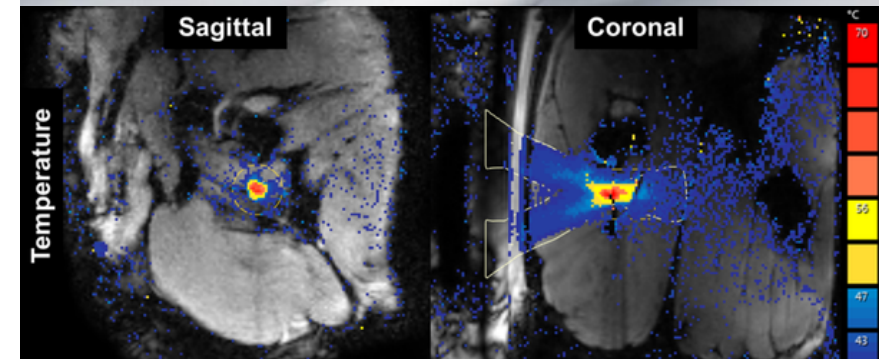
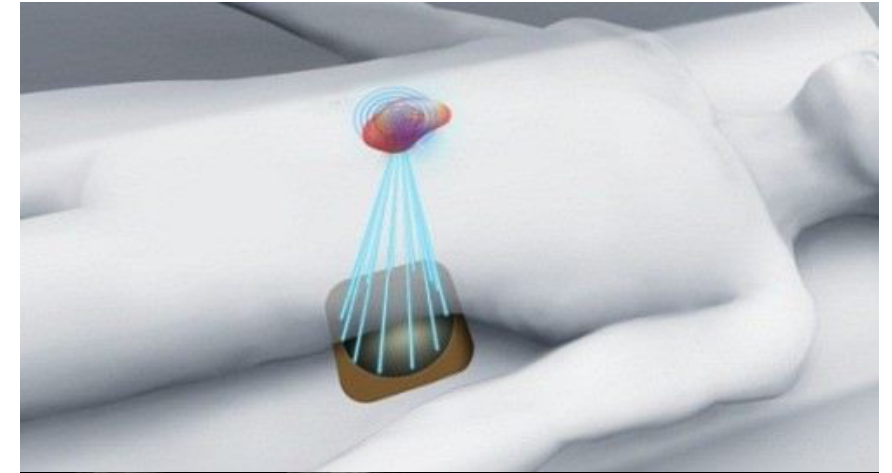
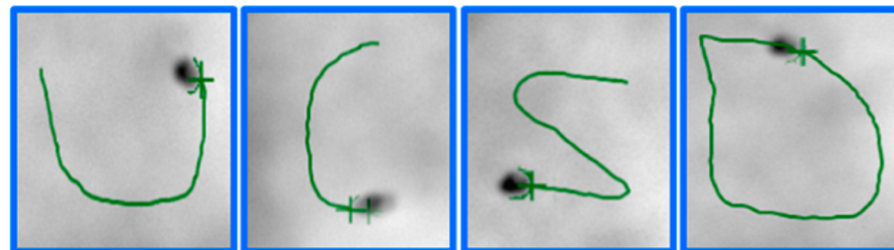
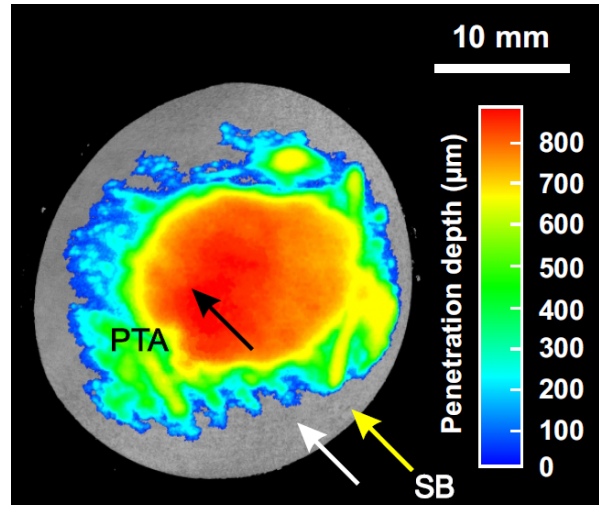


