## Value tree



## Independence checking

Check, e.g., whether DM agrees with following types of statements:

- (5500,8,excellent)>(3500,8,excellent) $\rightarrow$ (5500,2,poor)>(3500,2,poor)
- (5500,8,excellent)>(5500,2,excellent) $\rightarrow(3500,8$, poor $)>(3500,2$, poor $)$
- (5500,8,excellent)>(5500,8,poor) $\rightarrow$ (3500,2,excellent)>(3500,2,poor)
- (5500,2,excellent) $)(3500,8$, excellent $) \rightarrow(5500,2$, poor $)>(3500,8$, poor $)$

Mutual pref. Independence

- (5500,8,poor)>(3500,8,excellent) $\rightarrow$ (5500,2,poor)>(3500,2,excellent)
- $(5500,8$, poor $)>(5500,2$, excellent $) \rightarrow(3500,8$, poor $)>(3500,2$, excellent $)$
- (5500,8,excellent $) \leftarrow(3500,8$, excellent $) \sim d(5500,2$, poor $) \leftarrow(3500,2$, poor $)$

Difference

- $\quad(5500,8$, excellent $) \leftarrow(5500,2$, excellent $) \sim d(3500,8$, poor $) \leftarrow(3500,2$, poor $) \succ$ independence
- $(5500,8$, excellent $) \leftarrow(5500,8$, poor $) \sim d(3500,2$, excellent $) \sim(3500,2$, poor $)$


## Attribute specific value functions



| Salary <br> ( $€$ /month) | Bisection <br> method <br> checkpoints |
| :---: | :---: |
| 3500 | $\mathrm{x0}$ |
| 3800 | x 0.25 |
| 4200 | x 0.5 |
| 4800 | x 0.75 |
| 5500 | $\mathrm{X}^{*}$ |


| Vacation <br> (weeks/year) | Bisection <br> method <br> checkpoints |
| :---: | :---: |
| 2 | $\mathrm{X0}$ |
| 3 | x 0.25 |
| 4 | x 0.5 |
| 6 | x 0.75 |
| 8 | $\mathrm{X}^{*}$ |



| Fit with <br> interests | Value by <br> direct rating |
| :---: | :---: |
| poor | 0 |
| fair | 0.333333 |
| good | 0.666667 |
| excellent | 1 |

## Attribute weights + attribute levels and values of alternatives

- Suppose DM has stated that
$(3500,8$, poor $) \leftarrow(3500,2$, poor $) \sim(3500,2$, fair $) \leftarrow(3500,2, \text { poor })^{\sim}$ (5500,2, poor) $\leftarrow(3500,2$, poor $)$
- This implies $\mathrm{w} 2=\mathrm{w} 3 / 3=\mathrm{w} 1 \rightarrow \mathrm{w} 1=0.2, \mathrm{w} 2=0.2, \mathrm{w} 3=0.6$

|  |  | attr. Levels xi | Finance | Consultancy | Industry | Academia |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Salary | 4300 | 4600 | 4800 | 4000 |
|  |  | Vacation | 5 | 5 | 5 | 6 |
|  |  | Fit with interests | fair | good | good | excellent |
| weights | attr. Spec. Values vi(xi) | Finance | Consultancy | Industry | Academia |  |
| w1 | 0.2 | Salary | 0.541667 | 0.666667 | 0.75 | 0.375 |
| w2 | 0.2 | Vacation | 0.625 | 0.625 | 0.625 | 0.75 |
| w3 | 0.6 | Fit with interests | 0.333333 | 0.666667 | 0.666667 | 1 |
|  |  |  |  |  |  |  |
|  |  | overall values <br> $\mathbf{V ( x ) = w 1 * v 1 ( x 1 ) + ~}$ <br> w2*2(x2)+w3*v3(x3) | 0.433333 | 0.658333 | 0.675 | 0.825 |

