



Aalto University  
School of Engineering

**MEC-E5003**

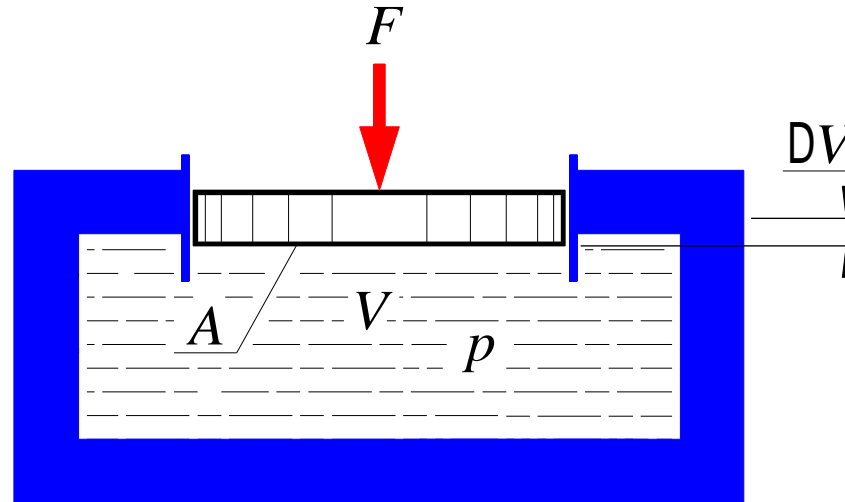
**FLUID POWER BASICS**

**Study Year 2018 - 2019**

# Hydraulic fluids, part 1

# Compressibility of fluid and elasticity of system

$$DV = \frac{1}{K_f} \times V_0 \times Dp$$



$K_f =$  Bulk modulus of fluid, [N/m<sup>2</sup>]

$\sim 1500 \text{ @ } 2000 \text{ MN/m}^2$

Mineral oil	$K_f = 1.5 \text{ GPa} - 1.6 \text{ GPa}$
Water	$K_f = 2.1 \text{ GPa} - 2.2 \text{ GPa}$

The pressure in a fluid volume can be changed (also) by altering the size of the fluid volume

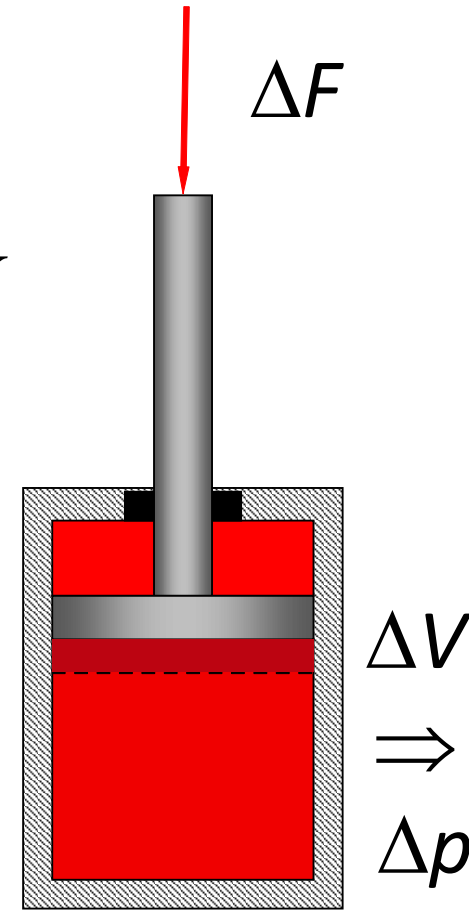
Attention: the sign (-)

$$\Delta p = -\frac{K_f}{V} \Delta V$$

- $K_f$  bulk modulus of fluid [Pa]
- $V$  (changing) volume full of fluid [m<sup>3</sup>]
- $\Delta V$  change in volume [m<sup>3</sup>]

How much does pressure increase if the volume of a (stiff) chamber filled with hydraulic oil is reduced by 1 %?

