

# **EQUATIONS, CHARTS AND TABLES FOR MASS TRANSFER**

**All equations are in SI units, unless differently stated  
below the equations**

## LIST OF SYMBOLS

(the meanings of symbols are the following unless stated differently below the equations)

- A surface area,  $m^2$   
a activity, -  
c concentration,  $mol/m^3$   
 $c_p$  specific heat at constant pressure,  $J/molK$  or  $J/kgK$   
 $c_{pk}$  specific heat of humid air at constant pressure,  $J/kg_{d.a.}K$   
d diameter, m  
 $D_{AB}$  diffusion coefficient between components A and B,  $m^2/s$   
 $D_{AK}$  Knudsen diffusion coefficient of component A,  $m^2/s$   
 $D_{AK,eff}$  effective Knudsen diffusion coefficient of component A,  $m^2/s$   
 $D_{eff}$  effective Knudsen diffusion coefficient,  $m^2/s$   
Gr Grashof number, -  
g acceleration due to gravity =  $9.807 m/s^2$   
H enthalpy, J  
 $\dot{H}$  enthalpy flow rate, W  
h specific enthalpy,  $J/kgK$  or  $J/molK$   
 $h_k$  specific enthalpy of humid air,  $J/kg_{d.a.}$   
J molar flux,  $mol/m^2s$   
j diffusion flux,  $mol/m^2s$   
Kn Knudsen number, -  
k mass transfer coefficient, m/s  
k' mass transfer coefficient corresponding to equimolar diffusion ( $J_A = -J_B$ ), m/s  
 $k_B$  Boltzmann's constant =  $1.381 \cdot 10^{-23} J/K$   
 $k_p$  permeability (Darcy's law),  $m^2$   
Le Lewis number, -  
l 1. heat of evaporation,  $J/mol$  or  $J/kg$   
2. length or characteristic length, m  
 $l_0$  heat of evaporation of non-bound liquid,  $J/mol$  or  $J/kg$   
M molar mass,  $kg/mol$   
m mass, kg  
 $\dot{m}$  mass flow rate,  $kg/s$   
N mass flux,  $kg/m^2s$   
n amount of substance, mol,  
Pe Péclet number, -  
Pr Prandtl number, -  
P pressure, Pa or bar  
 $p_A$  partial pressure of component A, Pa or bar  
 $p_A'$  partial pressure of saturated component A, Pa or bar  
q heat flux,  $W/m^2$   
R universal gas constant =  $8.314 J/molK$   
Ra Rayleigh number, -

Re Reynolds number, -  
 r 1. sorption heat, J/mol; J/kg  
    2. radius, m  
    3. mass transfer resistance,  $\text{m}^2\text{sPa/kg}$   
 s real path length, m  
 S term for formation of a component,  $\text{kg/m}^3\text{s}$  or  $\text{mol/m}^3\text{s}$   
 Sc Schmidt number, -  
 Sh Sherwood, -  
 T temperature, K  
 t 1. time, s  
    2. temperature,  $^{\circ}\text{C}$   
 $t_m$  wet bulb temperature,  $^{\circ}\text{C}$   
 V volume,  $\text{m}^3$   
 v velocity, m/s  
 $w_r$  moisture content/ratio for porous materials,  $\text{kg}_{\text{H}_2\text{O}} / \text{kg}_{\text{k.a.}}$   
 x 1. molar fraction, -  
    2. humidity of wet air/gas,  $\text{kg}_{\text{H}_2\text{O}} / \text{kg}_{\text{d.a.}}$   
 y molar fraction in gas phase, -  
 z coordinate, m  
  
 $\alpha$  convective heat transfer coefficient,  $\text{W} / \text{m}^2\text{K}$   
 $\gamma$  surface tension,  $\text{J/m}^2$   
 $\eta$  dynamic viscosity,  $\text{kgm}^{-1}\text{s}^{-1}$   
 $\varphi$  relative vapor pressure, -  
 $\lambda$  thermal conductivity,  $\text{W/mK}$   
 $\lambda_m$  mean free path, m  
 $\nu$  kinematic viscosity,  $\text{m}^2 / \text{s}$   
 $\rho$  density,  $\text{kg/m}^3$   
 $\sigma_{ii}$  collision diameter, m  
 $\tau$  tortuosity, -  
 $\xi$  activity coefficient, -  
 $\emptyset$  heat transfer rate/power, W  
 $\Phi$  porosity (volume fraction), -

