w_j, w_i)}{c(w_j)} \qquad \frac{c(\text{"eggplant stew"})}{c(\text{"eggplant"})}$$

- Bigram example:
 - Start from a maximum likelihood estimate
 - probability of P("stew" | "eggplant") is computed from counts of "eggplant stew" and "eggplant"

	1	want	to	eat	Chinese	food	lunch
1	8	1087	0	13	0	0	0
want	3	0	786	0	6	8	6
to	3	0	10	860	3	0	12
eat	0	0	2	0	19	2	52
Chinese	2	0	0	0	0	120	1
food	19	0	17	0	0	0	0
lunch	4	0	0	0	0	1	0

1	3437
want	1215
to	3256
eat	938
Chinese	213
food	1506
lunch	459

Uni-gram counts

Calculate missing bi-gram probabilities

	I	want	to	eat	Chinese	food	lunch
1	.0023		0	.0038	0	0	0
want	.0025	0	.65	0	.0049	.0066	
to	.00092	0	.0031	.26		0	.0037
eat	0	0	.0021	0	.020	.0021	.055
Chinese	.0094	0	0	0	0	.056	.0047
food	.013	0	.011	0	0	0	0
lunch	.0087	0	0	0	0	.0022	0

	I	want	to	eat	Chinese	food	lunch
1	8	1087	0	13	0	0	0
want	3	0	786	0	6	8	6
to	3	0	10	860	3	0	12
eat	0	0	2	0	19	2	52
Chinese	2/	0	0	0	0	120	1
food	19	0	17	0	0	0	0
lunch	4	0	0	0	0	1	0

Uni-gram counts

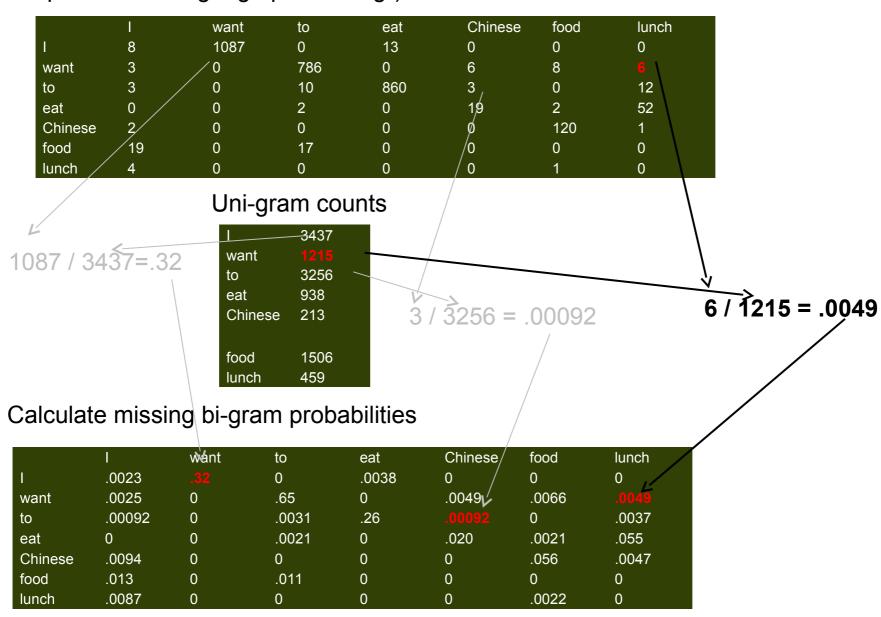
1087 / 3437=.32

	- 3 437
want	1215
to	3256
eat	938
Chinese	213
food	1506
lunch	459

Calculate missing bi-gram probabilities

		want	to	eat	Chinese	food	lunch
1	.0023		0	.0038	0	0	0
want	.0025	0	.65	0	.0049	.0066	
to	.00092	0	.0031	.26		0	.0037
eat	0	0	.0021	0	.020	.0021	.055
Chinese	.0094	0	0	0	0	.056	.0047
food	.013	0	.011	0	0	0	0
lunch	.0087	0	0	0	0	.0022	0