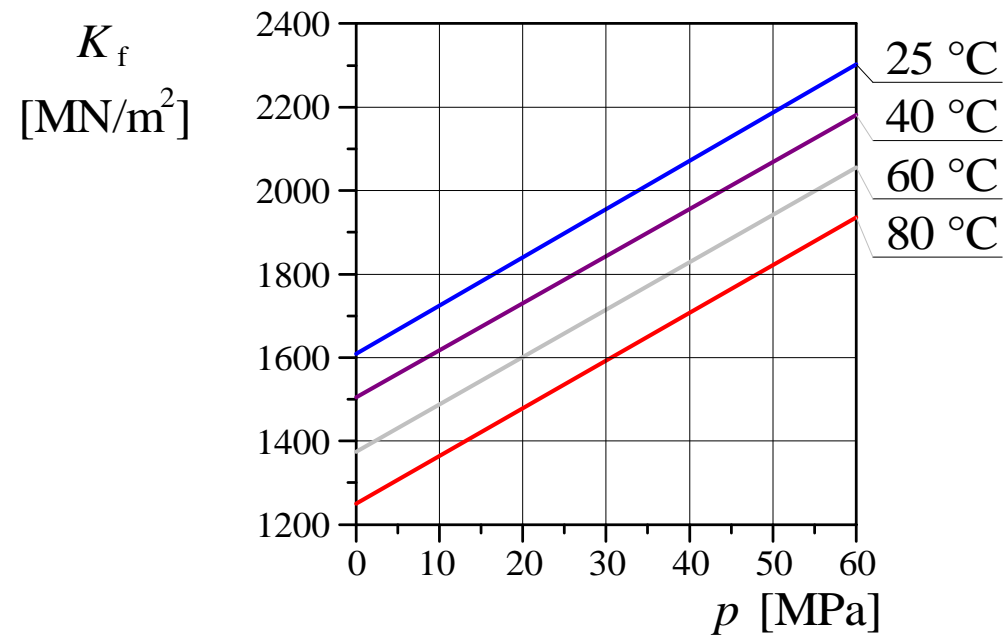
Bulk modulus of fluid [Pa],  $\sim 1.6 \cdot 10^9$  Pa (mineral oil)



$$\Delta V/V = 0.01 \Rightarrow \Delta p = 16 \cdot 10^6 \text{ Pa} = 160 \text{ bar}$$

## Bulk modulus of fluid

Effect of pressure and temperature



Volume of cylinders  
divided by  
Total volume  
etc.

### Effective bulk modulus of system $K_e$

$$\frac{1}{K_e} = \frac{1}{K_f} + \sum_{i=1}^{N1} \frac{V_{c,i}}{V_t} \times \frac{1}{K_{c,i}} + \sum_{j=1}^{N2} \frac{V_{p,j}}{V_t} \times \frac{1}{K_{p,j}} + \sum_{k=1}^{N3} \frac{V_{h,k}}{V_t} \times \frac{1}{K_{h,k}} + \frac{V_a}{V_t} \times \frac{1}{K_a}$$

### Effect of system components

$$K = \frac{E_m \cdot s}{d}$$

Pipes, cylinders, etc.

