# CHEM-E4115 Computational Chemistry I (5op) 2nd part: molecular modelling

Book Chapters 4.1-4.7
Empirical Force Field Models:
Molecular Mechanics

### Revision: From quantum mechanics to molecular mechanics

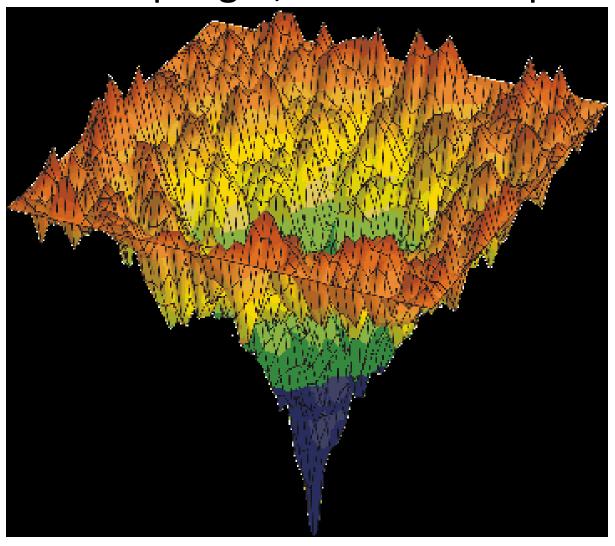
Quantum mechanics: Schrödinger's equation

$$i\hbar \frac{\partial}{\partial t} \psi = \hat{H} \psi$$
 Time-dependent Schrödinger equation (general)

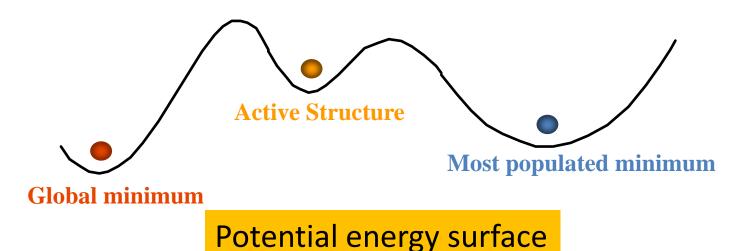
- Born-Oppenheimer approximation:
  - Electrons and nuclei motion treated separately
  - Consequently energy of a molecule in ground (electronic) state can be considered as a function of the nuclear coordinates only
  - If one or several of the nuclei move, this energy changes



This lecture: Potential energy surface, and basics of sampling it; measurable quantities

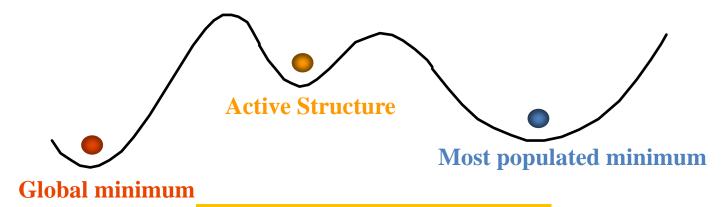


### Molecular modelling and simulations



- Interested in
  - Global minimum molecular conformation / system configuration
  - Active structures
  - Relative populations
  - Transitions and transition pathways between the states

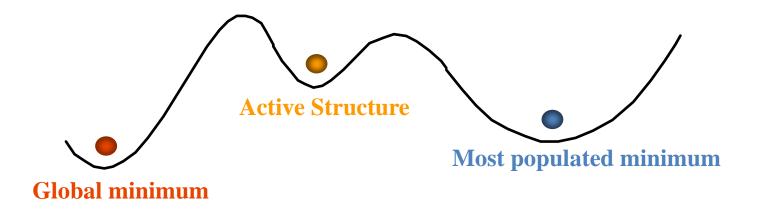
### Molecular modelling and simulations: How to resolve?



Potential energy surface

- Typical methodology
  - Minimum energy configuration determination (no dynamics, just potential energy surface)
  - Molecular dynamics (deterministic dynamic sampling of the potential energy surface)
  - Monte Carlo (stochastic sampling of the potential energy surface)

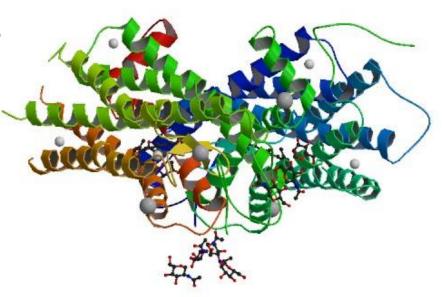
### Energy minimization vs simulations



- Energy minimization generates individual minimum energy configurations
- Assuming all minima could be defined, a statistical mechanics partition function would describe the system
  - Possible only for small molecules, small isolated clusters in vacuum (gas)
  - Not feasible for complex systems
- For complex (practically all) systems, computer simulations can be used to probe the potential energy surface