### Subscripts

A, B components (usually binary mixture)  
 i 1. component (when the number of components is not limited or defined)  
    2. dry air  
 d.a. dry air  
 eff effective  
 h vapor  
 k.a. solid material  
 ref reference

## MIXTURE THERMODYNAMICS

### Ideal gases

$$p_i V = n_i RT \quad n_i = \frac{m_i}{M_i} \quad \rho_i = \frac{p_i M_i}{RT} \quad \rho = \sum_i \rho_i \quad p = \sum_i p_i \quad y_i = \frac{p_i}{p}$$

### Wet ideal gases

$$x \equiv \frac{m_A}{m_B} = \frac{\rho_A}{\rho_B} \quad x = \frac{m_A}{m_B} = \frac{\rho_A}{\rho_B} = \frac{M_A}{M_B} \frac{p_A}{p - p_A} \quad p_A = \frac{x}{\frac{M_A}{M_B} + x} p$$

$$h_k \equiv \frac{H}{m_B} \quad h_k = h_B + x h_A \quad h_k = c_{pB}(T - T_{ref}) + x(l_{A,ref} + c_{pA}(T - T_{ref}))$$

$$\dot{H} = \dot{m}_B h_k$$

### Humid air (h=water vapor, i = dry air, k = humid air)

$$x = 0.6220 \frac{p_h}{p - p_h} \quad p_h = \frac{x}{0.6220 + x} p \quad \phi \equiv \frac{p_h}{p_h'(T)}$$

$$M_i = 0.02896 \text{ kg/mol ja } M_h = 0.01802 \text{ kg/mol}$$

$$h_k = 1.006 t + x(2501 + 1.85 t), \text{ kJ/kg}_{d.a.}$$

### Wet bulb temperature

$$t - t_m = l(t_m) \frac{M_h}{\rho c_p} \frac{p}{RT} \text{Le}^{1-n} \ln \left( \frac{p - p_h}{p - p_h'(t_m)} \right),$$

### Solutions

$$\text{Ideal solution (Raoult law)} \quad p_i = x_i p_i'$$

$p_i$  = the partial pressure of gas component i

$p_i'$  = vapor pressure of pure liquid i

x = molar fraction in solution.

$$\text{Henry's law: } p_i = K_i x_i$$

$K_i$  = Henry law constant, Pa

x = molar fraction in a solution

## DIFFUSION AND ADVECTION

Fick's diffusion law  $\mathbf{j}_A = -D_{AB} \frac{\partial c_A}{\partial z}$       Fick's 2<sup>nd</sup> law:  $\frac{\partial c_A}{\partial t} = D_{AB} \frac{\partial^2 c_A}{\partial z^2} + S_A$

$$\mathbf{J}_i = c_i \mathbf{v}_i \quad \mathbf{N}_i = \rho_i \mathbf{v}_i \quad \mathbf{J} = \sum_i \mathbf{J}_i = c\mathbf{v} \quad \mathbf{j}_i = c_i(\mathbf{v}_i - \mathbf{v})$$

$$\mathbf{J}_i = c_i \mathbf{v} + \mathbf{j}_i \quad c\mathbf{v} = \sum_i c_i \mathbf{v}_i \quad \mathbf{v} = \sum_i x_i \mathbf{v}_i$$

$$\sum_i \mathbf{j}_i = 0 \quad D_{AB} = D_{BA} \quad \text{Binary mixture when } \mathbf{v} = 0: \quad \mathbf{J}_A = -\mathbf{J}_B$$

### Diffusion + advection (1D)

$$J_A = c_A v - D_{AB} \frac{dc_A}{dz} \quad J = c v = J_A + J_B$$

Steady state solutions:

$$J_A = v \left( \frac{c_{A2} - c_{A1} e^{\frac{vL}{D_{AB}}}}{1 - e^{\frac{vL}{D_{AB}}}} \right) \quad J_B = v \left( \frac{c_{B2} - c_{B1} e^{\frac{vL}{D_{AB}}}}{1 - e^{\frac{vL}{D_{AB}}}} \right)$$