- $E_m$  modulus of elasticity
- $s$  thickness of wall
- $d$  inner diameter

$$K_h = 70\text{--}700 \text{ MN/m}^2$$

Hoses

$$K_a = 1,4 \times p$$

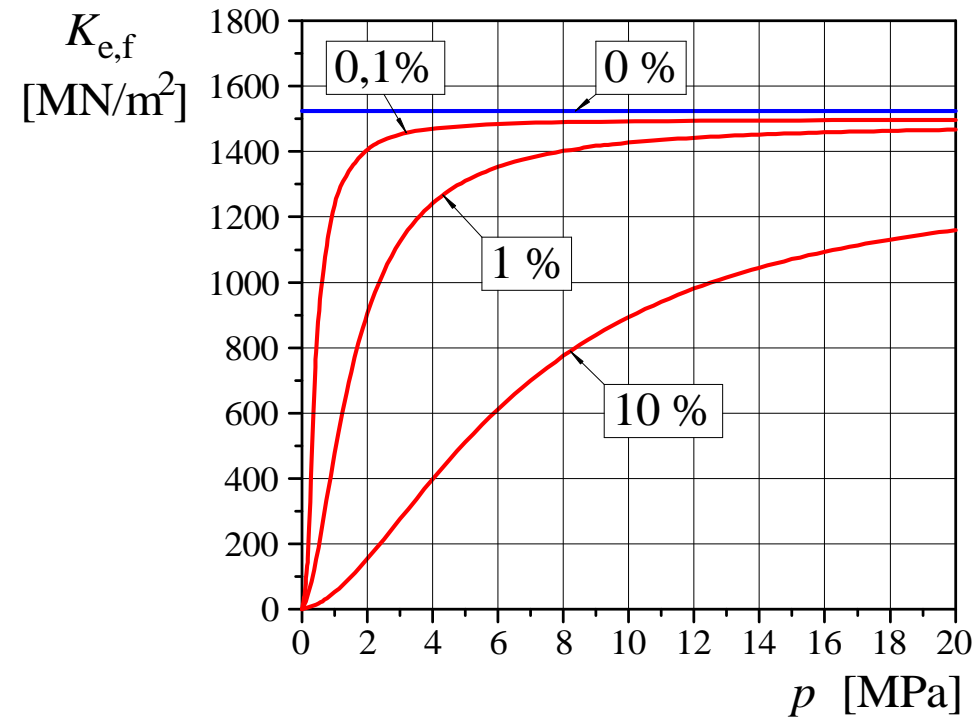
Free air (air bubbles)

$$DV = \frac{1}{K_e} \times V_t \times Dp$$

### Significance and effect of elasticity

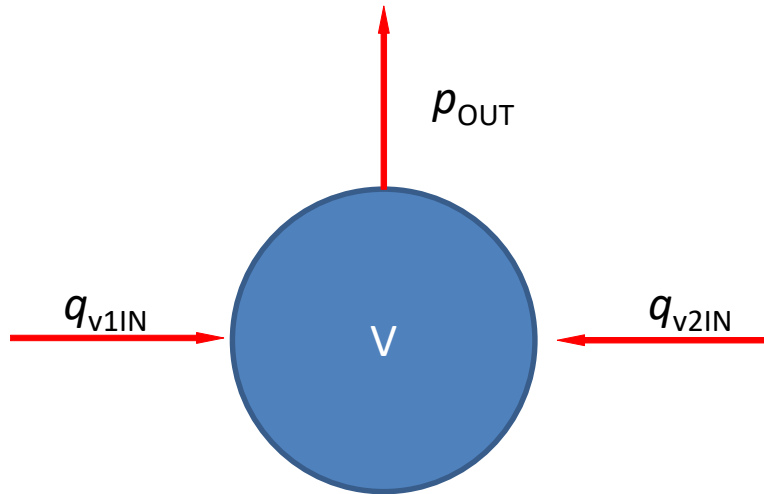
- depends on application
- no significance in force production
- has an impact on the accuracy in position, speed and acceleration control systems
- defines the actuator's mechanical stiffness