### Applications of energy minimization

- Structure optimization
  - Docking studies, structure analysis
  - X-ray structure molecular optimization
- Pre-step before molecular dynamics or Monte Carlo simulations
  - Structural relaxation

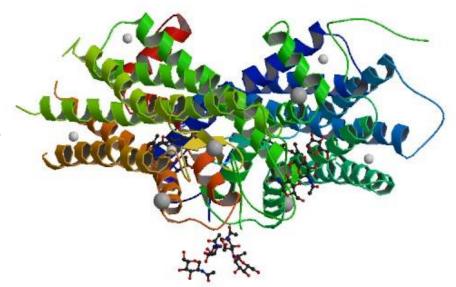


Rhodopsin, PDB entry 1f88

The molecule in the eye that senses light. Composed of a small light-sensitive molecule of retinal, bound inside the protein opsin

### Applications of energy minimization

- Normal mode analysis
  - Hessian matrix (=the second-order partial derivatives) provides a force-constant matrix for vibrations in a system
  - Eigenvalues relate to vibrations frequencies
- Transition structures and reaction pathways (saddle points)



Rhodopsin, PDB entry 1f88

The molecule in the eye that senses light. Composed of a small light-sensitive molecule of retinal, bound inside the protein opsin

## From molecular conformations to measurable averages

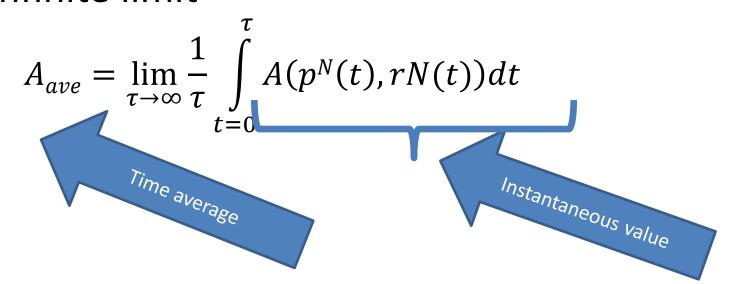
- We have: Potential energy surface
- We need: A measurable quantity

 Now: how do we obtain the measurable quantity from the potential energy surface

(force-field)

### Time averages, ensemble averages

- Determining experimentally measurable properties of a molecular system requires relating instantaneous values to average measurable value
- At infinite limit



### Time averages, ensemble averages

At infinite time limit, time average A<sub>ave</sub>

$$A_{ave} = \lim_{\tau \to \infty} \frac{1}{\tau} \int_{t=0}^{\tau} A(\boldsymbol{p}^{N}(t), \boldsymbol{r}^{N}(t)) dt$$

- Calculating this an issue with any real system ( $10^{23}$  atoms)
- Large number of replications: Ensemble average

$$< A_{ave} > = \int \int d\mathbf{p}^{N} d\mathbf{r}^{N} A(\mathbf{p}^{N}, \mathbf{r}^{N}) \rho(\mathbf{p}^{N}, \mathbf{r}^{N})$$

$$\stackrel{E_{nsemble}}{=} a_{verage}$$

$$\stackrel{Replica}{=} v_{alue}$$

### Ergodic hypothesis

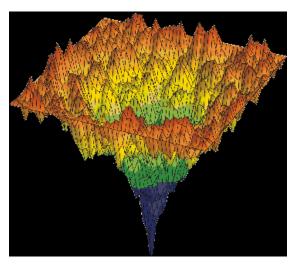
$$A_{ave} = \lim_{\tau \to \infty} \frac{1}{\tau} \int_{t=0}^{\tau} A(\boldsymbol{p}^{N}(t), \boldsymbol{r}^{N}(t)) dt$$

$$\langle A \rangle = \int \int d\mathbf{p}^N d\mathbf{r}^N A(\mathbf{p}^N, \mathbf{r}^N) \rho(\mathbf{p}^N, \mathbf{r}^N)$$

### Time average and ensemble average are equal

Key to obtaining "measurable" quantity from molecular simulation

- Model of real system: Potential energy surface
- Measurable quantity
  - ensemble average over a finite size ensemble
  - time average over a finite time