Biomedical Ultrasonics, 5 cr

Heikki Nieminen

7.1.-31.5.2019



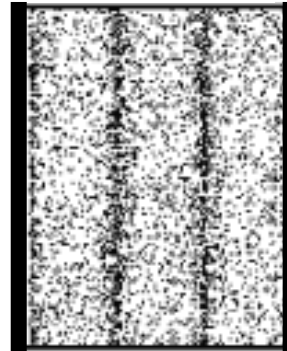
Standing wave



plane wave: →



plane wave: ←



plane waves: superposition

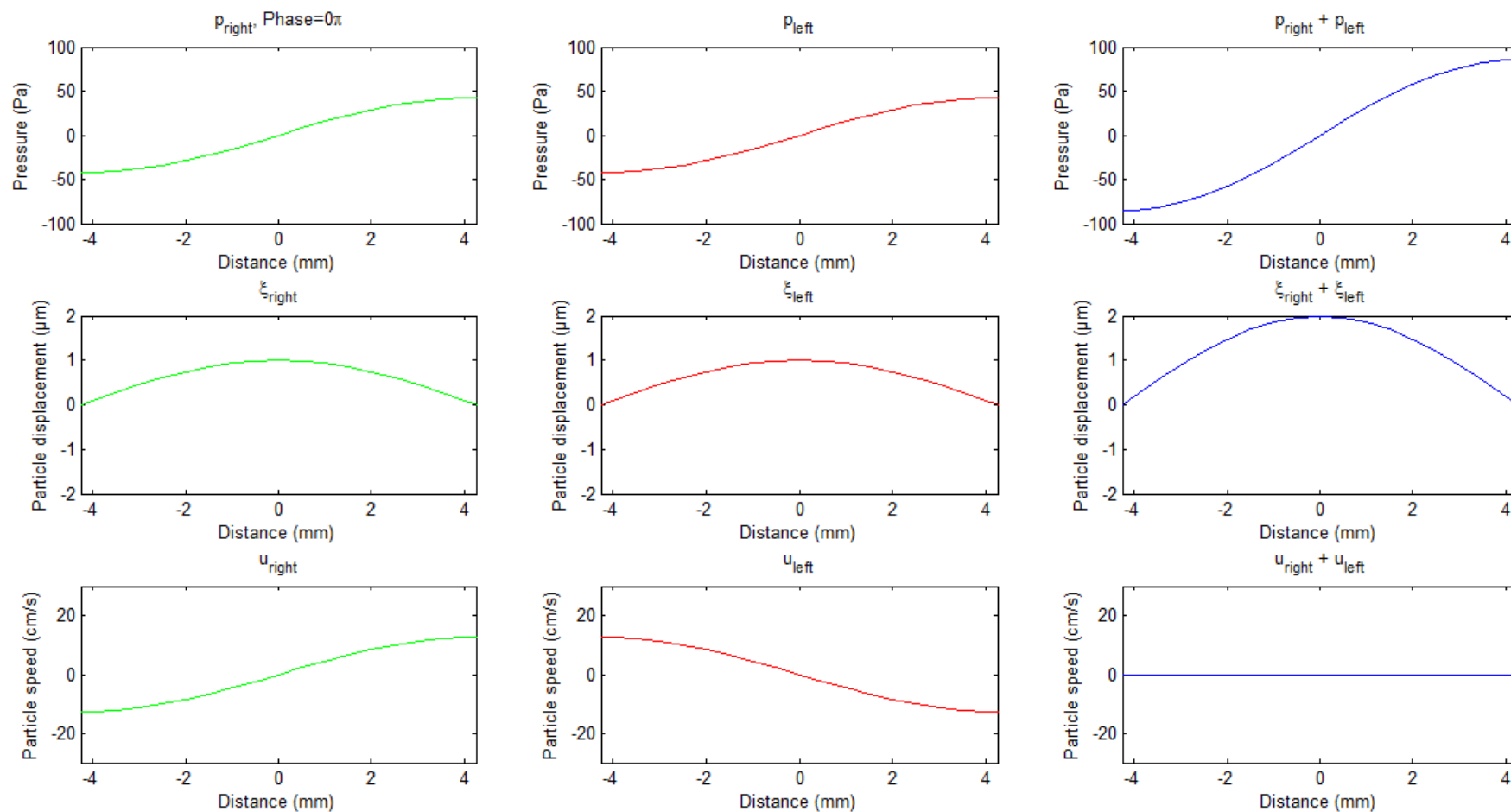
Where are the pressure nodes/anti-nodes?

Where are the displacement nodes?

Matlab demo

$\lambda/2$ resonator

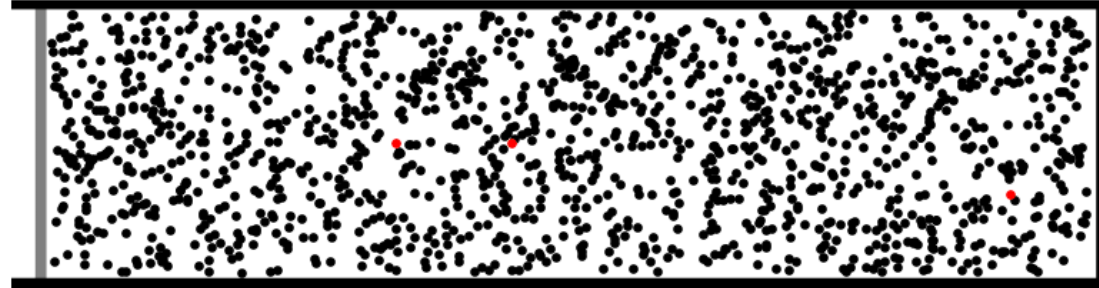
$c = 340 \text{ m/s}$, $f = 20 \text{ kHz}$



Standing wave

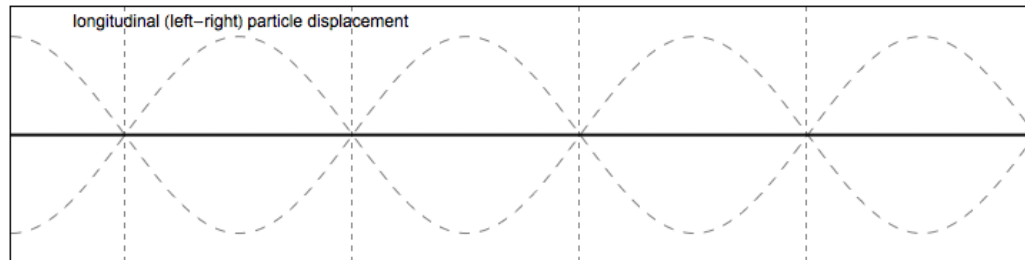
Where is the energy density the lowest?

Where is the energy density the highest?

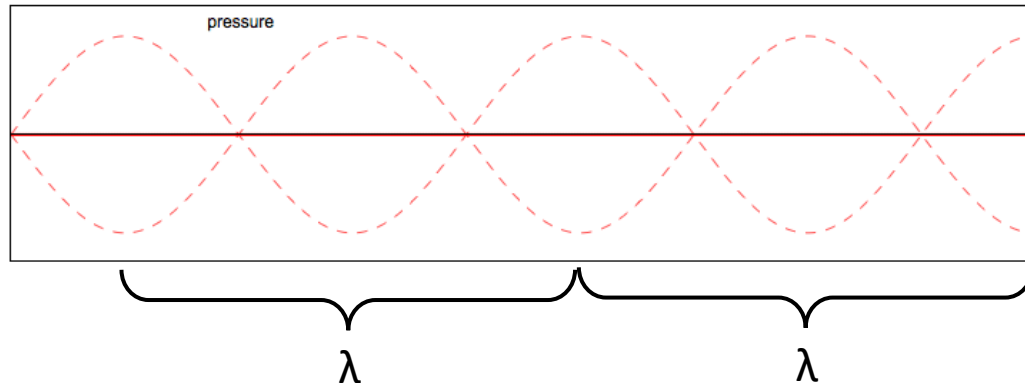


©2012, Dan Russell

Particle displacement:



Pressure:



Acoustic radiation force on a sphere within a standing wave

- A linear one-dimensional stationary standing wave the time-averaged radiation force applied to a sphere can be expressed as