### Stefan flow $J_B = 0$

$$J_A = \frac{j_A}{x_B}$$

steady state solution:

$$J_A = c v = \frac{D_{AB} c}{L} \ln \left( \frac{c_{B2}}{c_{B1}} \right)$$

## HEAT AND MASS TRANSFER ANALOGY

$$q = -\lambda \frac{\partial T}{\partial z} \Big|_{z=0} \quad \rightarrow J_A = -D_{AB} \frac{\partial c_A}{\partial z} \Big|_{z=0} \quad \text{Nu} \rightarrow \text{Sh} \quad \text{Pr} \rightarrow \text{Sc} \quad \text{Re does not change}$$

## DIFFUSION COEFFICIENT

Gas mixtures:  $D_{AB} = 0.0101 \frac{T^{1.75} (1/M_A + 1/M_B)^{1/2}}{p [(\Sigma v_A)^{1/3} + (\Sigma v_B)^{1/3}]^2}$

Note units! M = [g/mol], p = [Pa], T = [K]

	$\Sigma v$		$\Sigma v$
H <sub>2</sub>	7.07	CO	18.9
He	2.88	CO <sub>2</sub>	26.9
N <sub>2</sub>	17.9	NH <sub>3</sub>	14.9
O <sub>2</sub>	16.6	H <sub>2</sub> O	12.7
Air	20.1	SO <sub>2</sub>	41.1
N <sub>2</sub> O	35.9		

Solutions: Stokes-Einstein equation  $D_{AB} = \frac{k_B T}{6\pi\eta r}$

r = radius of the solute

$\eta$  = dynamic viscosity of the solvent

## HEAT TRANSFER

Conduction  $q = -\lambda \frac{\partial T}{\partial z}$

Convection (dry heat transfer)  $q = \alpha \Delta T$

Heat transferred due to evaporation (so called wet heat transfer)  $q = l \cdot N_h$

## MASS TRANSFER COEFFICIENT

General definition:  $J_A = k \Delta c_A$

$|J_A| \gg |J_B|$  :  $J_A = ck' \ln \left( \frac{c_{B2} - \frac{c}{r}}{c_{B1} - \frac{c}{r}} \right)$  where  $r = \frac{J_A}{J_B}$

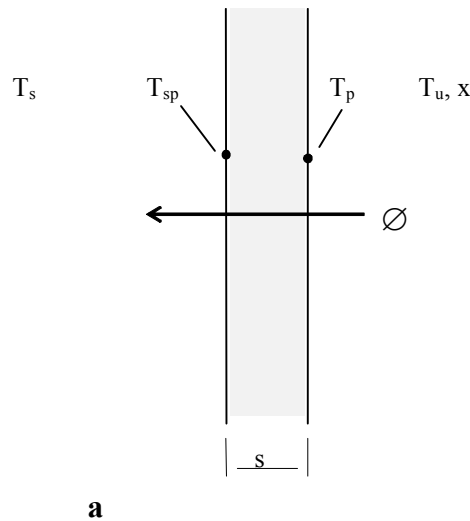
$r \rightarrow \infty$ :  $J_A = ck' \ln \left( \frac{c_{B2}}{c_{B1}} \right)$

mass transfer coefficient determined based on heat transfer coefficient  $\alpha$

$$k' = \frac{\alpha}{\rho c_p} Le^{1-n} \quad Le = \frac{D_{AB} \rho c_p}{\lambda} = \frac{Pr}{Sc}$$

Typically  $n \approx 0.33$ .

## DETERMINATION OF SURFACE TEMPERATURE $T_p$ DURING CONDENSATION OR EVAPORATION ON A WALL THAT SEPARATES TWO FLUIDS



$$\alpha_u (T_u - T_p) + l(T_p) M_h \frac{p}{RT_k} k' \ln \left( \frac{p - p'_h(T_p)}{p - p_h} \right) - G''(T_p - T_s) = 0$$

$$G'' = \frac{A_s}{A_u} \cdot \frac{1}{\frac{s}{\lambda} + \frac{1}{\alpha_s}}$$

$T_k$  = representative temperature at the wet side (as a first approximation, a dew point can be applied),

