

Functional Inorganic Materials Lecture 7: Thermal Conductivity

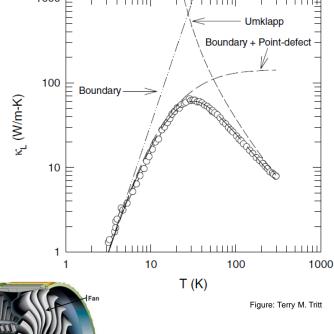
Fall 2022

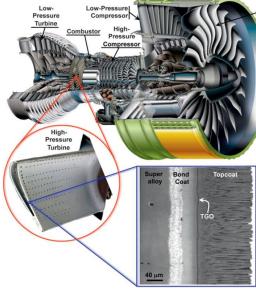
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Lecture Exercise 7 is a MyCourses Quiz

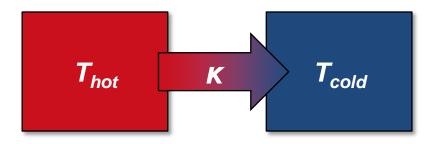
Contents

- Introduction to thermal conductivity
 - Atomic-level mechanisms
 - Electronic thermal conductivity
 - Lattice thermal conductivity
- Materials perspective
 - High thermal conductivity materials
 - Thermal insulators
- Applications
 - Microelectronics
 - Thermal barrier coatings
 - Thermoelectrics (Lecture 8)





Thermal conductivity κ



- Ability of a substance to conduct heat (units: W m⁻¹ K⁻¹)
- Very concrete property in our everyday life
 - Perhaps you've burnt your hand by touching the surface of a *hot metal* (a very good conductor of heat)
 - Perhaps after that, you've worn a thermally insulating glove in your hand
 - During the Finnish winter, it's good to live in a thermally insulated place
- Thermal conductivity is also very important material property for various technological applications:
 - Microelectronics (for example, CPU heat management)
 - Thermal barrier coatings in gas turbines (for example, airplane engines)
 - Thermoelectrics (direct heat-to-electricity conversion)

Warm-up

Do the following materials possess high or low thermal conductivity? Why?



Diamond



Graphite



Polyethylene



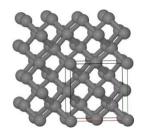
Copper

Figure: AJK

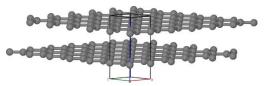


Silica aerogel





κ at 300 K (W m⁻¹ K⁻¹)







~2200 (natural diamond)

Diamond



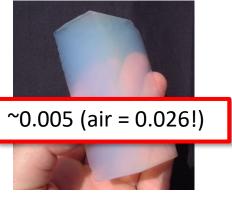
~2000 (in-plane); ~6 (out-of-plane)

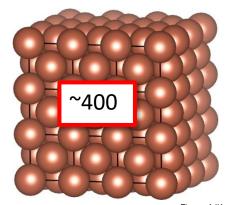
Graphite



Polyethylene







Copper

Figure: AJK

Atomic-level mechanisms behind thermal conductivity

Atomic-level mechanisms behind thermal conductivity

- Metals
 - Heat is primarily carried by conduction electrons
- Insulators
 - Heat is primarily carried by **phonons** (lattice vibrations)
- Semiconductors
 - Low doping levels -> insulator-like behavior
 - High doping levels -> both phononic and electronic thermal conductivity

Insulator – semiconductor – metal classification based on band structure:

Empty bands:

Occupied bands:

Insulator

Semiconductor

Metal

Electronic thermal conductivity

- Heat is carried by conduction electrons
- Electronic thermal conductivity κ_e is directly proportional to the electrical conductivity σ (Wiedemann-Franz law):