	1	want	to	eat	Chinese	food	lunch
	8	1087	0	13	0	0	0
want	3	0	786	0	6	8	6
to	3 /	0	10	860	3	0	12
eat	0 /	0	2	0	1/9	2	52
Chinese	2/	0	0	0	ρ	120	1
food	/ 19	0	17	0	0	0	0
lunch	4	0	0	0	0	1	0
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	\	to	3256 938	1			
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		food	1506			/	
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lculate	e missin	lunch	459	bilities	Chinese	food	lunch
	e missin	lunch ig bi-gra	⁴⁵⁹ m proba		Chinese 0	food 0	lunch 0
	I	lunch ng bi-gra wént	459 m proba to	eat	/		
ant	l .0023	lunch ig bi-gra want	459 m proba to 0	eat .0038	0	0	0
ant	l .0023 .0025	lunch ng bi-gra wént .32 0	459 m proba to 0 .65	eat .0038 0	0 .0049	0 .0066	0 X
ant	I .0023 .0025 .00092	lunch ig bi-gra want .32 0 0	459 m proba to 0 .65 .0031	eat .0038 0 .26	0 .0049 .00092	0 .0066 0	0 X .0037
ant at ninese	I .0023 .0025 .00092 0	want 32 0 0	459 m proba to 0 .65 .0031 .0021	eat .0038 0 .26	0 .0049 .00092 .020	0 .0066 0 .0021	0 X .0037 .055



Estimation of N-gram model

$$P(w_i \mid w_j) = \frac{c(w_j, w_i)}{c(w_j)} \qquad \frac{c(\text{"eggplant stew"})}{c(\text{"eggplant"})}$$

- Bigram example:
 - Start from a maximum likelihood estimate
 - probability of P("stew" | "eggplant") is computed from counts of "eggplant stew" and "eggplant"
 - works well for frequent bigrams P("want"|"I") = 1087 / 3437 = 0.32
 - why not for rare bigrams? P("Chinese"|"to") = 3 / 3256 = 0.00092

Exercise 2A: Where to use language models?

- Go in breakout rooms and discuss this topic
- Submit notes from your discussion in MyCourses > Lectures > Lecture 2A exercise return box:
 - List as many potential applications for statistical language models as you can!
 - Typically these are tasks where you need the probability or to find the most probable word or sentence given some background information

Some applications of SLMs

- 1. Spelling correction, text input
- 2. Optical character recognition, e.g. scanning old books
- 3. Automatic speech recognition
- 4. Statistical machine translation
- 5.Text-to-speech
- 6. Automatic question answering
- 7.Chatbots

Data sparsity

- Words and many other linguistic units follow a power-law distribution:
 - Zipf's law: kth frequent word occurs ∝ 1/k
 - "Long tail": few frequent words, lots of very rare words
- E.g. within the first 1.5 million words 23% subsequent trigrams were previously unseen (IBM laser patent text corpus)
- Maximum likelihood estimate overestimates frequencies of ngram that occurred rarely, and underestimates those that did not occur at all. (why?)
- One needs a systematic approach to assign some non-zero probability to unseen words and sequences. This is called smoothing.

Zero probability problem

- If an N-gram is not seen in the corpus, it will get probability = 0
- The higher N, the sparser data, and the more zero counts there will be
- 20K words => 400M 2-grams => 8000G 3-grams, so even the largest corpora have MANY zero counts!