$\lambda$  = thermal conductivity of the wall separating the two fluid

$s$  = thickness of the wall

Subscripts: h=vapor, u = gas at the "wet" side, p = surface where condensing or evaporation may happen (i.e. surface at the wet side), s= fluid (gas or liquid) at the "dry" side,

### SERIAL RESISTANCES

Heat transfer:  $R = \sum_i R_i$  where  $R_i$  is a single heat transfer resistance defined as

$$\emptyset = \frac{\Delta T_i}{R_i}$$

Mass transfer:  $r = \sum_i r_i$  where  $r_i$  is a single mass transfer resistance defined as

$$N_i = \frac{\Delta c_i}{r_i} \text{ or } N_i = \frac{\Delta p_i}{r_i}$$

### THERMAL DIFFUSION

$$\mathbf{j}_A = -cD_{AB} \left[ \nabla x_A + k_T \frac{\nabla T}{T} \right] \quad k_T = D_T/D_{AB} \quad \alpha_T = \frac{k_T}{x_A x_B}$$

$D_T$  = thermal diffusion coefficient (m<sup>2</sup>/s),  $k_T$  = thermal diffusion ratio (-),  $\alpha_T$  = thermal diffusion factor

## MASS TRANSFER IN POROUS MATERIALS

All fluxes and flows ( $j, J, N, v'$ ) are evaluated per total cross-sectional areas!

No surface effects (modified Fick and diffusion-advection equations)

$$j_A = -D_{\text{eff}} \frac{\partial c_A}{\partial z} \quad D_{\text{eff}} = \frac{\Phi}{\tau} D_{AB}$$

$$\tau = \frac{s}{z}, \text{ (where } s = \text{tortuous path, } z = \text{straight distance)}$$

$$J_A = c_A v' - D_{\text{eff}} \frac{\partial c_A}{\partial z}$$

Darcy equation for pressure gradient driven flow

$$N = -\frac{k_p}{\nu} \frac{\partial p}{\partial z}$$

$\nu$  = kinematic viscosity of the fluid

Knudsen diffusion and the dusty gas model

$$\text{Kn} = \frac{\lambda_m}{d} \quad \lambda_m = \frac{k_B T}{\sqrt{2} \pi \sigma_{ii}^2 p} \quad D_{AK} = \frac{d}{3} \sqrt{\frac{8RT}{\pi M_A}}$$

$d$  = radius of a pore or channel, m

$\sigma_{ii}$  = collision diameter of the molecule (see Table 10), m

$$D_{AK,\text{eff}} = \frac{\Phi}{\tau} D_{AK}$$

$$j_A = -D_A \frac{\partial c_A}{\partial z} + x_A [D_A / D_{\text{eff}}] j \quad \frac{1}{D_A} = \frac{1}{D_{AK,\text{eff}}} + \frac{1}{D_{\text{eff}}}$$

## CAPILLARY PRESSURE

$$\Delta p_{\text{kap}} = p - p_2 = \frac{2\gamma \cos \theta}{r}$$

$p_2$  pressure of liquid just below the surface, Pa

$p$  total pressure of gas above the surface, Pa

$\gamma$  surface tension, J/m<sup>2</sup>

$\theta$  angle between the liquid and solid surface

$R$  radius of the tube, m



## PROPERTIES OF BOUND WATER

### Sorption heat for paper

$$r = r_{s0} \left( \frac{T}{T_{cr}} \right) \left( 1 - \frac{T}{T_{cr}} \right)^{r_T} \exp \left( -r_u \frac{w_r}{w_{r,max}} \right) \quad w_r \equiv \rho_{2p} / \rho_{1p},$$

$$r_{s0} = 6.051 \cdot 10^4 \text{ kJ/kg}, \quad r_u = 30.05, \quad r_T = 5.06 \quad w_{r,max} = 1.581.$$

### Relative vapor pressure in paper

$$\ln \varphi = \ln \varphi_o \cdot \left( \frac{w_{r,max}}{w_r} \right) \left( 1 - \frac{T}{T_{cr}} \right)^{\varphi_T} \exp \left( -\varphi_w \frac{w_r}{w_{r,max}} \right), \quad \text{missä } \varphi_T = 5.144, \quad \ln \varphi_o = -$$

$$1.856, \quad \varphi_w = 3.475.$$

## OSMOSIS AND REVERSE OSMOSIS

### Osmotic pressure

$$\pi_o = -\frac{RT}{v} \ln a,$$

$\pi_o$  = osmotic pressure, Pa

$a = \xi x$  = activity of solvent, -

$\xi$  activity coefficient, -

$v$  = molar volume of solvent, m<sup>3</sup>/mol

If the amount of dissolved substance is small:  $\pi_o = c_s RT$  where  $c_s$  is the concentration of dissolved substances (take into account the dissociation of ions!)