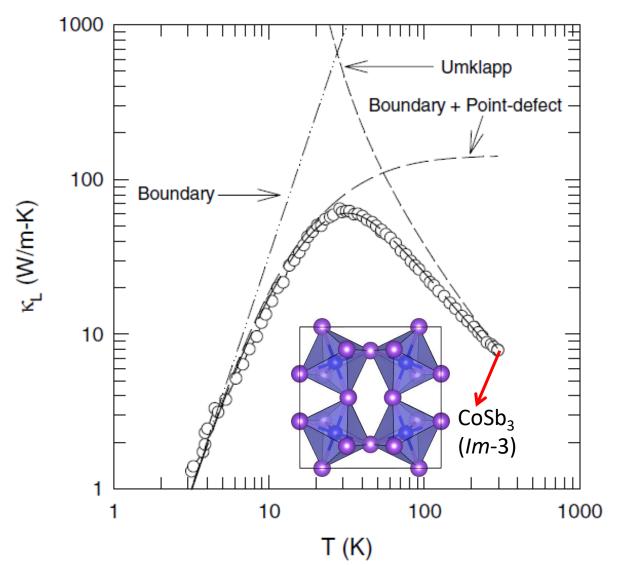
$$\kappa_e = LT\sigma$$
, where $L = 2.44 \times 10^{-8} \text{ W}\Omega\text{K}^{-2}$

- L is roughly constant, but not exactly same for all metals!
- Electrical conductivity
 - increases when T decreases
 - Decreases when T increases (electron-phonon scattering increases)

Metal	Electrical conductivity σ (S/m) at 300 K	Thermal conductivity κ (W m ⁻¹ K ⁻¹)
Ag	6.3×10^7	430
Cu	6.0×10^{7}	400
Al	3.5×10^{7}	235
Zn	1.7×10^7	120
Pb	4.6×10^6	35

Thermal conductivity of an insulator

Thermal conductivity of crystalline materials is usually highly temperature-dependent



Dots = experiment (CoSb₃)

Dashed curves =

Theoretical limits imposed by various **phonon** scattering mechanisms:

- Boundary
- Point-defect / massdefect (isotope)
- Umklapp = phononphonon scattering
- At T > 100, phononphonon scattering dominates (1/T dependence)

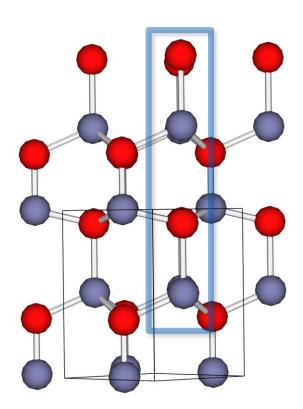
Here we focus on room temperature thermal conductivity

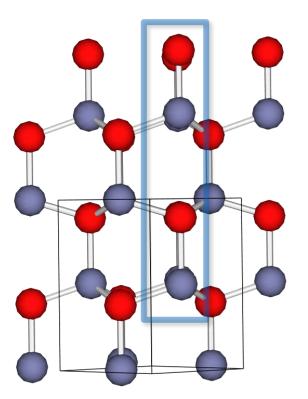
Lattice thermal conductivity

- In insulating solid-state materials, heat and sound is carried by vibrational excitations called *phonons* (from greek $\phi\omega\nu\dot{\eta} = phone = sound$)
- Phonons give rise to *lattice thermal conductivity*, κ_{i}
- Materials have finite thermal conductivity because of various phonon scattering mechanisms (boundary, point-defect, isotope, phonon-phonon, electron-phonon)
- Phonon-phonon scattering is the most important scattering mechanism for crystalline, electrically insulating materials at room temperature
 - Note that crystal with only harmonic phonons (vibrations) would have no phonon–phonon scattering
 - Phonon-phonon scattering arises due to anharmonicity (deviation from harmonic oscillator behavior)
 - Phonon anharmonicity is also the reason for negative thermal expansion (for example, silicon contracts when temperature increases from 18 K to 120 K)

Vibrations in molecules and solids

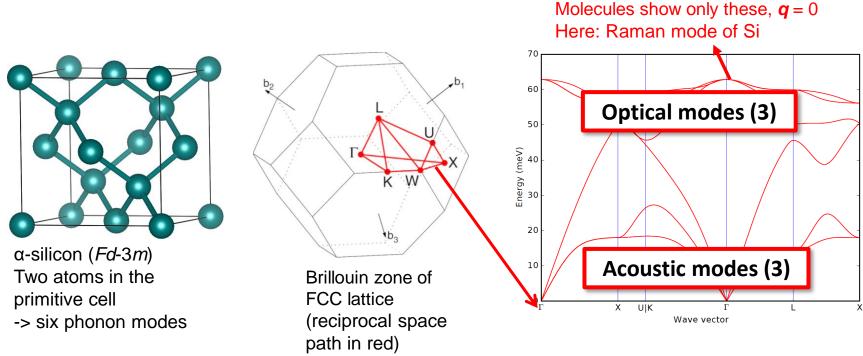
- A molecule with N atoms shows 3N 6 vibrational modes ω_i
- A crystal with *N* atoms in the primitive cell shows 3*N* vibrational modes
 - Atoms in neighboring cells can vibrate in-phase or out-of-phase!
- In-phase and anti-phase Zn–O stretching in ZnO:





Phonon dispersion relations

- The vibrational modes of a solid are described as a function of wavevector q in the reciprocal space: $\omega_i(q) = \mathbf{phonon\ dispersion\ relations}$
 - Phonon dispersion relations account for the periodic nature of the crystal
 - Atoms in neighboring cells can vibrate in a different phase



Phonons vs. electrons

60

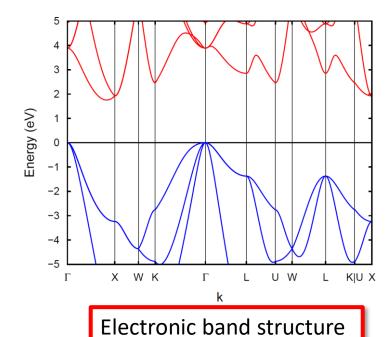
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Energy (meV)

20

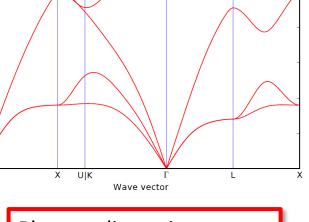
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- Electronic band structures are plotted as a function of wavevector k
 - The crystal orbitals can be in a different phase in neighboring cells
- Phonon dispersion relations are plotted as a function of wavevector q
 - Atoms in neighboring cells can vibrate in a different phase



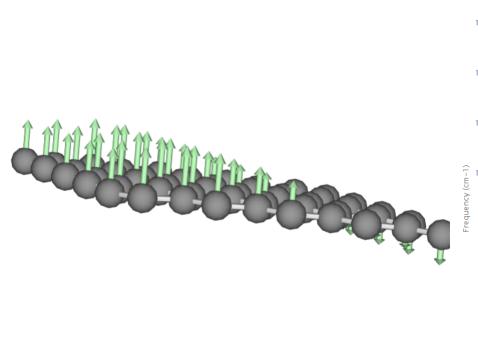
of α-silicon

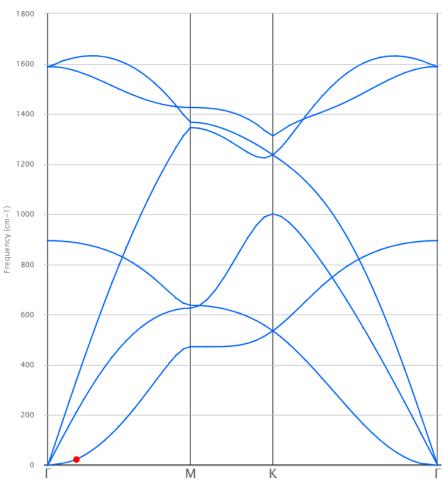
Phonon dispersion relations of α-silicon



Visualization of phonons

- http://henriquemiranda.github.io/phononwebsite/phonon.html
- Let's have a look for example on the acoustic modes of graphene