Solutions:

- Equivalence classes: Cluster several similar n-grams together to reach higher counts
- Smoothing: Redistribute some probability mass from seen Ngrams to unseen ones

Equivalence classes

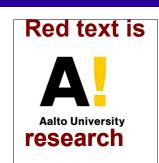
- Divide features (e.g. words) into equivalence classes a.k.a.
 bins
- Assume equal statistical properties within a bin
- Estimate a SLM for the bin as a whole
- The more bins, the more data is needed for model estimation
- The fewer bins, the lower prediction accuracy, because the model becomes too general

Ways to form classes

- Transforming inflected word forms into the baseform: 'saunan', 'saunalle', 'saunojemme', etc. → 'sauna'
- Grouping by part-of-speech tags (the same syntactic role: noun, verb, etc)
- Grouping by semantics (a similar meaning)

Important is that the words in a bin should really behave similarly! E.g. *february, may, august*

Ways to use classes



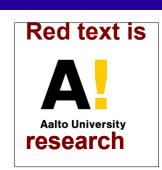
 using equivalence classes only for previous words (Virpioja and Kurimo, 2006):

```
p(wi \mid wi-2, wi-1) = p(wi \mid t(wi-2, wi-1))
```

using class-based n-gram models:

```
p(wi \mid wi-2, wi-1) = p(t(wi) \mid t(wi-2, wi-1))
 \times p(wi \mid t(wi), ...)
```

Combining estimators



- So far, the probability was estimated for all n-grams of a particular length
- How about improving the estimate using shorter sequences that are more frequent?
- The motivation is further smoothing of the estimates by combining different information sources.
- The additional models could also be other n-grams trained on different data, e.g. background models vs topical models
- determine bin-specific interpolation weights for model combination (Broman and Kurimo, 2005)

Backing-off

- In principle: Look for the most specific model that gives sufficient information from the current context
- In practice: Back off from using (too) long contexts to shorter ones that have more samples in the corpus.

Smoothing methods

- **1. Add-one**: Add 1 to each count and normalize => gives too much probability to unseen N-grams
- 2. (Absolute) discounting: Subtract a constant from all counts and redistribute this to unseen ones using N-1 gram probs and back-off (normalization) weights
- 3. Witten-Bell smoothing: Use the count of things seen once to help to estimate the count of unseen things
- **4. Good Turing smoothing**: Estimate the rare n-grams based on counts of more frequent counts
- 5. Best: Kneser-Ney smoothing: Instead of the number of occurrences, weigh the back-offs by the number of contexts the word appears in
- Mastead of only back-safftigases jarinterpolate all N-gram counts 24/58 with N-1 counts

Add-1 smoothing

$$c_i^* = (c_i + 1) \frac{N}{N + V}$$

Probability p = c / N:

$$p_i^* = \frac{c_i + 1}{N + V}$$

Ci*: new count

Ci: original count

N: Num of tokens

V: Total vocab size

	I	want	to	eat	Chinese	food	lunch
I	9	1088	1	14	1	1	1
want	4	1	787	1	7	9	7
to	4	1	11	861	4	1	13
eat	1	1	3	1	20	3	53
Chinese	3	1	1	1	1	121	2
food	20	1	18	1	1	1	1
lunch	5	1	1	1	1	2	1

Figure 6.6 Add-one Smoothed Bigram counts for 7 of the words (out of 1616 total word types) in the Berkeley Restaurant Project corpus of ~10,000 sentences.

$$c_i^* = (c_i + 1) \frac{N}{N + V}$$

Probability p = c / N:

$$p_i^* = \frac{c_i + 1}{N + V}$$

N: Num of tokens

T : Num of types (seen)

Z: Num of types (unseer

V: Total vocab size

$$c_i^* = \begin{cases} \frac{T}{Z} \frac{N}{N+T}, & \text{if } c_i = 0\\ c_i \frac{N}{N+T}, & \text{if } c_i > 0 \end{cases}$$

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	I	want	to	eat	Chinese	food	lunch
I	9	1088	1	14	1	1	1
want	4	1	787	1	7	9	7
to	4	1	11	861	4	1	13
eat	1	1	3	1	20	3	53
Chinese	3	1	1	1	1	121	2
food	20	1	18	1	1	1	1
lunch	5	1	1	1	1	2	1

Figure 6.6 Add-one Smoothed Bigram counts for 7 of the words (out of 1616 total word types) in the Berkeley Restaurant Project corpus of ~10,000 sentences.

