

ELEC-E8126 Robotic Manipulation Introduction

Ville Kyrki 17.1.2022

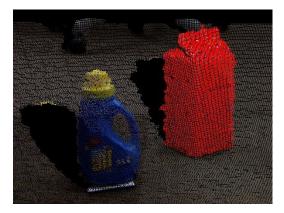


- Course arrangements (see another slide set)
- Quick overview of course contents
- Re-cap of many things

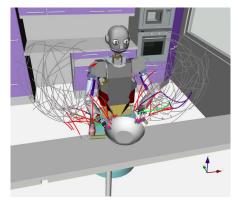


Typical (advanced) manipulation pipeline

Perception



Planning



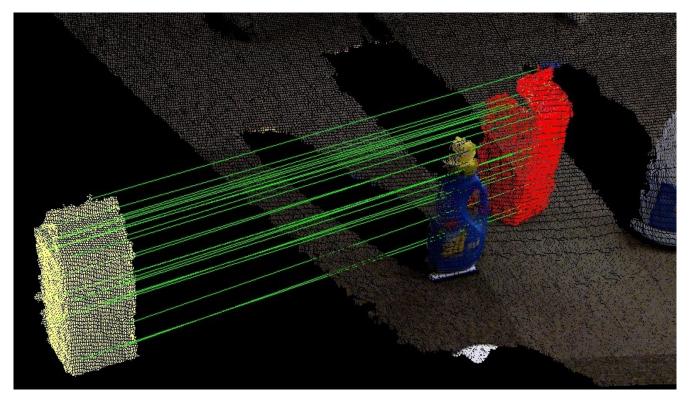
Control / Execution





Perception

• Primarily: Detection of target objects and obstacles





Computer vision course

Planning problems in manipulation

- How a robot can re-arrange objects surrounding it in order to reach a particular goal? E.g. complete an assembly.
 - Mixture of mechanics and planning (synthesis)
- Hierarchy of techniques: (for finding a sequence of actions)
 - Kinematic manipulation: Based on kinematics. E.g. how to move joints to move from a start to end position without collisions.
 Lecture 2.
 - Static manipulation: Based on statics and kinematics. E.g. how to place an object at rest on a table.
 - Quasi-static manipulation: Kinematics, statics, dynamics without inertia. E.g. grasping stably.
 Lectures 7-8.
 - Dynamic manipulation: Kinematics, statics, dynamics. E.g. throwing an object.



Control problems in manipulation

- How to move along a trajectory?
- How to perform several simultaneous tasks?
 Lecture 3
 - E.g. avoid obstacles while moving
- How to perform in-contact motions?
 Lectures 5-6
- How to perform coordinated motions with several Lecture 9
 manipulators?



Towards state-of-the-art

• Modeling and learning manipulation skills

Lecture 4

• State of art learning in manipulation

Lecture 11

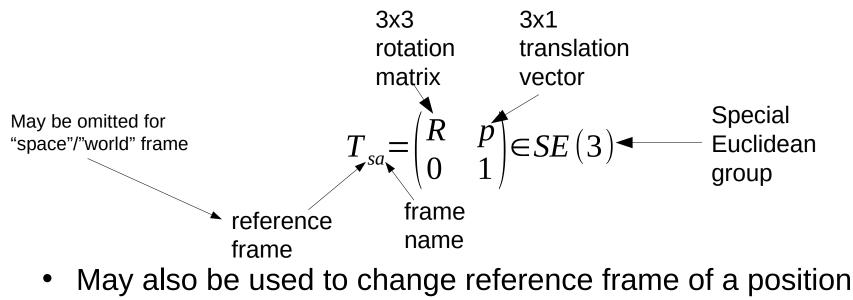




What kind of basic knowledge is needed?

Re-cap: Coordinate frames and transforms

 Coordinate frame {a} can be represented as a 4x4 matrix consisting of translation and rotation



vector or frame.
$$T_{sb} = T_{sa}T_{ab}$$
 $v_b = T_{ba}v_a$

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Electrical

Can this be done for velocity vectors?

Other representations for rotation?

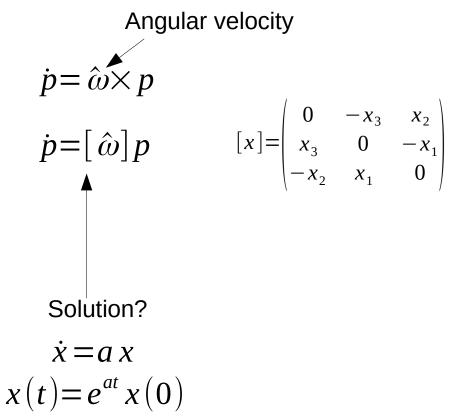
Exponential coordinates for rotation

- Any rotation can be obtained from *I* by rotating it by some θ about axis $\hat{\omega}$ (axis-angle representation)
- Can be combined to $\hat{\omega} \theta \in \mathbb{R}^3$ called exponential coordinates for rotation
- What's the relationship between exponential coordinates and rotation matrix?