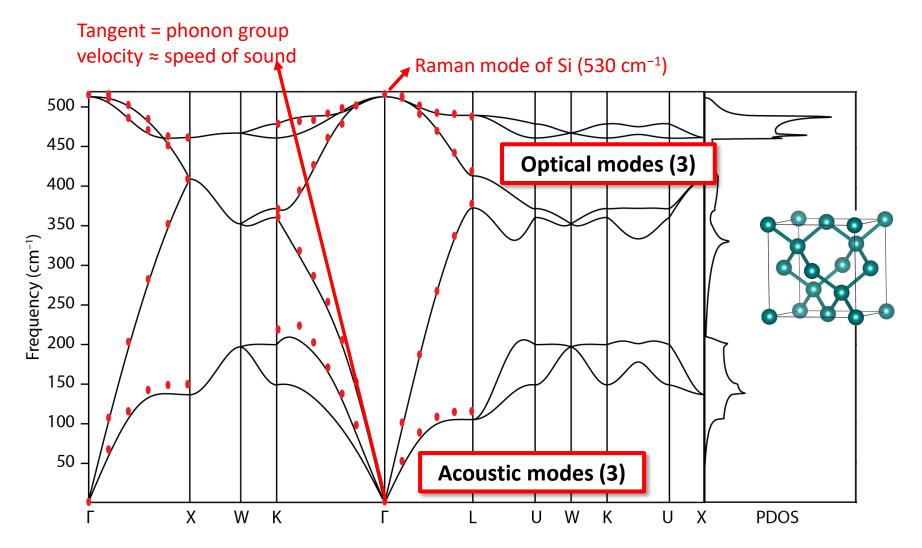






Phonon dispersions for silicon (1)

Red = *Inelastic Neutron Scattering*. Calculated lines: Density Functional Theory.

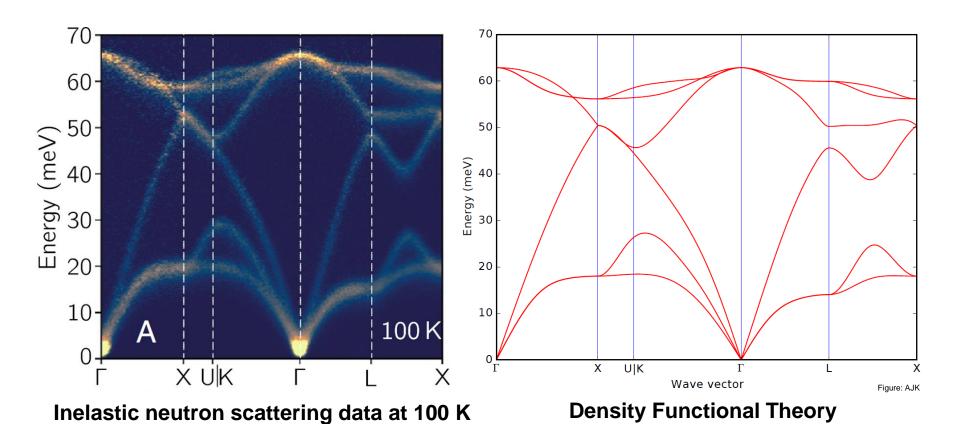


Phonon dispersions for silicon (2)

Experimental data on previous slide were from the 1960s

(Proc. Natl. Acad. Sci. 2018, 115, 1192)

 Excellent agreement also between theory and recent state-of-the-art inelastic neutron scattering data



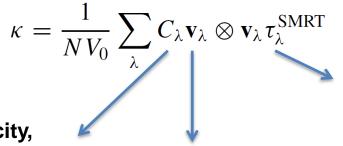
(DFT-PBE0/SVP)

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Lattice thermal conductivities can be explained and predicted computationally with DFT methods

Lattice thermal conductivity κ_L from Boltzmann Transport Equation

- In the past few years, the theoretical methods have evolved to a level, where it is possible to predict the lattice thermal conductivity of non-metallic materials with a good precision (5-10%)
- κ_l can be solved with the help of the semiclassical Boltzmann Transport Equation
- In Single-Mode Relaxation Time approximation:



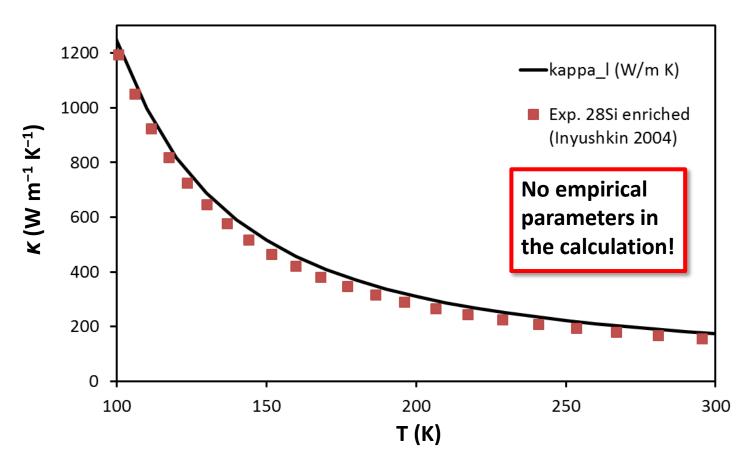
Heat capacity, calculated from phonon dispersions