## Effect of free air and pressure on the bulk modulus

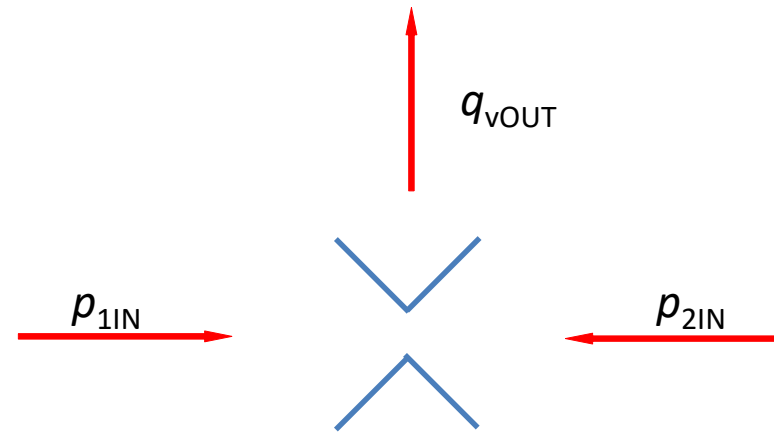




# Simulation model



**"Fluid volume"**: pressure is solved, flow rates as inputs

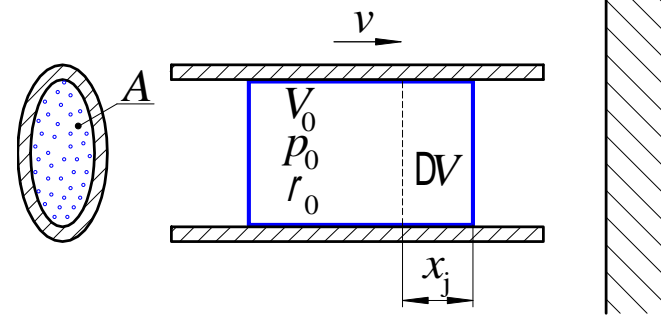
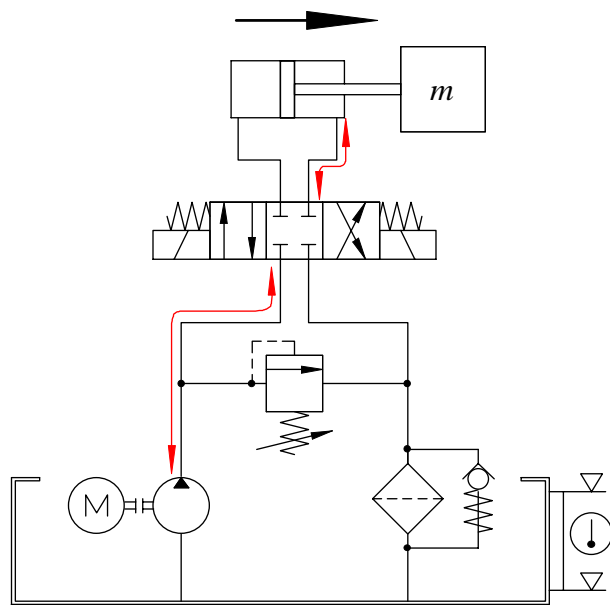


**"Valve"**: flow rate is solved, pressures as inputs

- Common way to realize a model of a system is to divide it into
  - Fluid volumes (pressure is essential to these volumes)
  - Components between fluid volumes ("valves" ja "pumps", flow rate is essential to these volumes)