,	I	want	to	eat	Chinese	food	lunch
ly	8	1060	.062	13	.062	.062	.062
want	3	.046	740	.046	6	8	6
to	3	.085	10	827	3	.085	12
eat	.075	.075	2	.075	17	2	46
Chinese	2	.012	.012	.012	.012	109	1
food	18	.059	16	.059	.059	.059	.059
lunch	4	.026	.026	.026	.026	1	.026

Figure 6.9 Witten-Bell smoothed bigram counts for 7 of the words (out of 1616 total word types) in the Berkeley Restaurant Project corpus of ~10,000 sentences.

Good-Turing smoothing

- How to compute the probability of an unseen event, e.g. an out-of-vocabulary word?
- Idea invented by Alan Turing during World War 2 when he was working to break German cipher
- Published later by his student (Good, 1953)
- Set:
 - N = Num of words
 - N_c = Num of words that occur c-times (freq. of freq.)
- Estimate prob of unseen things = N_1/N
- Estimate count of things seen once = (c+1)*N_2/N_1
- Smoothed count c* for all c:

$$c^* = (c+1)\frac{N_{c+1}}{N_c}$$

Exercise 2B: Good-Turing smoothing

- Watch a video where Prof. Jurafsky (Stanford) explains Good-Turing smoothing (between 02:00 – 08:45)
 - Click: http://www.youtube.com/watch?v=GwP8gKa-ij8
 - Or search:"Good Turing video Jurafsky"
- Go in breakout rooms and submit answers for 3 questions in MyCourses > Lectures > Lecture 2B exercise return box:
- 1. Estimate the prob. of catching next any new fish species, if you already got: 5 perch, 2 pike, 1 trout, 1 zander and 1 salmon?
- 2. Estimate the prob. of catching next a salmon?
- 3. What may cause practical problems when applying Good-Turing smoothing for rare words in large text corpora?

Hints for solving the exercise

- 1.Estimate the prob of unseen things using the prob of things seen only once N_1/N
- 2. The counts must be smoothed. The new count for things seen once is (c+1)*N_2/N_1
- 3. What if $N_c = 0$ for some c?

Estimation of N-gram model

$$P(w_i \mid w_j) = \frac{c(w_j, w_i)}{c(w_j)} \qquad \frac{c(\text{"eggplant stew"})}{c(\text{"eggplant"})}$$

- Bigram example:
 - Start from a maximum likelihood estimate
 - probability of P("stew" | "eggplant") is computed from counts of "eggplant stew" and "eggplant"
 - works well for frequent bigrams

Backing off

$$P(w_i \mid w_j) = \frac{c(w_j, w_i)}{c(w_j)} \quad \text{if } c(w_j, w_i) > c$$
$$= P(w_i)b_{w_j} \quad \text{otherwise}$$

- Divide the room of rare bigrams, e.g. "eggplant francisco", in proportion to the unigram P("francisco")
- The sum of all these rare bigrams "eggplant [word j]" is b("eggplant") which is called the back-off weight

Absolute discounting and backing off

$$P(w_i \mid w_j) = \frac{c(w_j, w_i) - D}{c(w_j)} \quad \text{if } c(w_j, w_i) > c$$
$$= P(w_i)b_{w_i} \quad \text{otherwise}$$

- If bigram is common: Subtract constant D from the count
- If not: Back off to the unigram probability normalized by the back-off weight
- Similarly back off all rare N-grams to N-1 grams

Kneser-Ney smoothing

$$P(w_i \mid w_j) = \frac{c(w_j, w_i) - D}{c(w_j)} \quad \text{if } c(w_j, w_i) > c$$
$$= \mathbf{V}(w_i)b_{w_j} \quad \text{otherwise}$$

- Instead of the number of occurrences, weigh the back-offs by the **number of contexts** *V*(*word*) the word appears in:
 - In this case the context is the previous word, thus, how many different previous words the corpus has for that word
 - E.g. *P(Stew | EggPlant)* is high, because stew occurs in many contexts
 - But *P(Francisco | EggPlant)* is low, because Francisco is common, but only in "San Francisco"
 Statistical natural language processing

