

Solution of homework 2

- a. Draw the sketch of the 3-phases circuit and its corresponding single-phase equivalent circuit

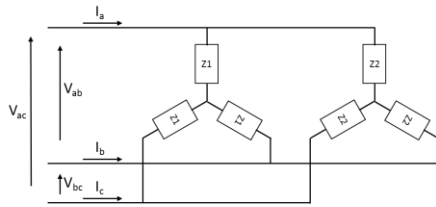


Fig 1: two parallel connected 3-phase loads. Both loads are wye-connected. In the exercise there is no mention of the source connection, but in 3-phases systems the voltage is always the line-to-line voltage, unless otherwise mentioned.

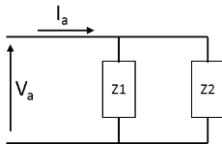


Fig 2: Single-phase equivalent circuit $V_a = \frac{V_{ab}}{\sqrt{3}}$

- b. Calculate the source line current

$$I_a = I_{z1} + I_{z2}, \text{ where } \begin{array}{l} I_{z1} = 20 \angle \arccos(0,9) \\ \quad = 20 \angle 25,84^\circ \end{array} \quad \begin{array}{l} I_{z2} = 30 \angle -\arccos(0,8) \\ \quad = 30 \angle -36,87^\circ \end{array}, \text{ i.e.,}$$

$$\begin{aligned} I_a &= 20 \angle 25,84^\circ + 30 \angle -36,87^\circ \\ &= 43,014 \angle -12,46^\circ \text{ A} \end{aligned}$$

the rms value of the line current is 43,01 A

- c. Calculate the power factor of the whole load

From the above we can see that the angle of the current is $-12,46^\circ$. The power factor is thus: $\cos(-12,46) = 0,976$. The minus sign means that the whole load is inductive (lagging current).