# Pressure surge (aka shock)

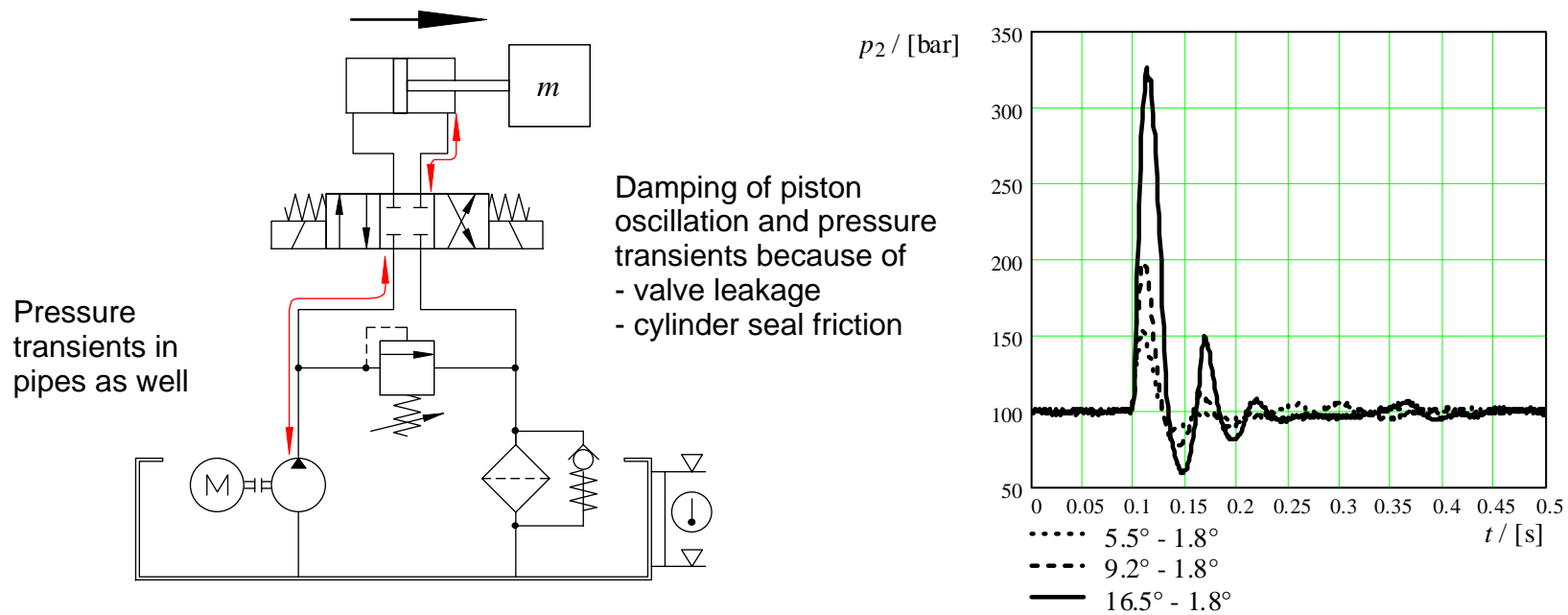
Source: Change in flow velocity



$$E_{\text{kin}} = \frac{1}{2} \times m \times v^2$$

$$E_{\text{spr}} = \frac{1}{2} \times k_R \times x_j^2$$

## Outcome: Rise of pressure level and shock wave

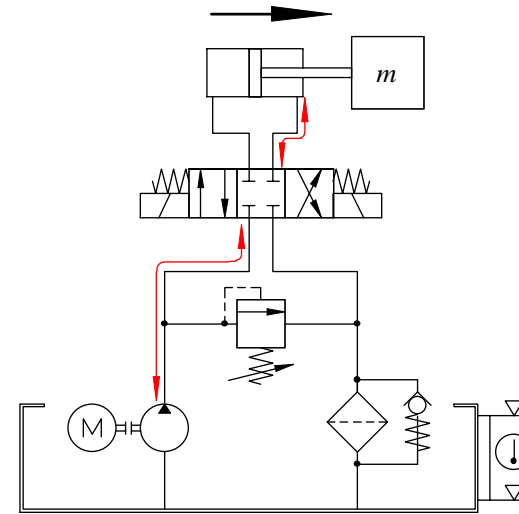


Velocity of pressure wave

$$c = \sqrt{\frac{K_e}{r}}$$

Critical time

$$t_{cr} = \frac{2 \times l}{c}$$

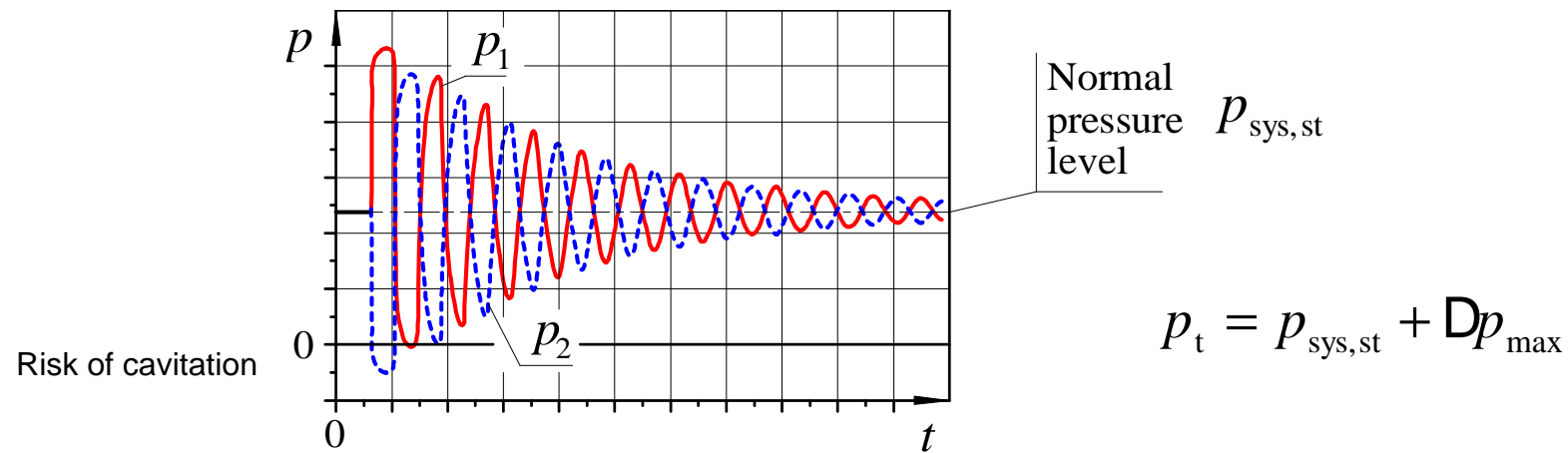
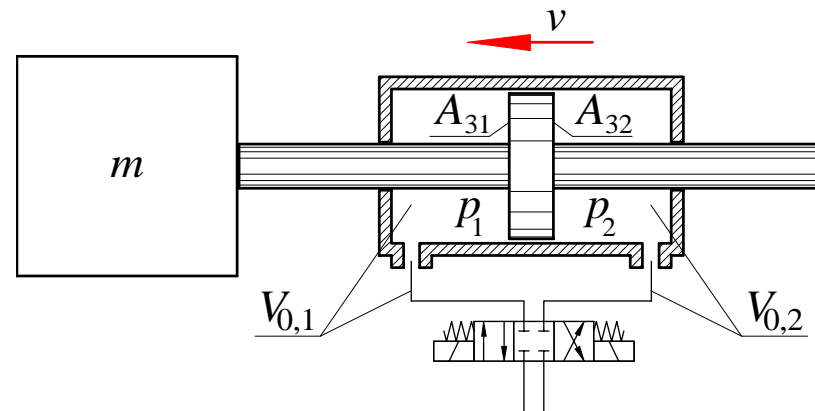