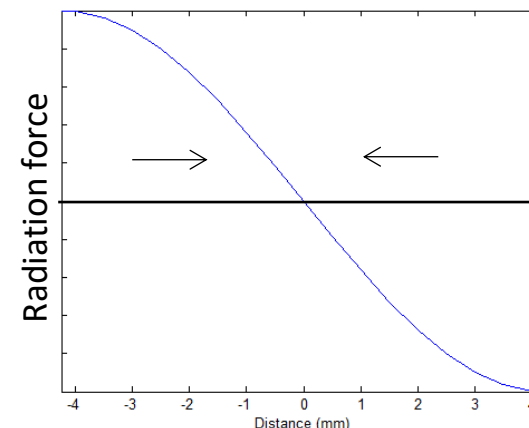
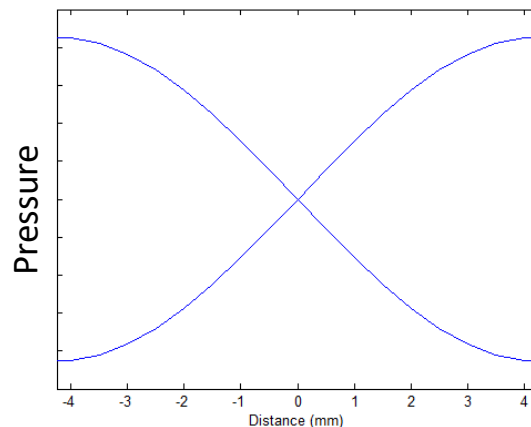
$$F = - \left(\frac{\pi \hat{p}^2 V_s \beta_m}{2\lambda} \right) \phi \sin(2kx) = - \underbrace{\frac{4\pi}{3} R^3}_{V_s} \underbrace{\frac{k}{2}}_{k = \text{wavenumber} = 2\pi/\lambda} \underbrace{\frac{\hat{p}^2}{2\rho_m c_m^2}}_{\text{Maximum energy density}} \underbrace{\phi}_{\text{Contrast factor}} \sin(2kx)$$

where

- R = sphere radius
- x = distance from the pressure node
- \hat{p} = peak pressure amplitude of the standing wave
- $\beta_m = 1/K = \text{compressibility}$
- ϕ = is a contrast factor, *i.e.* $\phi = \frac{5\Lambda - 2}{2\Lambda + 1} - \frac{1}{\Lambda\sigma^2} = \frac{5\Lambda - 2}{2\Lambda + 1} - \frac{\beta_s}{\beta_m}$, where $\Lambda = \rho_s/\rho_m$, $\sigma = c_s/c_m$, and $s = \text{sphere}$, $m = \text{medium}$.

$\lambda/2$ resonator

When $\phi > 0$, the sphere travels towards the pressure node. When $\phi < 0$, the sphere travels towards the pressure antinode.



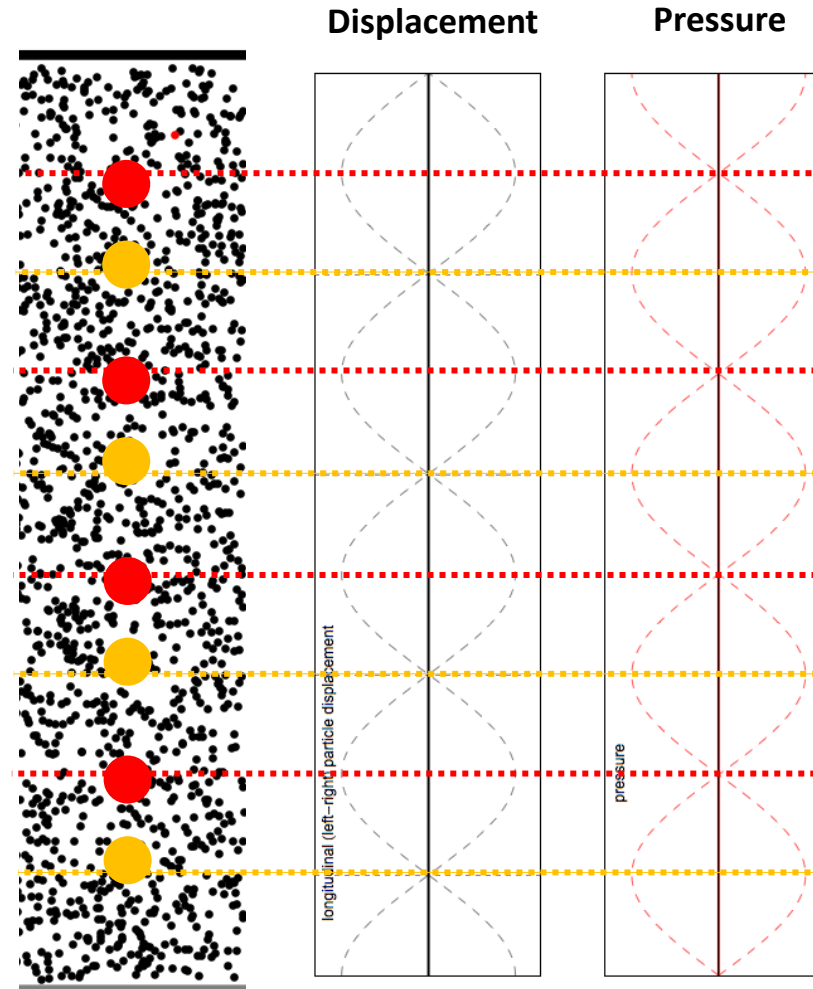
Where does the particle want to go? Acoustic trap with blood