Phonon group velocity, calculated from phonon dispersions

Phonon relaxation time, calculated from phonon scattering rates (using phonon dispersions and anharmonic force constants)

Lattice thermal conductivity of silicon

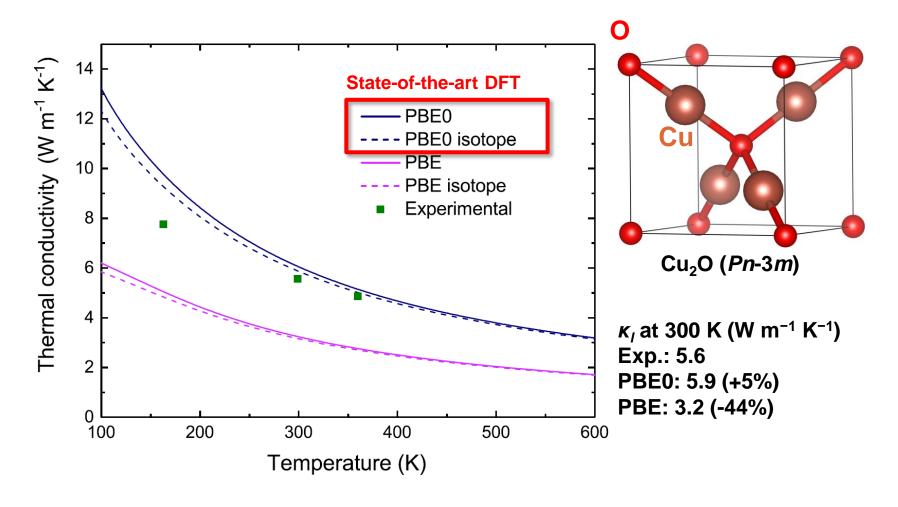
For a simple semiconductor like silicon, κ_l can be predicted with good accuracy using Density Functional Theory (DFT) and semiclassical Boltzmann Transport Equation



Experiment: A. V. Inyushkin et al. Phys. Status Solidi C 2004, 1, 2995–2998.

DFT results: A. J. Karttunen, unpublished results.

Lattice thermal conductivity of Cu₂O



J. Linnera, A. J. Karttunen, *Phys. Rev. B* **2017**, *96*, 014304.

Lattice thermal conductivity of NiO

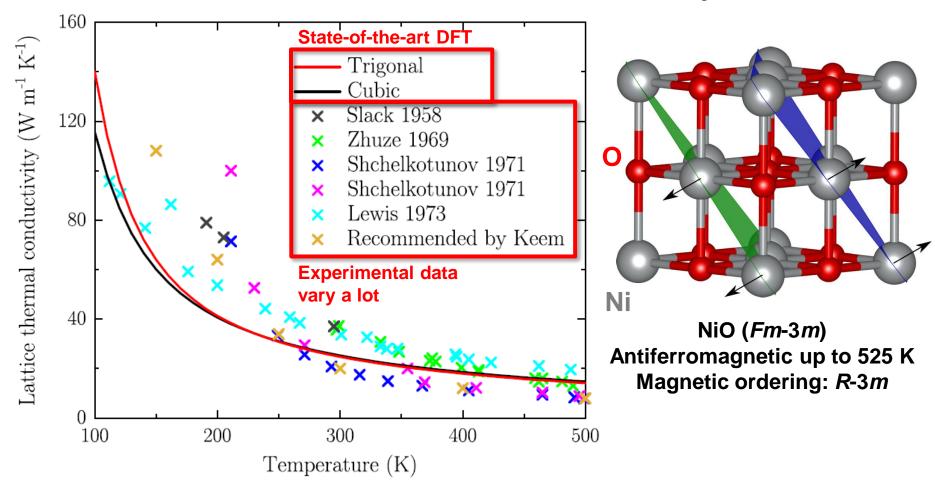


FIG. 4. Lattice thermal conductivity of NiO calculated using both the trigonal (red line) and cubic (black line) primitive cells. Crosses denote the different experimental data points [48–52].