Exponential coordinates cont'd

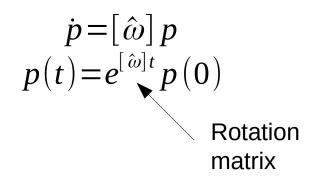
• Velocity of a point in rotation





Exponential coordinates cont'd

• Solution to previous



$$[\hat{\omega}]\theta = [\hat{\omega}\theta] = \log R \qquad R = e^{[\hat{\omega}]\theta}$$

• Rodrigues' formula

$$R(\hat{\omega},\theta) = e^{[\hat{\omega}]\theta} = I + \sin\theta[\hat{\omega}] + (1 - \cos\theta)[\hat{\omega}]^2$$

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Spatial velocity

• Similar to angular velocity, we can define spatial velocity as *twist*

$$V = \begin{pmatrix} \omega \\ v \end{pmatrix} \in \mathbb{R}^6$$
translational velocity

• Let's define skew-operator for twist as

$$[V] = \begin{pmatrix} [\omega] & v \\ 0 & 0 \end{pmatrix} \in se(3)$$

 $Ad_{T_{ab}}$

• Transform between frames

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Adjoint representation of T $[Ad_T]$

 $V_{a} = \begin{pmatrix} R_{ab} & 0\\ [p_{ab}]R_{ab} & R_{ab} \end{pmatrix} V_{b} = \begin{bmatrix} Ad_{T_{ab}} \end{bmatrix} V_{b}$

Exponential coordinates of rigid-body motion

• To define unique twist, let us define *screw axis* S

$$S = \begin{pmatrix} \omega \\ v \end{pmatrix} \in \mathbb{R}^{6}$$

such that $\|\omega\| = 1$ or $\|v\| = 1, \|\omega\| = 0$

• Analogous to rotations, we can then define exponential coordinates for rigid-body motions

$$[S]\theta = \log T \in se(3) \qquad T = e^{[S]\theta} \in SE(3)$$



For formulas, see Lynch&Park

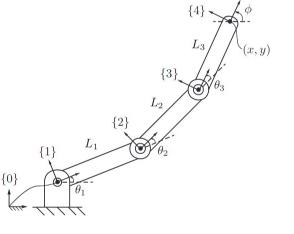
Re-cap: Forward kinematics

- Forward kinamatics is mapping from joint values to end-effector pose
- Forward kinematics of serial chain can be obtained from product of transformation matrices

 $T_{04} = T_{01} T_{12} T_{23} T_{34}$

• Forward kinematics can also be expressed as product of exponentials

$$T(\theta) = e^{[S_1]\theta_1} \cdots e^{[S_N]\theta_N} M$$



End-effector pose at zero position

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space (world) vs body (e-e) frame

Re-cap: Velocity kinematics

- Jacobian: mapping from joint velocities to Cartesian velocities (expressed e.g. as twists) $V=J(\theta)\theta$
- Using screw representation of kinematics, i:th column of Jacobian in space frame is

$$J_{si}(\theta) = [Ad_{e^{[S_1]\theta_1}\cdots e^{[S_{i-1}]\theta_{i-1}}}]S_i$$

- Kinematic singularity: Jacobian is not full rank
 - Can you name examples?



Re-cap: Forward kinematics

- Fwd kinematics
 - Serial chain, product of exponentials
- Jacobian & body-Jacobian
 - Null-space
 - Singularities
- Inverse kinematics
 - Analytical or numerical



Manipulability and force ellipsoids

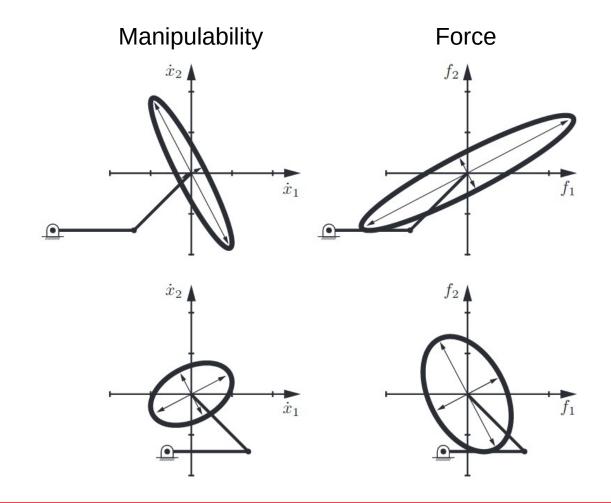
 Manipulability ellipsoid: how easily the robot can move in different directions, corresponds to eigenvalue decomposition of J J^T

PCA

- Force ellipsoid: how easily the robot can produce forces in different directions, corresponds to eigenvalue decomposition of $(J J^T)^{-1}$
- What happens to these at a singularity?



Manipulability and force ellipsoids





For next time

- To complement this lecture, read L&P chapter 5-5.1.4 (also ch. 3 is useful)
- Next time we'll talk about motion planning (ch. 10)



Extra: Series representation of solution of differential equations