- = red blood cell
- = fat particle

Gravitation ↓

Heavy particles go
to pressure node

Light particles go
to pressure anti-node



Wall-less chemistry by acoustic levitator

**Multiple
polystyrene
spheres**



**Multiple
liquid
droplet**



**Liquid
compressed to
a pancake**



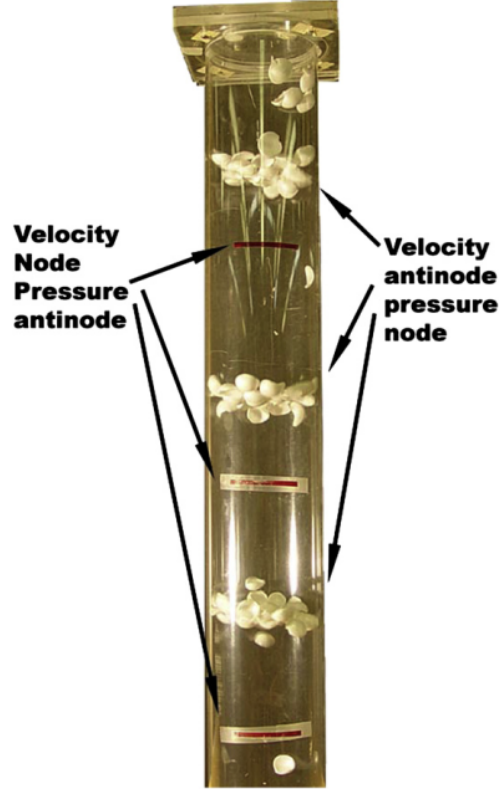
**Heavy
Tungsten
sphere**



Acoustic levitator

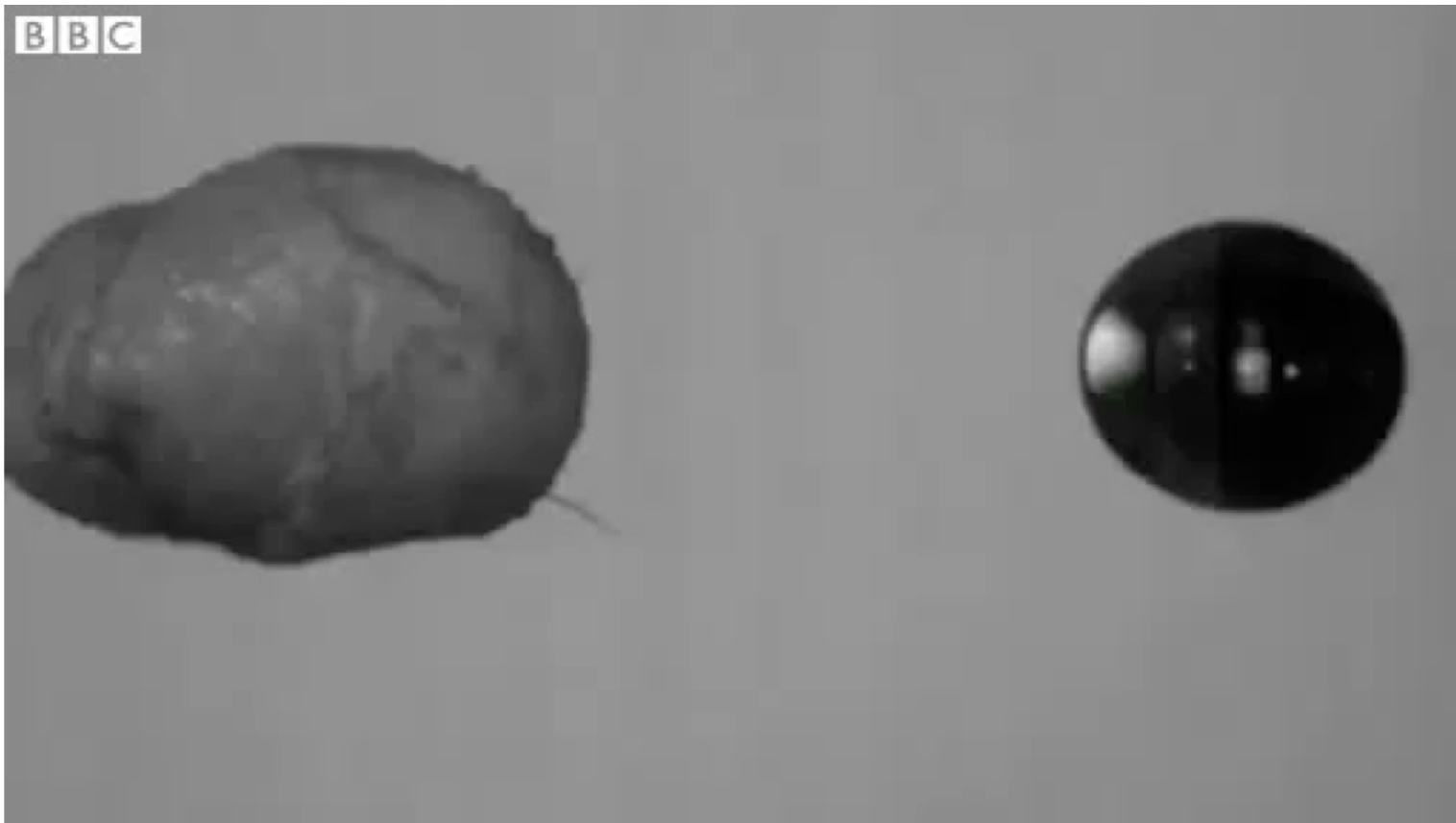


Styrofoam chips levitating in a vertical Kundt's tube



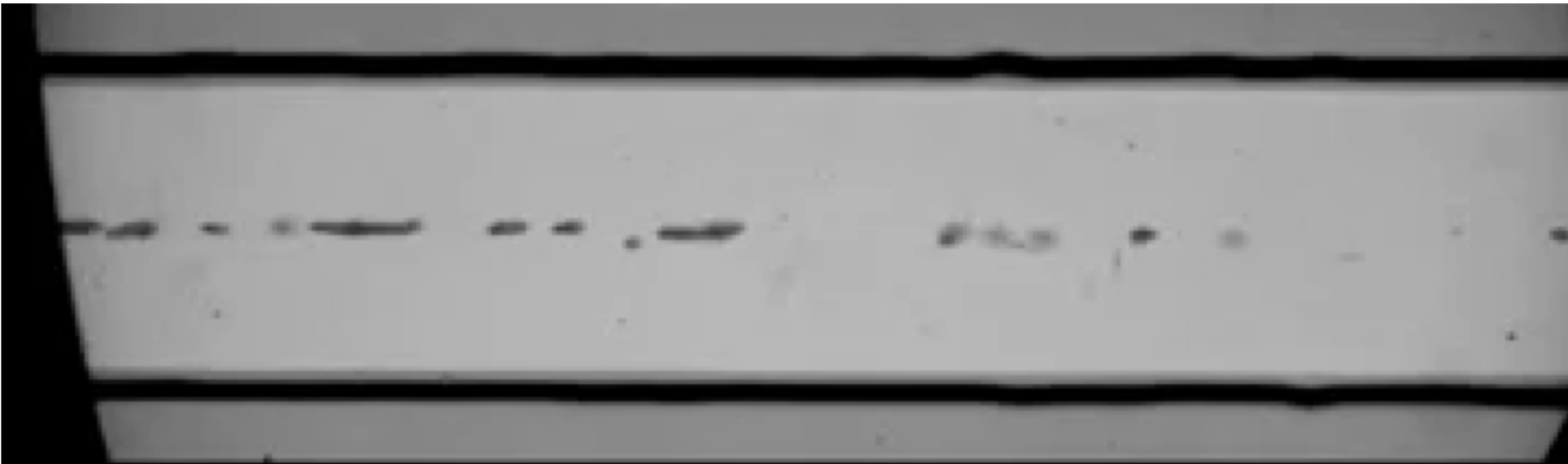
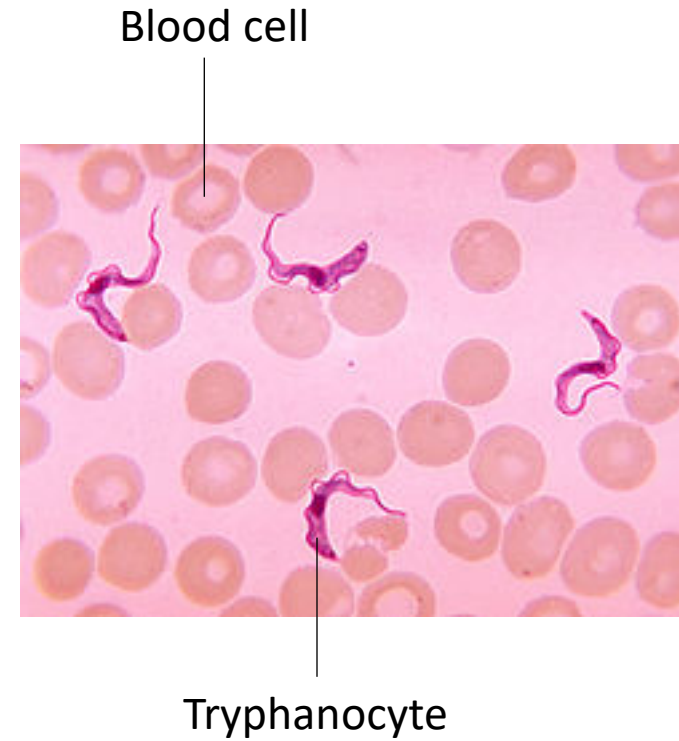
Acoustic levitator