$$t_c > t_{cr}$$

$$\Delta p_{max} = \frac{2 \times l \times r_0 \times v}{t_c}$$

$$t_c < t_{cr}$$

$$\Delta p_{max} = r_0 \times c \times v$$



### Consequences of pressure shock:

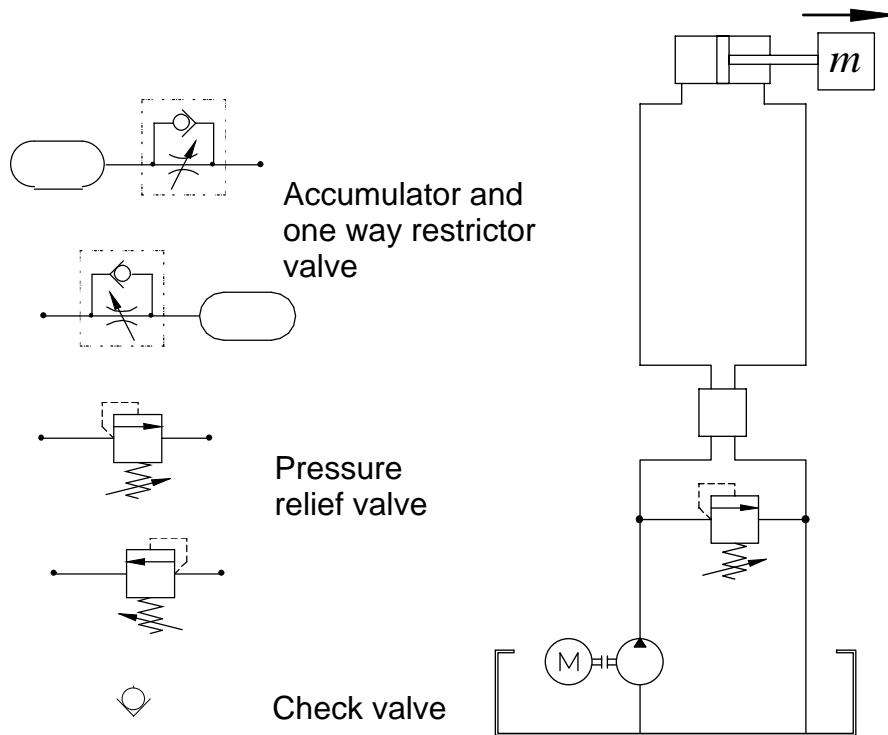
- damages the hydraulic system
- damages systems connected to hydraulic system

### Diminishing the pressure shock:

- lower flow velocity
- slower valves
- lower actuator velocities
- smaller inertial loads
- larger fluid volumes
- with assisting components

Effects of these actions?