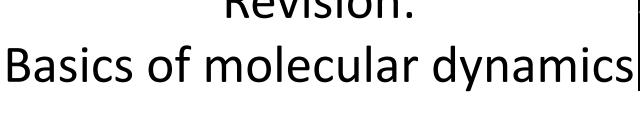


## Now to molecular dynamics Static vs dynamics





#### Revision:



 Potential energy functional E (function of nuclei positions) -> Force on each nuclei

$$\vec{F}$$
=- $\nabla E$ 

$$\vec{F}$$
= $m\vec{a}$ = $m\frac{d\vec{v}}{dt}$ = $m\frac{d^2\vec{r}}{dt^2}$ 

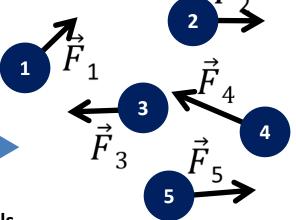
 $t_0$   $t_0$ + $\delta t$   $t_0$ + $2\delta t$  ...

time

Force for each particle calculated at discrete time intervals
Particle positions updated assuming particle moves with
this force (acceleration) in the direction of force for
the entire (short) time interval

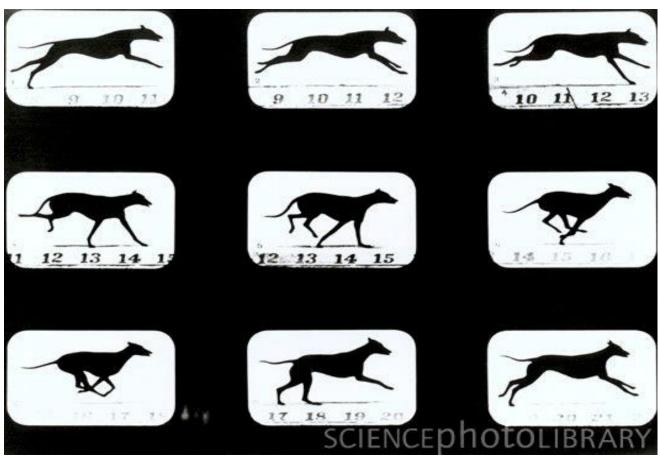
New forces calculated with updated positions

loop-as-long-as-wanted (typically as long as possible)



## Molecular dynamics in brief: sequence of static images





### Molecular dynamics

$$\vec{F} = -\nabla E$$

$$\vec{F} = m\vec{a}$$

$$time$$

$$t_0 \quad t_0 + \delta t \quad t_0 + 2\delta t \quad \dots$$

- Any state of the system in future can be predicted from the state right now
  - Deterministic
- Any state in the past can be predicted by reversing time in the algorithm
  - Numerical accuracy provides a limit

### Molecular dynamics

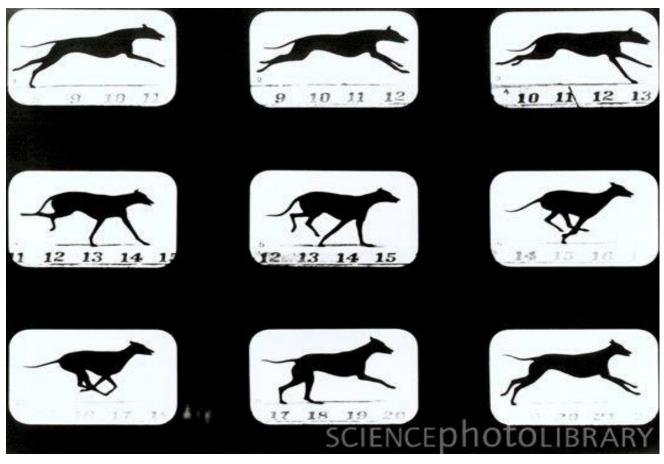
- Thermodynamic quantities, conformation properties as average corresponding to the configurations that have been present
- M number of time steps

$$A_{ave} = \lim_{\tau \to \infty} \frac{1}{\tau} \int_{t=0}^{\tau} A(\boldsymbol{p}^{N}(t), \boldsymbol{r}^{N}(t)) dt$$

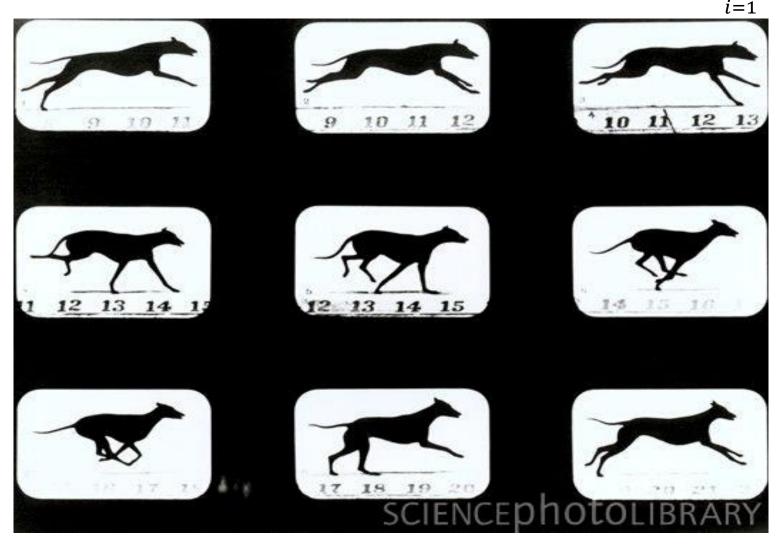
$$< A > = \frac{1}{M} \sum_{i=1}^{M} A(\boldsymbol{r}^{N})$$

