Density-Functional Theory for Practitioners

Metallic Bonding

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Atomistic Computer Simulations – A Practical Guide
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Bonding

Atoms are quantum mechanical objects with both the nucleus and the electrons properly described by the laws of quantum mechanics. However, when considering the interactions between atoms in molecules and solids, the nucleus can, to a very good approximation, be treated classically: it serves as a source of electrostatic potential. The interaction of electrons, however, remains entirely quantum mechanical. In this chapter, we consider the behavior of electrons and how they are responsible both for the properties of atoms and for the interactions between atoms which make the world so interesting. The interaction between atoms is generally known as bonding.

There are many different types of bonds, and the structure of molecules and solids is linked strongly to the bonding. We have seen that some bonds are strongly directional, which are responsible for the structures of molecules such as water and methane. Other bonds are nondirectional, and the structure of materials with these bonds is determined by other factors that increase the stability of the system, for example, by maximizing the number of neighbors. The strength of bonds also varies, and goes some way towards determining the strength of materials, though other factors such as microstructure can be important.

This chapter focuses on the electrons and their role in atomic structure, and many atomistic simulations will include the electrons explicitly. However, it is perfectly possible to consider the electrons implicitly and to parameterize the interactions between atoms, replacing the bonds with numerical functions. At the simplest level, these act very much like springs. For instance, forcefields such as CHARMM, Amber and GROMACS are widely used within biochemistry, while empirical potentials have a long history within physics. However, these methods still need data for fitting the potentials, which often comes from electronic structure calculations; understanding electronic interactions is therefore extremely important.

Electronic Ground State

The starting point for all simulations must be the lowest energy or ground state: any understanding of the properties of a system must build from the most stable configuration. Any system which is not in its lowest energy state will be liable to fall into that state as it evolves. The response of a system to excitation is an important means of characterization, but we must start from a thorough understanding of the ground state.

In most circumstances, the behavior of a set of atoms, and hence of many forms of matter including molecules and solids, can be modelled by assuming that the electrons arrange themselves in their lowest energy state for a given set of atomic positions; in other words, we can place the electrons in their ground state for every set of atomic positions. This approximation is known as the Born-Oppenheimer approximation. Naturally, there are occasions when this is not applicable: to take a simple example, consider a flame, which is a complex system involving

heat, chemical reactions, electronic excitations and de-excitations with emission of light, and many other processes. The question of excitations is too complex for a detailed treatment in a textbook of this nature.

As we have seen, the electronic structure of atoms is an important starting point in understanding the interactions between atoms. The structure of the periodic table of the elements reflects the distribution of electrons in atoms, and this distribution of electrons determines the bonding properties of atoms. The outermost electrons, known as valence electrons, are most strongly involved in determining how atoms interact, whatever the bonding mechanism.

The electronic ground state can be calculated using density-functional theory, for example. The interaction between atoms will disturb the atomic electronic configurations, leading to new distributions of electrons: bonds. Chemistry textbooks define a number of different types of bonds which are useful in understanding the behavior of matter; it is important to note, however, that the real world rarely fits well within any particular picture, and bonds tend to have a mixture of characters.

Metallic Bonding

Bonding in metals is more difficult to picture in simple terms than the previous bonding types. It involves the valence electrons becoming relatively delocalized and behaving like an electron gas. They then are only influenced by the electrostatic potential of the ionic cores. The electrons can be thought of as being shared between all the atoms in the solid rather than any particular pair of atoms. Metallic bonds are much weaker than the previous bonds we have described, though in metals, there are typically many more neighbors, so that the total strength of binding can be com- parable. Metallic bonds are largely nondirectional. It is important to note that the metals we encounter in everyday life gain their strength from the microstructure rather than atomic structure. This is demonstrated by phenomena such as work hardening, where repeated hammering as traditionally employed by a blacksmith strengthens metal by creating dislocations which interact to give strength.