### Osmotic mass transfer through membranes

Volume flux of solvent (e.g. water) (m<sup>3</sup>/s/m<sup>2</sup><sub>membrane</sub>):

$$v' = L_p [\Delta p - \sigma \Delta \pi_o], \quad \text{where}$$

$\Delta p$  and  $\Delta \pi_o$  are the transmembrane pressure (Pa) and osmotic pressure (Pa) differences, respectively.

$\sigma$  reflection coefficient, -

$L_p$  filtration coefficient, m/sPa

## SOLUTION-DIFFUSION MODEL FOR NON-POROUS MEMBRANES

$$J_i = b_i \frac{\Delta c_i}{s}$$

$$b_i = H_i D_i$$

$$\alpha_{ij} = \frac{b_i}{b_j} = \frac{D_i}{D_j} \frac{H_i}{H_j}$$

$b_i$  = permeability,  $m^2/s$

$H_i$  = solubility of component  $i$  in the membrane material, -

$s$  = thickness of the membrane,  $m$

$D_i$  = diffusion coefficient of component  $i$  in the membrane,  $m^2/s$

$\alpha_{ij}$  = selectivity of the membrane between components  $i$  and  $j$  ( $\alpha_{ij} > 1$ ), -

*Table 1. Molar masses of elements.*

	M (g/mol)		M (g/mol)
Al	26.98	H	1.01
C	12.01	He	4.00
Ca	40.08	N	14.01
Cl	35.45	Na	22.99
Cu	63.55	O	16.00
Fe	55.85	S	32.06

*Table 1.3 Henry law constants at 298 K.*

Gas	Water as solvent (MPa)	Benzene as a solvent (MPa)
H <sub>2</sub>	7120	367
CH <sub>4</sub>	41.9	56.9
N <sub>2</sub>	8680	239
CO <sub>2</sub>	167	11.4
O <sub>2</sub>	4400	

Table 1.1. Properties of saturated air at an atmospheric pressure.