²¹

Thermal engineering of crystalline materials

Thermal engineering

- How to decrease the thermal conductivity of crystalline solid-state materials?
 - In general: add *disorder*
 - Alloying
 - Pure Si: **150** W m⁻¹ K⁻¹; Pure Ge: **60** W m⁻¹ K⁻¹
 - 50:50 Si-Ge alloy: **10** W m⁻¹ K⁻¹
 - Doping: electronic doping also introduces kind of point defects, decreasing lattice thermal conductivity.
 - For example, ZnO: **43** W m⁻¹ K⁻¹; 2% Al doping decreases the thermal conductivity to ~**7** W m⁻¹ K⁻¹
 - Create interfaces that scatter phonons
 - Superlattices
- How to increase thermal conductivity?
 - Prepare samples with high isotopic purity. The effect is large < 100 K, but typically only ~10% at 300 K. There are exceptions like cubic BN (below).
 - Create better materials!
 - Recent prediction from DFT: Ultrahigh Thermal Conductivity of θ-Phase Tantalum Nitride (DOI)

Review on extreme thermal conductivity materials

Nature Materials **2021**, *20*, 1188–1202, https://doi.org/10.1038/s41563-021-00918-3.

Discusses both experimental and computational (DFT) state-of-the-art.

REVIEW ARTICLE

https://doi.org/10.1038/s41563-021-00918-3





Phonon-engineered extreme thermal conductivity materials

Xin Qian [□] ^{1,2}, Jiawei Zhou [□] ^{1,2} and Gang Chen [□] ¹

Materials with ultrahigh or low thermal conductivity are desirable for many technological applications, such as thermal management of electronic and photonic devices, heat exchangers, energy converters and thermal insulation. Recent advances in simulation tools (first principles, the atomistic Green's function and molecular dynamics) and experimental techniques (pump-probe techniques and microfabricated platforms) have led to new insights on phonon transport and scattering in materials and the discovery of new thermal materials, and are enabling the engineering of phonons towards desired thermal properties. We review recent discoveries of both inorganic and organic materials with ultrahigh and low thermal conductivity, highlighting heat-conduction physics, strategies used to change thermal conductivity, and future directions to achieve extreme thermal conductivities in solid-state materials.

Periodic trends for lattice thermal conductivity

- Lattice thermal conductivity depends strongly on the interatomic forces.
- The stronger the interactomic forces, the more strongly the atoms are coupled to each other
 - Strong covalent bonds -> larger phonon velocities
 - Speed of sound in diamond: 12 000 m/s
 - Si: 8500 m/s
 - Pb: 1300 m/s
- Strong covalent bonds show the largest interatomic force constants, resulting in the highest lattice thermal conductivity.
- In simple ionic materials, the interatomic force constants and phonon velocities are typically smaller
 - For NaCl, $\kappa = 6.5 \text{ W m}^{-1} \text{ K}^{-1}$

	Thermal conductivity κ (W m ⁻¹ K ⁻¹)
С	~2200 (diamond)
Si	~150
Ge	~60
Sn	~60 (metal)
Pb	~35 (metal)

Increasing thermal conductivity with isotope enrichment

Science 2020, 367, 555–559, https://doi.org/10.1126/science.aaz6149

Thermal conductivity of cubic BN at 300 K was increased from about 850 m⁻¹ K⁻¹ to over 1600 W m⁻¹ K⁻¹ by isotopic enrichment: ¹⁰BN or ¹¹BN instead of ^{nat}BN.

Proven experimentally, atomic-level mechanism explained with DFT calculations.

