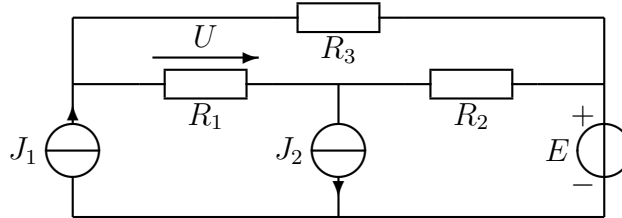


1. Laske jännite  $U$ .

1. Beräkna spänningen  $U$ .

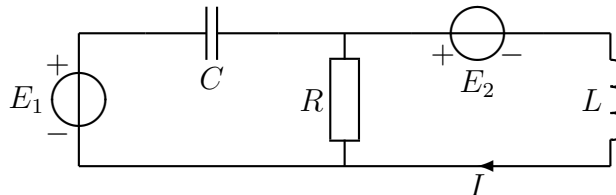
$R_1 = 2 \Omega$ ,  $R_2 = 4 \Omega$ ,  $R_3 = 8 \Omega$ ,  $E = 14 \text{ V}$ ,  $J_1 = 2 \text{ A}$ ,  $J_2 = 3 \text{ A}$ .



2. Laske virta  $I$ .

2. Beräkna strömmen  $I$ .

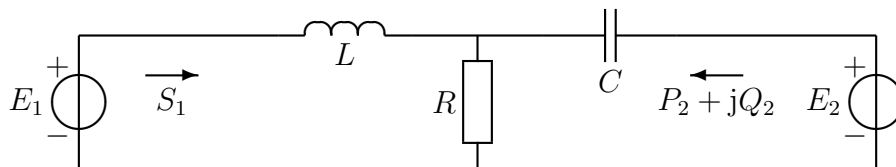
$R = 10 \Omega$ ,  $L = 0,5 \text{ H}$ ,  $C = 0,02 \text{ F}$ ,  $\omega = 10 \frac{\text{rad}}{\text{s}}$ ,  $E_1 = 10 \angle 0^\circ \text{ V}$ ,  $E_2 = 20 \angle 90^\circ \text{ V}$ .



3. Tiedämme, että  $E_1$  luovuttaa kompleksisen tehon  $S_1 = 50 - j50 \text{ VA}$ . Kuinka suuri on  $E_2$ :n luovuttama pätöteho  $P_2$ ?

3. Vi vet, att den komplexa effekten av  $E_1$  är  $S_1 = 50 - j50 \text{ VA}$ . Beräkna den genomsnittliga effekten  $P_2$  som tas från spänningskällan  $E_2$ .

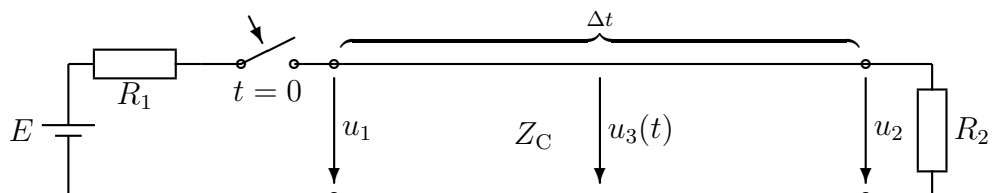
$R = 2 \Omega$ ,  $L = 0,4 \text{ H}$ ,  $C = 0,1 \text{ F}$ ,  $\omega = 5 \frac{\text{rad}}{\text{s}}$ ,  $E_1 = 10 \angle 0^\circ \text{ V}$ ,  $E_2 = ?$



4. Miten kauan kestää, että siirtojohdon keskikohdan jännite  $u_3(t)$  ylittää 98% loppuarvostaan?

4. Hur lång tid tar det för spänningen  $u_3(t)$  i mitten av transmissionslinjen att överstiga 98 % av slutvärdet?

$R_1 = 50 \Omega$ ,  $R_2 = 85 \Omega$ ,  $Z_C = 40 \Omega$ ,  $E = 13,5 \text{ V}$ ,  $\Delta t = 2 \text{ ms}$ .



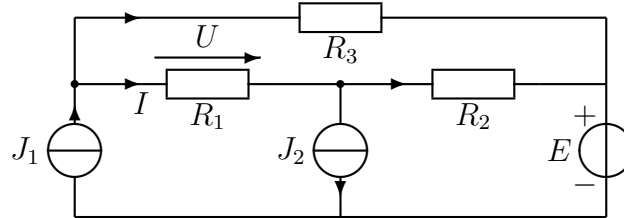
Resultat och svar kan hittas i MyCo.