## Diminishing pressure shock with hydraulic components



# Cavitation

Pressure in fluid lowers below atmospheric pressure:

- in fluid dissolved air separates into air bubbles

® air bubble cavitation

Pressure in fluid lowers to vapour pressure of the fluid:

- vapour bubbles start to appear

® cavitation

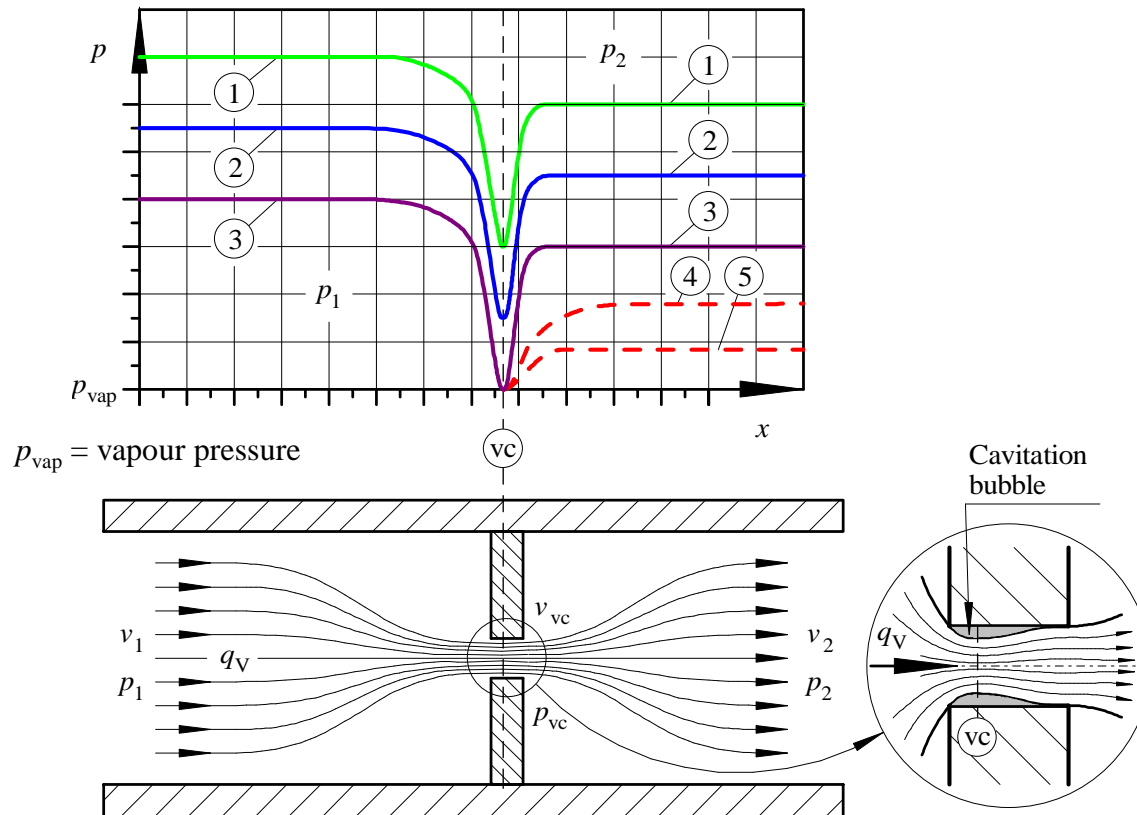
Lowering of the pressure is due to pressure losses in the flow channel

Cavitation appears typically in:

- pumps and their suction lines

- orifices (throttles)





$$q_v = C_q \times A \times \sqrt{\frac{2 \times \Delta p}{\rho}}$$

Cavitation  
in orifice

$$q_v \propto C_q \times A \times \sqrt{\frac{2 \times \Delta p}{\rho}}$$

## Consequences of cavitation

When pressure rises:

- bubbles collapse rapidly (“implosion”)

Ⓜ pressure shocks

Ⓜ material damages, rapid wear, noise

In addition in pumps

Ⓜ the vapour bubbles reduce output flow

# Lecture themes – Intermediate Recap

Does the elasticity of fluid have any significance?

Pressure shocks, harmless heaving?

Cavitation, is it something to worry about?