- Wall-less chemistry:



Acoustic levitator

- Separation of blood cells and tryphanocytes:

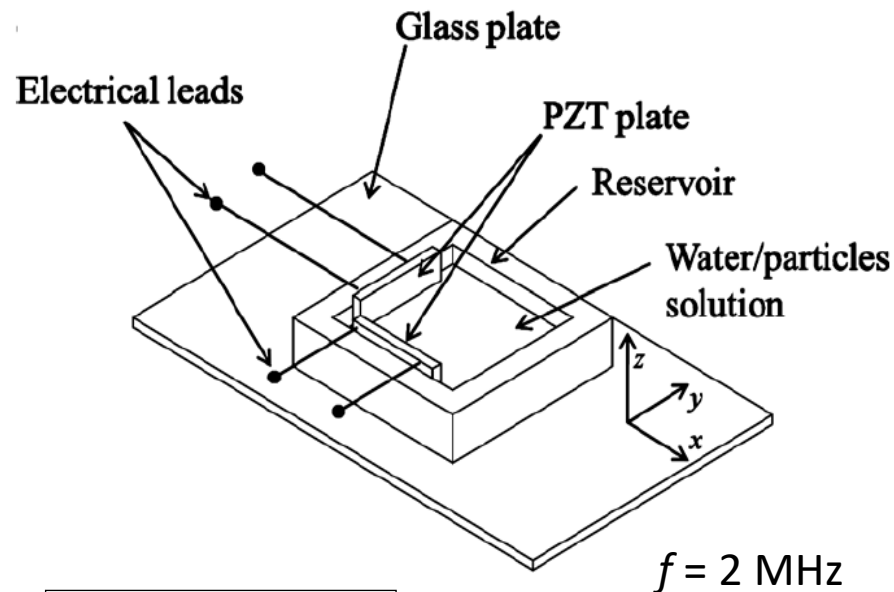


Advantages of acoustic levitators

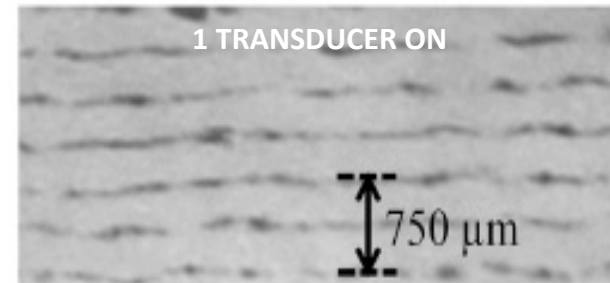
- Wall-less chemistry, bio-chemistry
- Remote forces → non-touching platform
- Trapping of entities in blood stream
- However, not yet applied in human *in vivo*

Separation of diamond nanoparticles

- Radiation force
- Collecting 5nm diamond spheres using radiation force in standing waves



$$f = 2 \text{ MHz}$$
$$\rho_0 = 50.2 \text{ kPa}$$

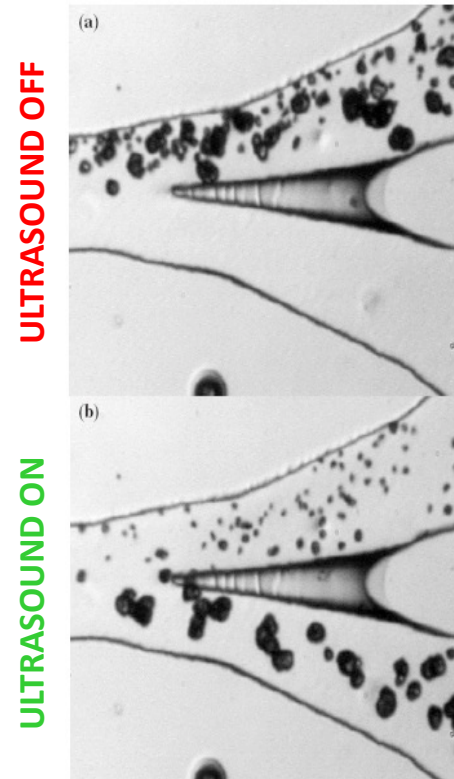
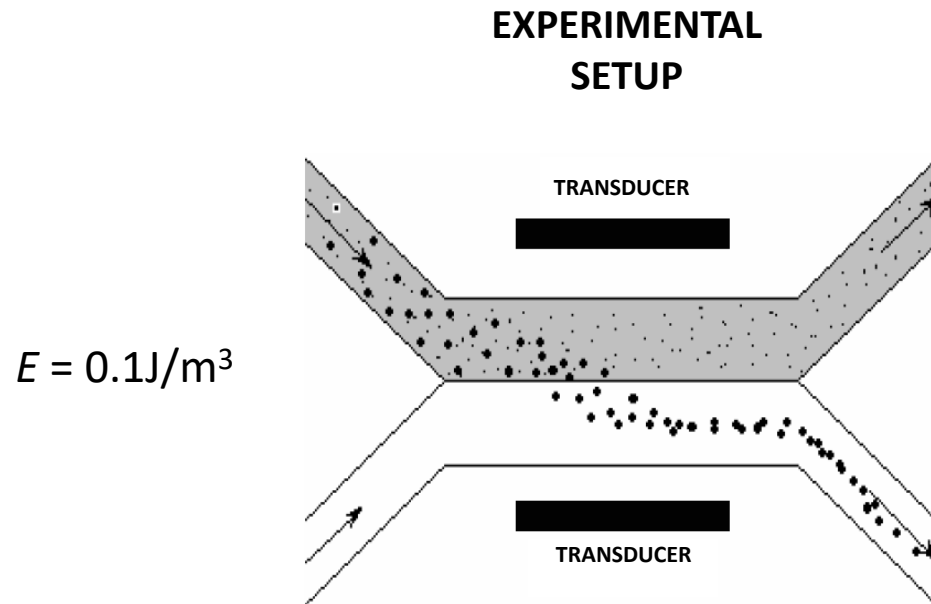