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Smoothing by interpolation

$$P(w_i \mid w_j) = \frac{c(w_j, w_i) - D}{c(w_j)}$$
+
$$P(w_i)b_{w_j}$$

- Like backing off, but always compute the probability as a linear combination (weighted average) with lower order (N-1)gram probabilities
- Improves the probabilities of rare N-grams
- Discounts (D) (and interpolation weights) can be separately optimized for each N using a held-out data

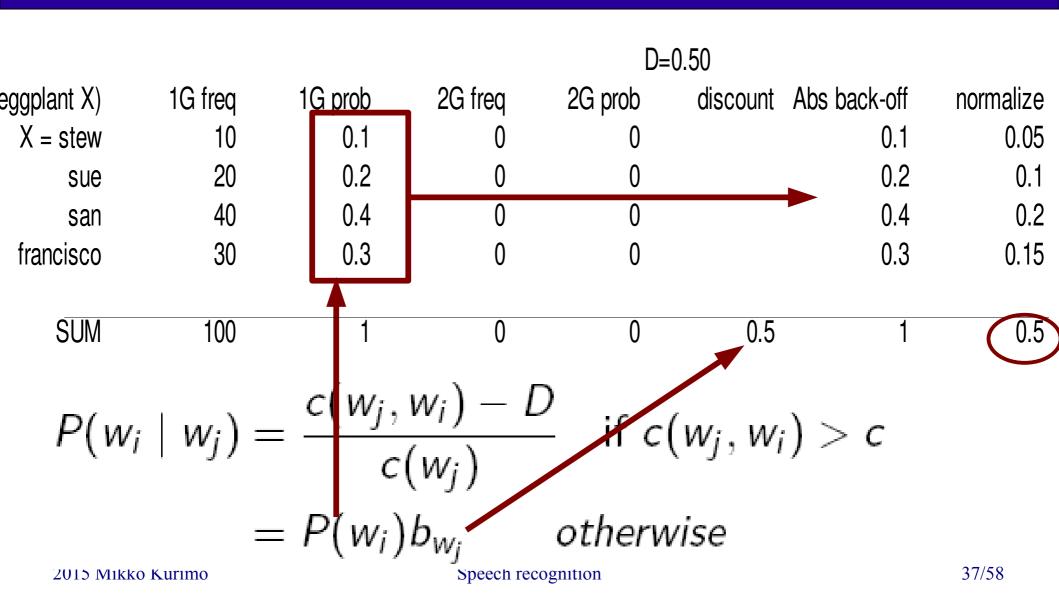
N-gram example

eggplant X) X = stew sue san francisco	1G freq 10 20 40 30	1G prob 0.1 0.2 0.4 0.3	2G freq 0 0 0 0	2G prob 0 0 0		
SUM	100	1	10/100	0		
$P(w_i)$	$ w_j) =$	$\frac{c(w_j, w_j)}{c(w_j)}$	(w_i)	_		

Absolute discounting

			D=0.50						
eggplant X)	1G freq	1G prob	2G freq	2G prob	discount				
X = stew	10	0.1	0	0					
sue	20	0.2	0	0					
san	40	0.4	0	0					
francisco	30	0.3	0	0					
SUM	100	1	0	0	0.5				
P(w)	; w _j) =	$=\frac{c(w_j,}{c}$	$\frac{w_i) - E}{(w_j)}$) - if <i>c</i>	(w_j, w_i)	> <i>c</i>			
			`		(C=	=0, D=0.5 sele	cted)		