Simple metals, for example, Na or Al, are often described in terms of a nearly-free electron (NFE) metal, where the electronic structure is very close to the free electron gas. Transition metals are rather different, and can be described simply in terms of a rectangular band whose bonding is determined by the filling of the band. Figure 1 shows a cross-section through a simple metal, Na. There are two electrons in the unit cell, which has a volume of 73.41 Å^3: the average electron density if the charge density was uniform would be 0.0272 electrons/Å^3. Note how the charge density is very uniform, and is actually very close to the average charge density, confirming the simple picture of metallic bonding. There is increased electronic charge density between the ions, but the increase is only a small percentage.
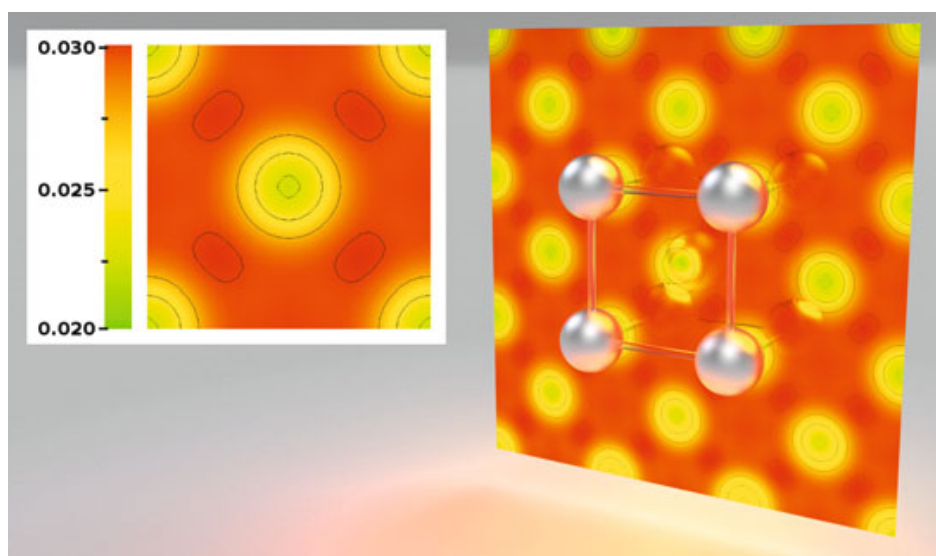
Figure 1: Charge density for a simple metal, sodium. The density is plotted in a plane that lies between planes of Na ions, so that no ion crosses the plane, as seen in the three-dimensional plot to the right. The contours are plotted at densities of 0.0225, 0.0250, 0.0275 and 0.0300 electrons/Å^3.

Bond breaking and making

Having reviewed the types of bonds found, we must turn to the important question of the formation and breaking of bonds. These processes are key to any dynamical process on the atomic scale, such as chemical reactions, or in determining diffusion barriers.

A typical covalent bond will have an energy of several electron volts, with ionic bonds similarly strong. Metallic bonding is weaker, but the close packed nature of most metals compensates for this, as each atom will have many neighbors, so the total bonding energy in a metal can be high. A typical hydrogen bond is a few tenths of an electron volt, while dispersion bonding is weaker.

It should be clear from these energy scales that the formation of a bond will stabilize a structure considerably. The presence of a covalent bond can compensate for significant amounts of strain: some surprising organic molecules such as cubane, which features carbon atoms with 90° bonds, are excellent examples of this. The strength of bonds provides most of the driving force behind the structures of the materials observed in the world around us.

The breaking of a bond, as is evident from the energies just mentioned, will require input of energy to the system. There are ways to reduce the energy required to break a bond, often found in active sites of enzymes or industrial catalysts. The interaction of molecules with the active site or the industrial catalyst reduces the barrier. The detailed energy profile of a reaction will determine whether more enthalpy is released by breaking a bond than is needed to break it: this

is an exothermic reaction. The storage of chemical energy in bonds forms the basis for many biochemical processes, notably the storage and release of energy in adenosine triphosphate, ATP. The opposite of exothermic reactions are endothermic, and require more energy input than is released.

Bonds are formed between atoms when they move close enough for electron clouds to start interacting, or when electrostatic interactions are stronger than thermal energy. In both cases, it is important to realize that atoms are mobile, except at extremely low temperatures which are only reached in experiments or under certain astrophysical conditions: the study of small molecules in space is an important area. Bonds can be broken by stretching due to thermal motion or some larger motion of the system. Electron injection into an antibonding orbital will weaken a bond, and can also lead to bond breaking.