Raeymaekers *et al.* *J. Appl. Phys.* (2011)
doi:10.1063/1.3530670

Radiation force – standing wave

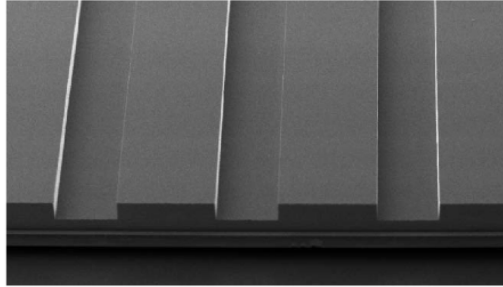
- Separation of blood cells: standing waves in microfluidic channel

Why are big particles moved and not small ones?

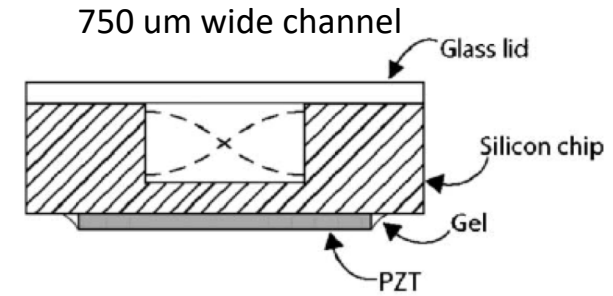
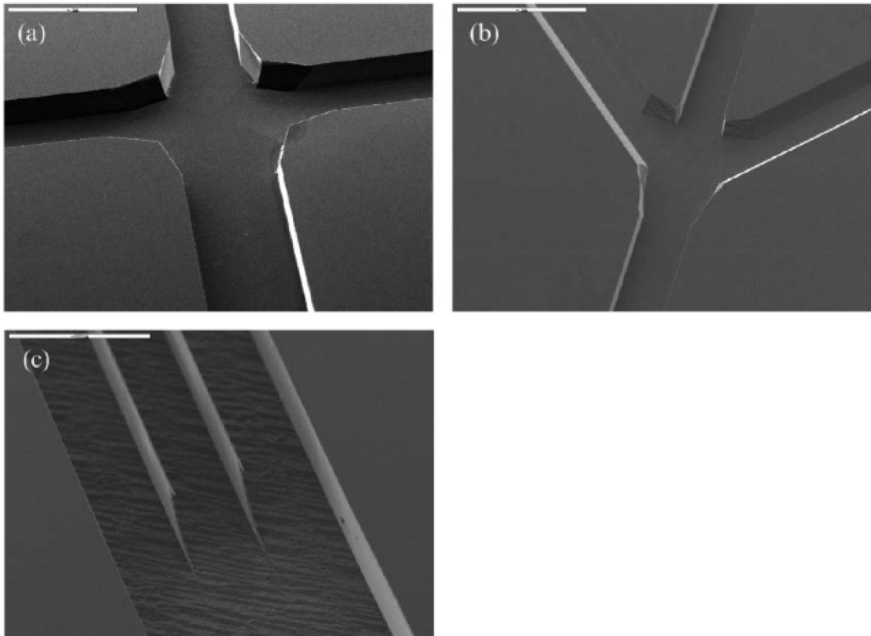


Cell separation with ultrasound

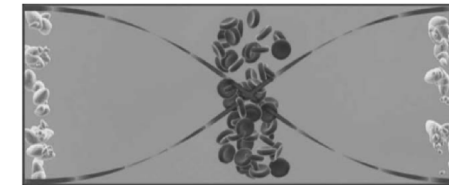
Single channel
in silicon wafer



Complex channels in silicon wafer



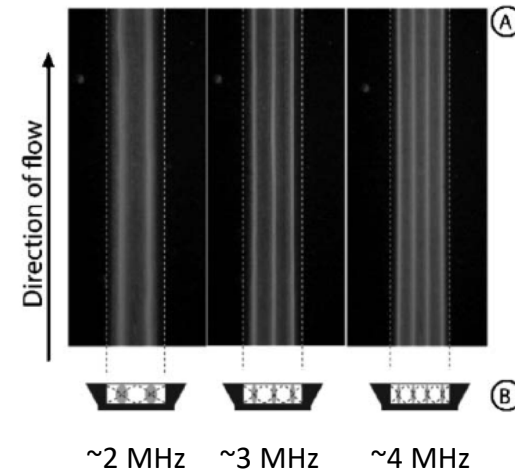
Cell separation principle



Fat Red blood cells Fat

Separation in single channel

Separation at different harmonics



Cell separation with ultrasound

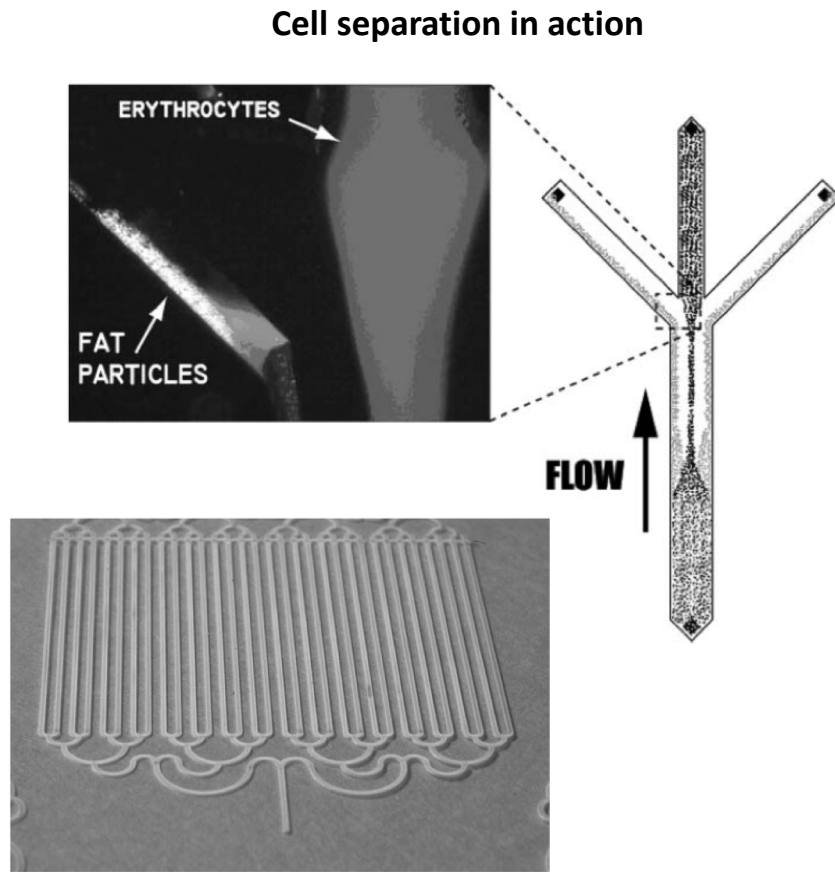


Fig. 20 2^5 bifurcation channel tree holding 32 parallel $\sim 400 \mu\text{m}$ channels realised by micromilling in a polycarbonate sheet. It is possible to realize separation channels in polymers but due to acoustic losses in the bulk material this is less preferential.