Back-off



Back-off

	D=0.50						
eggplant X)	1G freq	1G prob	2G freq	2G prob	discount A	Abs back-off	normalize
X = stew	10	0.1	0	0		0.1	0.05
sue	20	0.2	0	0		0.2	▲ 0.1
san	40	0.4	0	0		0.4	0.2
francisco	30	0.3	0	0		0.3	0.15
SUM	100	1	0	0	0.5		0.5
$P(w_i)$: w _j) =	$=\frac{c(w_j,}{c}$	$\frac{w_i) - L}{(w_j)}$) - if <i>c</i>	(w_j, w_i)	> <i>c</i>	
	=	$= P(w_i)$	b_{w_i}	otherw	/ise	0.1/	1.0*0.5
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Absolute discounting and back-off

eggplant X)	1G freq	2G freq	Abs back-off	normalize	
X = stew	10	0	0.1	0	
sue	20	0	0.2	0	
san	40	0	0.4	0	
francisco	30	0	0.3	0	
SUM	100	0	1	0	
$P(w_i$	$ w_j) =$	$\frac{c(w_j, c_j)}{c}$	$\frac{(w_i) - E}{(w_j)}$) - if c(v	$(v_j, w_i) > c$
		$P(w_i)$		otherwis	(c=0, D=0.5 selected)
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2015 Mikko Kurimo Speech recognition 39/58

Kneser-Ney smoothing

(eggplant X)	1G freq	2G freq	Abs back-off	normalize	#contexts		
X = stew	10	0	0.1	0	10		
sue	20	0	0.2	0	5		
san	40	0	0.4	0	3		
francisco	30	0	0.3	0	1		
SUM	100	0	1	0	19		
$P(w_i \mid w_j) = \frac{c(w_j, w_i) - D}{c(w_j)}$ if $c(w_j, w_i) > c$							
$=\mathbf{V}(w_i)b_{w_i}$ otherwise (c=0, D=0.5 selected)							
2015 Mikko	Kurimo		Speech r	recognition		40/58	

Kneser-Ney smoothing

(eggplant X)	1G freq	2G freq	Abs back-off	normalize	#contexts	KN back-off		
X = stew	10	0	0.1	0.05	(10)	0.26		
sue	20	0	0.2	0.1	5	0.13		
san	40	0	0.4	0.2	3	0.08		
francisco	30	0	0.3	0.15	1	0.03		
SUM	100	0	1	0.5	19	0.5		
$P(w_i \mid w_j) = \frac{c(w_j, w_i) - D}{c(w_j)}$ if $c(w_j, w_i) > c$								
	_	$V(w_i)$	` 2'	otherwi	ise (c:	=0, D=0.5 sel 10/	edted) 19*0.5	

Speech recognition

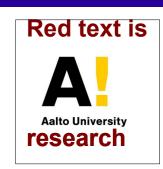
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Weaknesses of N-grams

- Skips long-span dependencies:
 - "The girl that I met in the train was ..."
- Too dependent on word order:
 - "dog chased cat": "koira jahtasi kissaa" ~ "kissaa koira jahtasi"
- Dependencies directly between words, instead of latent variables, e.g. word categories

Some model variants

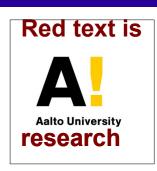


- Variable-length n-gram, aka. Varigram:
 - Span depends on particular context, optimized for the data, e.g. [Siivola, 2007]
 - Especially useful for short units (letters, morphemes)
- Class-based n-gram, e.g. [Brown, 1992]:
 - Cluster words into classes, find class sequences
 - Reduces sparsity, model size, and accuracy
- Bayesian n-gram:
 - Computationally demanding
 - Kneser-Ney smoothing approximates hierarchical Pitman-Yor process model [Goldwater, 2006; Teh, 2006]

Sources and further reading

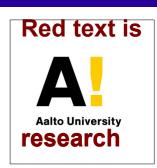
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Other language modeling approaches



- Maximum-entropy LM (Rosenfeld, 2007)
 - Combines different knowledge sources into a single model
 - Good for adaptation (Alumäe and Kurimo, 2010)
- Continuous-space LM (a.k.a. Neural Network LM (NNLM))
 - Map words to continuous-valued vectors and models them using DNN (Bengio et al, 2003; Siivola and Honkela, 2003)
 - State-space models can use indefinitely long contexts, such as in Recurrent Neural Networks (Mikolov et al, 2010)
- Cache models and Topic models