REPORT

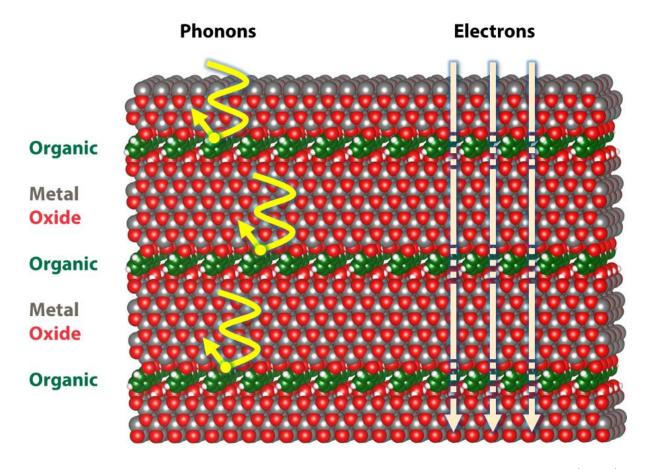
THERMAL CONDUCTIVITY

Ultrahigh thermal conductivity in isotope-enriched cubic boron nitride

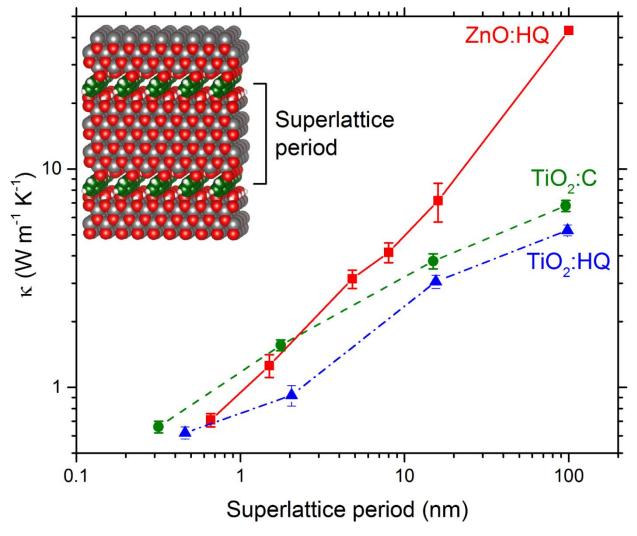
Ke Chen¹*, Bai Song¹*†‡, Navaneetha K. Ravichandran²*, Qiye Zheng³§, Xi Chen⁴¶, Hwijong Lee⁴, Haoran Sun⁵, Sheng Li⁶, Geethal Amila Gamage Udalamatta Gamage⁵, Fei Tian⁵, Zhiwei Ding¹, Qichen Song¹, Akash Rai³, Hanlin Wu⁶, Pawan Koirala⁶, Aaron J. Schmidt¹, Kenji Watanabe⁷, Bing Lv⁶, Zhifeng Ren⁵, Li Shi^{4,8}, David G. Cahill³, Takashi Taniguchi⁷, David Broido²†, Gang Chen¹†

Decreasing thermal conductivity with oxide-organic superlattices (1)

- ZnO:organic superlattices fabricated by ALD/MLD
- Create phonon-blocking interfaces (that would not scatter electrons too much)



Decreasing thermal conductivity with oxide-organic superlattices (2)



Crystalline vs. amorphous

- So far, we have mainly discussed crystalline materials
- For amorphous, non-crystalline materials, phonons are not well-defined
- Generally, they possess low thermal conductivity (e.g. acrylic glass 0.2 W m⁻¹ K⁻¹)

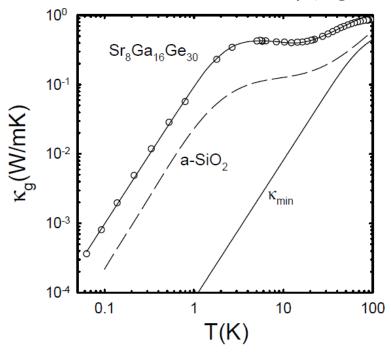


FIG. 2. Lattice thermal conductivity measured from 60 mK to 100 K for $Sr_8Ga_{16}Ge_{30}$ with a fit (solid curve) to the model discussed in the text (see also Fig. 3). The dashed line is for a-SiO₂, and the solid curve labeled κ_{min} is the calculated minimum thermal conductivity of Ge.