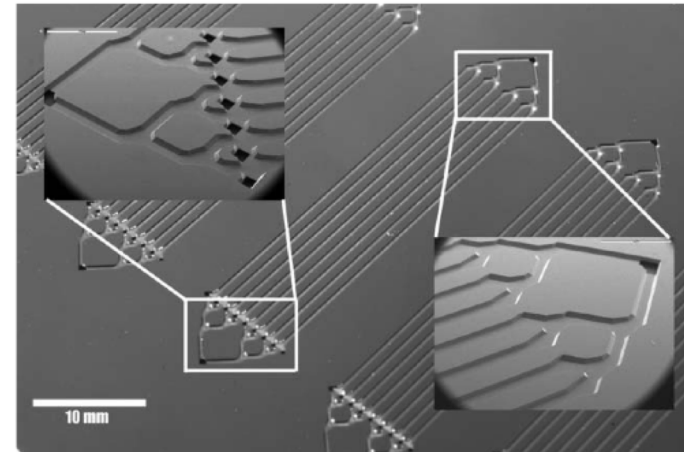


Fig. 21 Picture of eight channel separation structures with scanning electron micrographs showing details of the bifurcation channel outlets (left) and inlet (right). The row of black diamond-shaped structures are the waste outlets. These are connected to a common waste outlet on the back side of the chip. The single outlet at the far left is the enrichment outlet.

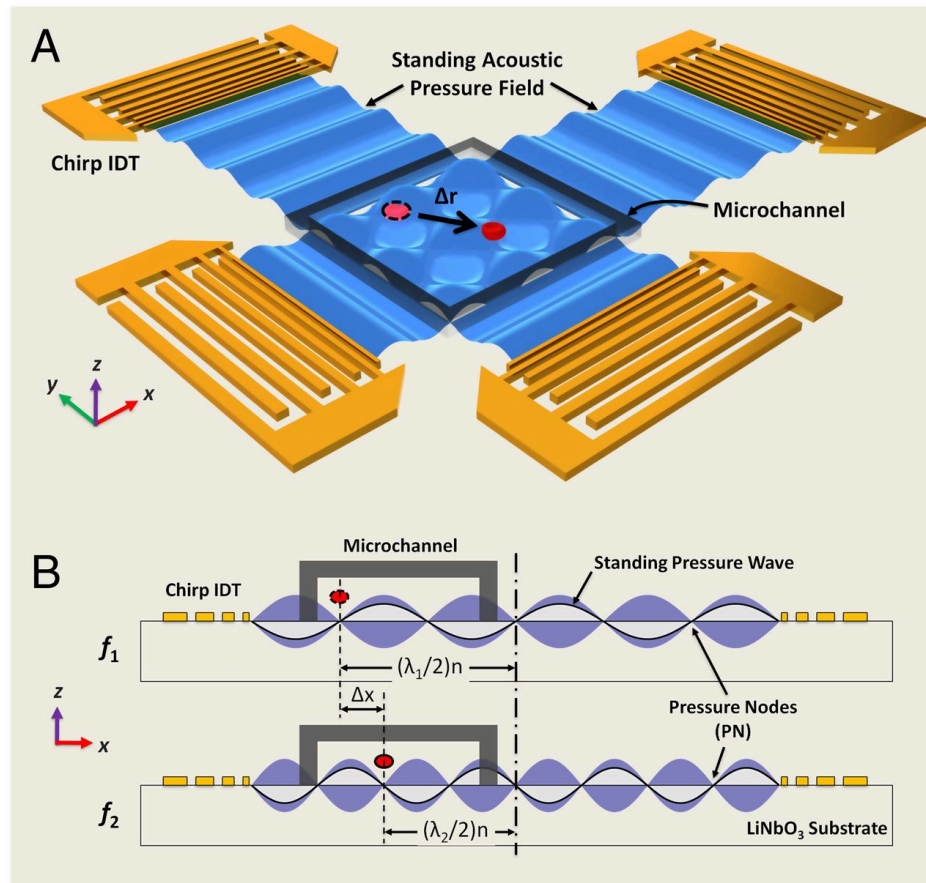
Bifurcation enables:

- More efficient particle separation
- Higher concentration of the end product
- Less contaminants in the end product

Radiation force
(standing SAWs)