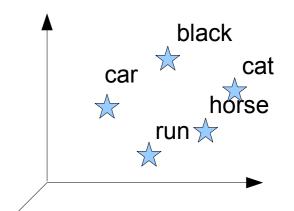
Maximum entropy LMs



- Represents dependency information by a weighted sum of features f(x,h) $P(x|h) = \frac{e^{\sum_i \lambda_i f_i(x,h)}}{\sum_{i} e^{\sum_j \lambda_j f_j(x',h)}}$
- Features can be e.g. n-gram counts
- Alleviates the data sparsity problem by smoothing the feature weights (lambda) towards zero
- The weights can be adapted in more flexible ways than n-grams
 - Adapting only those weights that significantly differ from a large background model (Alumäe and Kurimo, 2010)
- Normalization is computationally hard, but can be approximated effectively

Mapping words into continuous space

- Map words into a continuous vector space to learn a distributed representation known as word embedding
- The goal is to use a vector space that keeps similarly behaving words near each other



- Words can be clustered by context, e.g. n-gram probabilities
 - word2vec (Mikolov, 2013) is one widely used option
 - Other embeddings to reflect various contextual properties
- Set of words can be represented by a sum of the vectors
- N-gram can be represented by a sequence of vectors

Continuous space LMs

- Alleviates the data sparsity problem by representing words in a distributed way
- Various algorithms can be used to learn the most efficient and discriminative representations and classifiers
- The most popular family of algorithm is called (Deep) Neural Networks (NN)
 - can learn very complex functions by combining simple computation units in a hierarchy of non-linear layers
 - Fast in action, but training takes a lot of time and labeled training data
- Can be seen as a non-linear multilayer generalization of the maximum entropy model

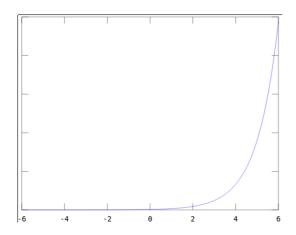
A simple bigram NN LM

- Outputs the probability of next word y(t) given the previous word x(t)
- Input layer maps the previous word as a vector x(t)
- Hidden layer has a linear transform h(t) = Ax(t) + b to compute a representation of linear distributional features

• Output layer maps the values by y(t) = softmax (h(t)) to range (0,1)

that add up to 1

Resembles a bigram Maximum entropy LM



Softmax:

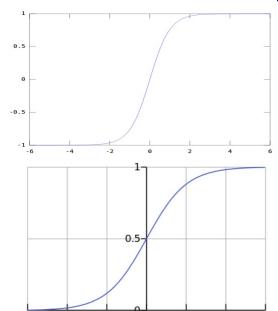
$$\sigma(\mathbf{z})_j = \frac{e^{z_j}}{\sum_{k=1}^K e^{z_k}}$$
 for $j = 1, ..., K$.

 $\begin{array}{c|c} & & & & \\ \hline Ax+b & & & \\ \hline & & & \\ &$

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A non-linear bigram NN LM

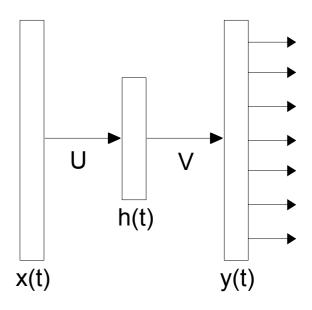
- The only difference to the simple NN LM is that the hidden layer h(t) now includes a non-linear function h(t) = U(Ax(t) + b)
- Can learn more complex feature representations
- Common examples of non-linear functions U:



$$U(t) = tanh(t)$$

Sigmoid

$$\mathsf{U}\left(t
ight) = rac{1}{1+e^{-t}}$$

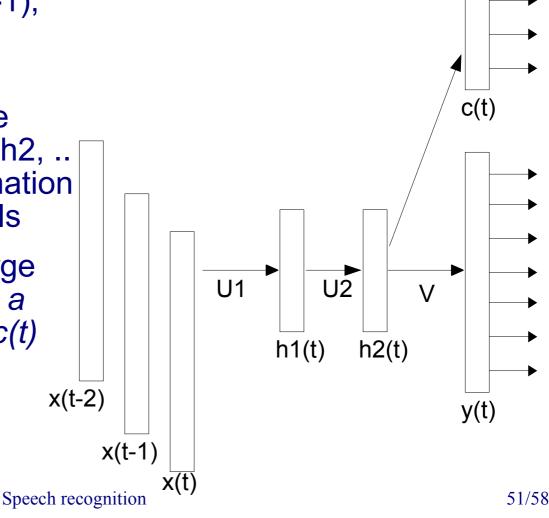


Common NN LM extensions

 Input layer is expanded over several previous words x(t-1), x(t-2), .. to learn richer representations

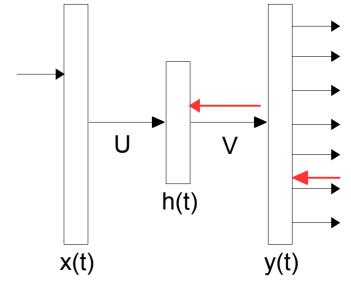
 Deep neural networks have several hidden layers h1, h2, ... to learn to represent information at several hierarchical levels

 Can be scaled to a very large vocabulary by training also a class-based output layer c(t)



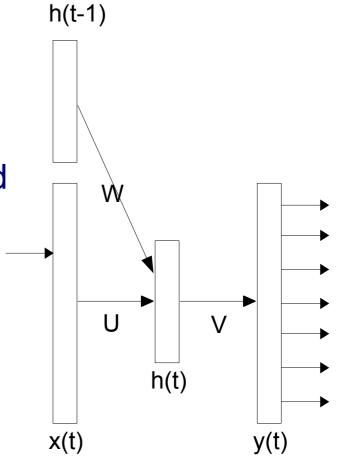
NN LM training

- Supervised training minimizes the output errors by training the weights for V by stochastic gradient descend
- Propagate the output error to hidden layer to train the weights for U
- In practice, a deep NN will require more complex training procedures, since the gradients vanish quickly



Recurrent Neural Network (RNN) LM

- Looks like a bigram NNLM
- But, takes an additional input from the hidden layer of the previous time step
- Hidden layer becomes a compressed representation of the word history
- Can learn to represent unlimited memory, in theory

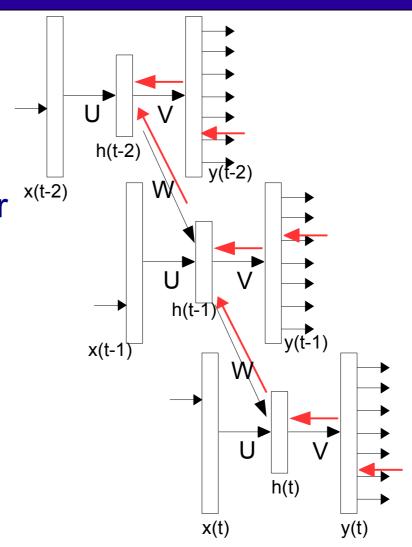


RNN LM training

 Minimizes the output error by training the weights by stochastic gradient descend

 Propagates the output error to all layers and time steps (called backpropagation through time) to train the hidden layer

 Looks now like a very deep neural network with shared weights U and W



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 Onegin concerning the connection of samples in chains. (In Russian.) Bulletin of the
 Imperial Academy of Sciences of St. Petersburg 7(3):153–162.
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 Mikk Computer Speech and Language 120(44):51512547pcessing

Feedback

Go to MyCourses > Lectures > Feedback for Lecture 2 and fill in the form.

Some of the feedback from the previous week:

- + The lecture was clear and at an appropriate pace
- + The small group thing was okey. There was some talking. Not sure if 10 min is required for that
- + Aalto research stuff highlighting concept. First time saw this in any lecture..
- I didn't fully grasp the project work goals and practicalities
- Maybe some video presentation of available techniques would make the lecture even more thrilling
- I think you could end the break out rooms and then announce the break

Thanks for all the valuable feedback!