Ratkaisut ja tulokset tulevat MyCoon.

1. Laske jännite  $U$ .

1. Beräkna spänningen  $U$ .

$R_1 = 2 \Omega$ ,  $R_2 = 4 \Omega$ ,  $R_3 = 8 \Omega$ ,  $E = 14 \text{ V}$ ,  $J_1 = 2 \text{ A}$ ,  $J_2 = 3 \text{ A}$ .



$$J_1 = I + I_{R3} \Rightarrow I_{R3} = J_1 - I \quad (1)$$

$$I = J_2 + I_{R2} \Rightarrow I_{R2} = I - J_2 \quad (2)$$

$$R_3 I_{R3} - R_2 I_{R2} - R_1 I = 0 \quad (3)$$

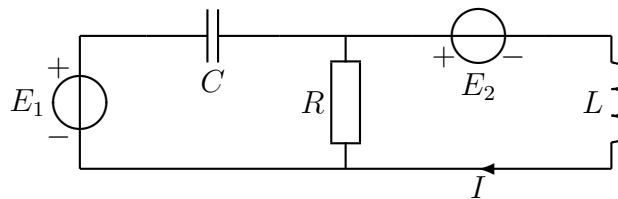
$$R_3(J_1 - I) - R_2(I - J_2) - R_1 I = 0 \Rightarrow I = \frac{R_3 J_1 + R_2 J_2}{R_3 + R_2 + R_1} = 2 \quad (4)$$

$$U = R_1 I = 4 \text{ V} \quad (5)$$

2. Laske virta  $I$ .

2. Beräkna strömmen  $I$ .

$R = 10 \Omega$ ,  $L = 0,5 \text{ H}$ ,  $C = 0,02 \text{ F}$ ,  $\omega = 10 \frac{\text{rad}}{\text{s}}$ ,  $E_1 = 10 \angle 0^\circ \text{ V}$ ,  $E_2 = 20 \angle 90^\circ \text{ V}$ .



$$R(I_1 + I) + E_2 + j\omega LI = 0 \Rightarrow I_1 = \frac{-RI - E_2 - j\omega LI}{R} \quad (6)$$

$$E_1 + R(I_1 + I) + \frac{1}{j\omega C} I_1 = 0 \quad (7)$$

$$\Rightarrow E_1 + RI + \left(R + \frac{1}{j\omega C}\right) \left(\frac{-RI - E_2 - j\omega LI}{R}\right) = 0 \quad (8)$$

$$I = \frac{-E_1 + \left(R + \frac{1}{j\omega C}\right) \left(\frac{E_2}{R}\right)}{R - \left(R + \frac{1}{j\omega C}\right) \left(\frac{R+j\omega L}{R}\right)} = \frac{E_2 - E_1 + \frac{1}{j\omega C} \frac{E_2}{R}}{R - \left(R + \frac{1}{j\omega C}\right) \left(1 + \frac{j\omega L}{R}\right)} \quad (9)$$

$$= \frac{E_2 - E_1 + \frac{1}{j\omega C} \frac{E_2}{R}}{-j\omega L - \frac{1}{j\omega C} \left(1 + \frac{j\omega L}{R}\right)} = \frac{j\omega C(E_2 - E_1) + \frac{E_2}{R}}{\omega^2 LC - \left(1 + \frac{j\omega L}{R}\right)} \quad (10)$$

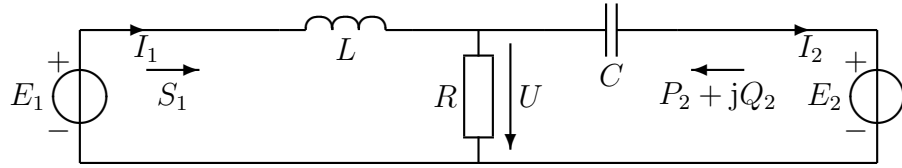
$$= \frac{j0,2(E_2 - E_1)R + E_2}{-j\omega L} = \frac{j0,2(20j - 10)R + 20j}{-j5} \quad (11)$$

$$= -0,2(4j - 2)R - 4 = -8j = 8 \angle -90^\circ \text{ A} \quad (12)$$

3. Tiedämme, että  $E_1$  luovuttaa kompleksisen tehon  $S_1 = 50 - j50$  VA. Kuinka suuri on  $E_2$ :n luovuttama pätöteho  $P_2$ ?