Surface acoustic wave (SAW) tweezers

Movement of an organism using SAW tweezers



IDT = interdigital transducers

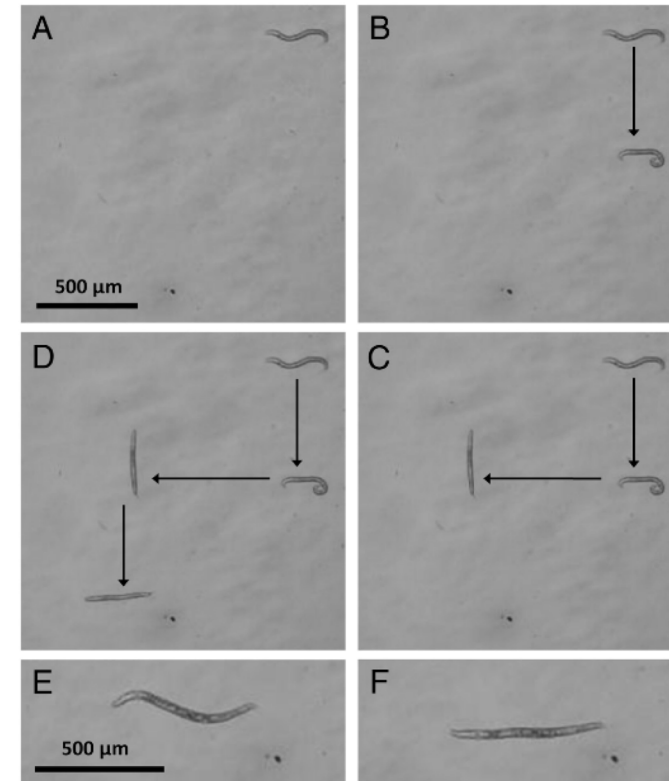
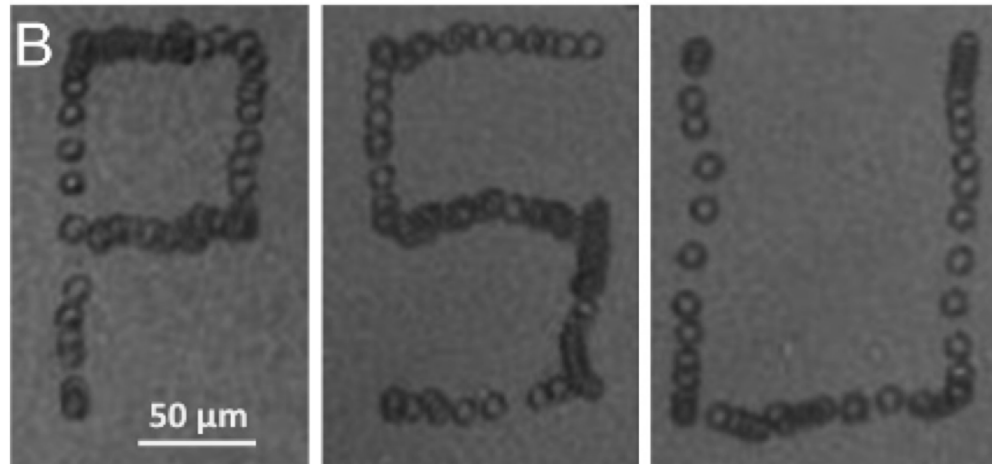


Fig. 5. Single *C. elegans* manipulation. One single *C. elegans* was (A) trapped, (B) moved in y direction, (C) moved in x direction, and (D) moved in y direction again and released, with the average velocity of approximately 40 $\mu\text{m/s}$. An optical image of *C. elegans* (E) before and (F) after being fully stretched. *C. elegans* = Caenorhabditis elegans

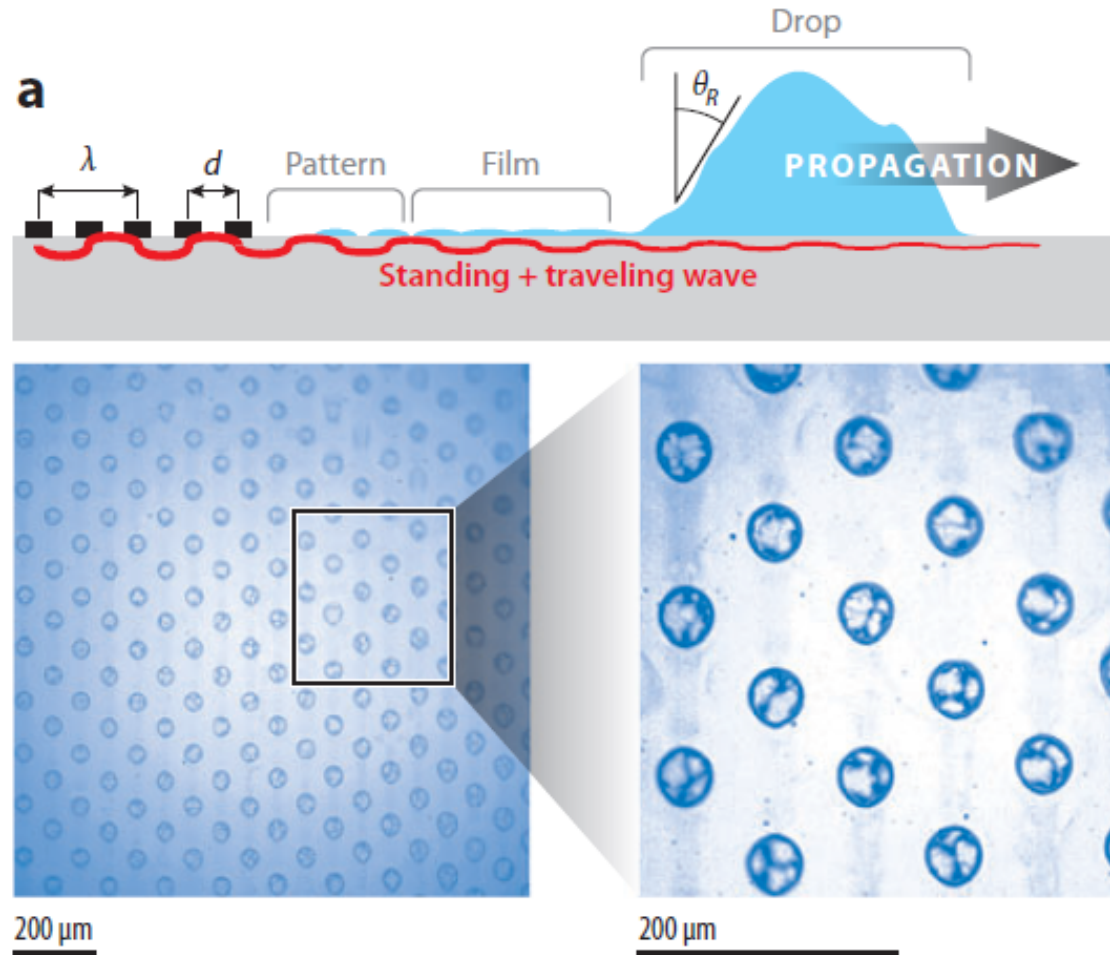
Track generated by surface acoustic wave tweezers

Path drawn by

- A. Polystyrene spheres
- B. Bovine red blood cells



Droplet matrix generation



Biological responses to radiation force

Table 3.3. *Summary of pulsing regimes required to generate acoustic bio-responses apparently caused by radiation pressure.*

Effect	Pulse length	Number of pulses
Choroid blanching (Lizzi)	100 μ s	1
Tactile sensation (Daleki)	1 ms	repetitive
Cardiac response in frog (Daleki)	5 ms	1
Fluid movement (Starritt)	0.5 μ s	1

Drug delivery & standing waves

- How would you apply standing wave radiation force for drug delivery?
 - IOP?
 - Melanoma?
 - Meniscus tear?
 - Other ideas?

Summary: Radiation force

- Radiation force (travelling wave):
 - Can move tissue and tissue interfaces
 - Secondary streaming near a moving interface?
 - Can translate particles (and gas voids)
 - Translation of drug or drug vehicle
 - Contribution to drug localization/deposition/release
 - Depends on material properties:
 - Absorption
 - Reflection
 - Scattering
 - Speed of sound