25 January 1999

Thermal insulator application: Thermal barrier coatings for gasturbine engines

Thermal barrier coatings for gasturbine engines

MRS BULLETIN • VOLUME 37 • OCTOBER 2012 • www.mrs.org/bulletin 891

Introduction

Thermal-barrier coatings (TBCs) are refractory-oxide ceramic coatings applied to the surfaces of metallic parts in the hottest part of gas-turbine engines (Figures 1 and 2), enabling modern engines to operate at significantly higher gas temperatures than their predecessors (see recent reviews¹⁻⁶). Gas-turbine engines, used to propel aircraft and to generate electricity, are Carnot engines where their efficiency and core power are directly related to the gas temperature entering the turbine section.^{7,8} Further increases in the energy efficiency of gasturbine engines, both to increase the electricity output and, for jet engines, the thrust-to-weight ratio and durability, will rely on further improvements in TBCs. At the same time, as gas temperatures are increased in the pursuit of higher engine efficiency, there are new challenges to existing TBCs.

To place this in context, gas-turbine engines are a \$42 billion industry worldwide (2010), with ~65% of the sales accounting for jet engines and the remainder land-based engines for electricity generation.9 The latter, fueled by natural gas or liquid A refractory material retains its strength at high temperatures

Low-Pressure Low-Pressure Compressor Turbine High-Combustor Pressure Compressor High-Pressure Turbine Super Bond Topcoat allov Coat TGO TBC 40 um

Figure 1. Cutaway view of Engine Alliance GP7200 aircraft engine, photograph of a turbine blade (~10 cm long) with thermal-barrier coating (TBC) from the high-pressure hot section of an engine, and a scanning electron microscope (SEM) image of a cross-section of an electron beam physical vapor deposited 7 wt% yttria-stabilized zirconia TBC. (Engine image courtesy of Engine Alliance, turbine blade photograph courtesy of YXLON, and the SEM micrograph is from Reference 44.) TGO, thermally grown oxide.

Thermal barrier coatings

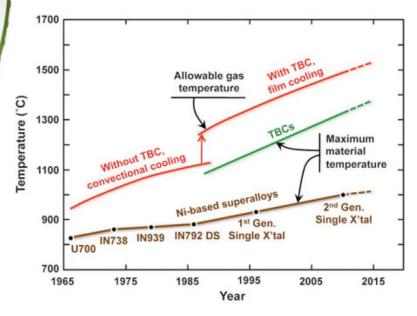


Figure 3. Progression of temperature capabilities of Ni-based superalloys and thermal-barrier coating (TBC) materials over the past 50 years. The red lines indicate progression of maximum allowable gas temperatures in engines, with the large increase gained from employing TBCs. Based on a diagram from the late Professor Tony Evans.

Yttria-stabilized Zirconia (YSZ)

• Zirconia, ZrO_2 , is potentially a very useful ceramic material with a high melting point of ~2700 °C but on cooling it undergoes a series of phase transitions:

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cubic (fluorite) \xrightarrow{2400\,^{\circ}\text{C}} tetragonal \xrightarrow{1050\,^{\circ}\text{C}} monoclinic (baddeleyite)
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- The tetragonal to monoclinic transition is associated with an increase in unit cell volume by \sim 9% -> ceramic bodies fabricated at high T shatter on cooling
- The transitions can be avoided by creating a solid solution ZrO₂-Y₂O₃

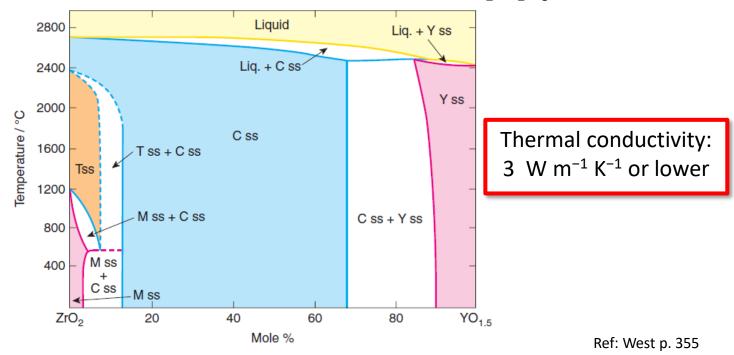


Figure 7.28 ZrO_2 – Y_2O_3 phase diagram. M, T and C refer to the monoclinic, tetragonal and cubic polymorphs of zirconia, and their solid solutions, ss. Y = yttria, Y_2O_3 .