## Molecular dynamics in brief: sequence of static images $\langle A \rangle = \frac{1}{M} \sum_{i=1}^{M} A(\mathbf{r}^N)$



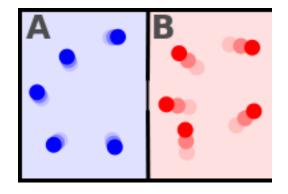


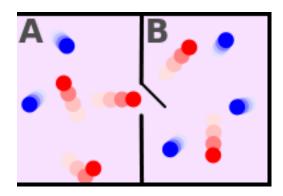
# Note: Average may not be representative $\langle A \rangle = \frac{1}{M} \sum_{i=1}^{M} A(\mathbf{r}^{N})$



#### Statistical mechanics ensembles

- Microcanonical ensemble NVE
- Canonical ensemble NVT
- Isothermal-isobaric ensemble NTP
- Grand canonical ensemble  $\mu$  VT



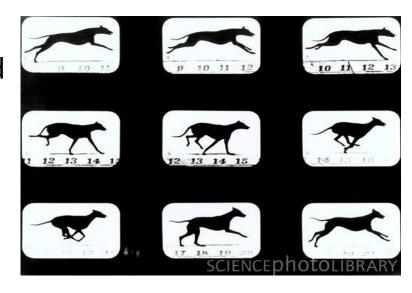


### Microcanonical ensemble (NVE) is the natural ensemble of molecular dynamics

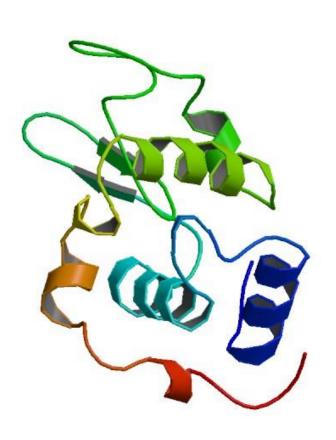
- Number of atoms (N), box volume (V), and energy (E) are conserved
  - NVE, microcanonical ensemble
- Equations of motions satisfy naturally energy conservation
- Energy conservation can be used as an inherent check on the implementation
- Free from coupling the microscopic system to macroscopic variables (NVT and NPT do this)
- In the exercise also NVT and NPT via algorithm modification (more about this later)

### At the end of this lecture, you should know

- Connection of potential energy surface and force-field in molecular modelling
  - One defines the other
- Obtaining a measurable quantity that is based on the potential energy surface:
  - Time average and ensemble average
- Concept of molecular dynamics: sequence of coordinate and velocity snapshots

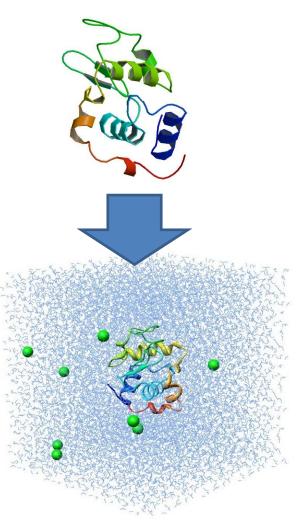


#### Content of the 1<sup>st</sup> exercise



- How to find crystal structures of proteins
- Setting up and run a molecular modelling simulation of a small protein
- Analyze the simulation data

# How to do a molecular dynamics simulations study for a practical biomolecular system (the small protein)



#### Research question?

- Modelling method according to the relevant length and time scales involved in the phenomena.
- Design molecule study system so that matches the research question.
- Appropriate environment (in atomistic detail modelling, for example, solvent such as water and ions or added salt)

#### Simulation needs defined

- "size" -> simulation box
- "boundaries"
- Interactions of all atoms / molecules in the system (force-field)
- Choice of statistical mechanics ensemble (Gibbs free energy / isothermal-isobaric ensemble most common for chemical and biomolecular systems). T and p controlled by algorithms.
- System conditions such as molecular concentrations, pressure p, temperature T, ...
- How is time evolution obtained? Integration algorithm for the equations of motion resulting from forces on each particle.
- Analysis methods / analysis questions

## A GROMACS workflow for exercise 1. The workflow takes a PDB (Protein Data Bank) structure file as input and returns a MD trajectory.