3. Vi vet, att den komplexa effekten av  $E_1$  är  $S_1 = 50 - j50$  VA. Beräkna den genomsnittliga effekten  $P_2$  som tas från spänningskällan  $E_2$ .

$R = 2 \Omega$ ,  $L = 0,4$  H,  $C = 0,1$  F,  $\omega = 5 \frac{\text{rad}}{\text{s}}$ ,  $E_1 = 10 \angle 0^\circ$  V,  $E_2 = ?$ .



$$S_1 = P_1 + jQ_1 = E_1 I_1^* \Rightarrow I_1^* = \frac{S_1}{E_1} = 5 - j5 \Rightarrow I_1 = 5 + j5 \quad (13)$$

$$U = E_1 - j\omega L I_1 = 10 - j2(5 + j5) = 20 - j10 \quad (14)$$

$$P = \frac{|U|^2}{R} = \frac{20^2 + 10^2}{2} = 250 \quad (15)$$

$$P = P_1 + P_2 \Rightarrow P_2 = P - P_1 = 200 \text{ W} \quad (16)$$

Tarkistus

$$I_2 = I_1 - I_R = I_1 - \frac{U}{R} = 5 + j5 - (10 - j5) = -5 + j10 \quad (17)$$

$$E_2 = U - \frac{1}{j\omega C} I_2 = 20 - j10 + j2(-5 + j10) = -j20 \quad (18)$$

$$S_2 = P_2 + jQ_2 = E_2(-I_2)^* = -j20(5 - j10)^* = -j20(5 + j10) = 200 - j100 \text{ VA} \quad (19)$$

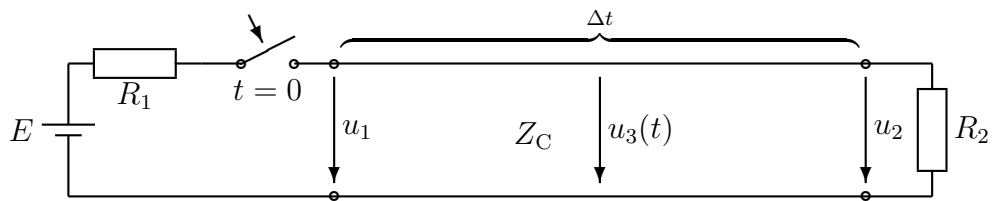
$$j(Q_1 + Q_2) = j\omega L |I_1|^2 + \frac{1}{j\omega C} |I_2|^2 \quad (20)$$

$$Q_1 + Q_2 = -50 - 100 = 2(5^2 + 5^2) - 2(5^2 + 10^2) = -150 \text{ VAR} \quad (21)$$

4. Miten kauan kestää, että johdon keskikohdan jännite  $u_3(t)$  ylittää 98% loppuarvostaan?

4. Hur lång tid tar det för spänningen  $u_3(t)$  i mitten av transmissionslinjen att överstiga 98 % av slutvärdet?

$R_1 = 50 \Omega$ ,  $R_2 = 85 \Omega$ ,  $Z_C = 40 \Omega$ ,  $E = 13.5$  V,  $\Delta t = 2$  ms.



$$u_1(\infty) = u_2(\infty) = u_3(\infty) = \frac{R_2}{R_1 + R_2} E = 8,5 \quad (22)$$

$$u_1(0) = \frac{Z_C}{R_1 + Z_C} \cdot E = 6 \quad (23)$$

$$\rho_2 = \frac{R_2 - Z_C}{R_2 + Z_C} = \frac{9}{25} \quad (24)$$

$$\rho_1 = \frac{R_1 - Z_C}{R_1 + Z_C} = \frac{1}{9} \quad (25)$$

$$u_3(0,5\Delta t) = u_1(0) = 6 \quad (26)$$

$$u_3(1,5\Delta t) = u_1(0) + u_1(0)\rho_2 = 8,16 \quad (27)$$

$$u_3(2,5\Delta t) = u_1(0) + u_1(0)\rho_2 + u_1(0)\rho_2\rho_1 = 8,4 \quad (28)$$

Tämä on 98,8% loppuarvosta. Aikaa kului  $2,5\Delta t = 5$  ms.