Temperature °C	humidity kg <sub>H2O</sub> / kg <sub>dry air</sub>	Partial pressure of water vapor kPa	Partial density of water vapor kg <sub>H2O</sub> / m <sup>3</sup>	Partial density of dry air kg <sub>dry air</sub> / m <sup>3</sup>	Specific enthalpy of mixture kJ/kg <sub>dry air</sub>	Specific heat of mixture J/kg <sub>dry air</sub> K
0	0.003821	0.6108	0.004846	1.285	9.55	1010.8
2	0.004418	0.7054	0.005557	1.275	13.06	1012.0
4	0.005100	0.8129	0.006358	1.264	16.39	1013.4
6	0.005868	0.9346	0.007257	1.254	20.77	1014.9
8	0.006749	1.0721	0.008267	1.243	25.00	1016.7
10	0.007733	1.2271	0.009396	1.232	29.52	1018.6
12	0.008849	1.4015	0.01066	1.221	34.37	1020.8
14	0.010105	1.5974	0.01206	1.211	39.57	1023.3
16	0.011513	1.8168	0.01363	1.199	45.18	1026.0
18	0.013108	2.062	0.01536	1.188	51.29	1029.1
20	0.014895	2.337	0.01729	1.177	57.86	1032.5
22	0.016892	2.642	0.01942	1.165	65.02	1036.4
24	0.019131	2.982	0.02177	1.154	72.60	1040.7
26	0.021635	3.360	0.02437	1.141	81.22	1045.5
28	0.024435	3.778	0.02723	1.129	90.48	1050.9
30	0.027558	4.241	0.03036	1.116	100.57	1056.9
32	0.031050	4.753	0.03380	1.103	111.58	1063.5
34	0.034950	5.318	0.03758	1.090	123.72	1071.0
36	0.039289	5.940	0.04171	1.076	136.99	1079.3
38	0.044136	6.624	0.04622	1.061	151.60	1088.5
40	0.049532	7.375	0.05114	1.046	167.64	1098.9
42	0.055560	8.198	0.05650	1.030	185.40	1110.3
44	0.062278	9.010	0.06233	1.014	204.94	1123.2
46	0.069778	10.085	0.06867	0.997	226.55	1137.5
48	0.078146	11.161	0.07553	0.9791	250.45	1153.4
50	0.087516	12.335	0.08298	0.9606	277.04	1171.3
52	0.098018	13.613	0.09103	0.9411	306.64	1191.3
54	0.10976	15.002	0.09974	0.9207	339.51	1213.7
56	0.12297	16.509	0.1091	0.8999	373.31	1238.9
58	0.13790	18.146	0.1193	0.8768	417.72	1267.3
60	0.15472	19.92	0.1302	0.8532	464.11	1299.4
62	0.17380	21.84	0.1419	0.8283	516.57	1335.7
64	0.19541	23.91	0.1545	0.8021	575.77	1377.0
66	0.22021	26.14	0.1680	0.7746	643.51	1424.1
68	0.24866	28.55	0.1826	0.7456	721.01	1478.2
70	0.28154	31.16	0.1981	0.715	810.36	1541.8
72	0.31966	33.96	0.2146	0.6829	915.57	1613.2
74	0.36468	36.96	0.2324	0.6489	1035.6	1698.6
76	0.41790	40.19	0.2514	0.6132	1179.42	1799.4
78	0.48048	43.65	0.2717	0.5755	1348.40	1919.9
80	0.55931	47.36	0.2933	0.5358	1560.80	2066.4
82	0.65573	51.33	0.3162	0.4939	1820.46	2247.7
84	0.77781	55.57	0.3406	0.4497	2148.92	2476.7
86	0.93768	60.5	0.3666	0.4031	2578.73	2773.9
88	1.15244	64.95	0.3942	0.3542	3155.67	3170.8
90	1.45873	70.11	0.4235	0.3026	3978.42	3730.4
92	1.92718	75.61	0.4545	0.2482	5236.61	4574
94	2.73170	81.46	0.4873	0.1909	7395.49	5987
96	4.42670	87.69	0.5221	0.1305	11944.39	8820
98	10.30306	94.3	0.5588	0.06694	27711.34	17338
100	∞	101.325	0.5977	0.000	∞	∞

Table 1.1 (continues).

Temp °C	Evaporation heat of water kJ/kg	Kinematic viscosity $10^{-6} \text{ m}^2/\text{s}$	Diffusion coefficient water-air $10^{-6} \text{ m}^2/\text{s}$	Thermal conductivity W/mK
0	2500.8	13.25	22.2	0.02380
2	2495.9	13.43	22.4	0.02413
4	2491.3	13.61	22.6	0.02427
6	2486.6	13.79	22.8	0.02440
8	2481.9	13.97	23.1	0.02454
10	2477.2	14.15	23.3	0.02466
12	2472.5	14.34	23.6	0.02478
14	2467.8	14.52	23.9	0.02490
16	2463.1	14.71	24.2	0.02500
18	2458.4	14.89	24.5	0.02511
20	2453.1	15.08	24.8	0.02520
22	2449.0	15.27	25.2	0.02529
24	2442.0	15.46	25.5	0.02537
26	2439.5	15.65	25.9	0.02544
28	2434.8	15.84	26.3	0.02548
30	2430.0	16.03	26.6	0.02556
32	2425.3	16.22	27.0	0.02561
34	2420.5	16.41	27.4	0.02565
36	2415.8	16.61	27.8	0.02567
38	2411.0	16.80	28.3	0.02569
40	2406.2	17.00	28.7	0.02569
42	2401.4	17.20	29.1	0.02568
44	2396.6	17.39	29.6	0.02566
46	2391.8	17.59	30.0	0.02563
48	2387.0	17.79	30.5	0.02558
50	2382.1	17.99	30.9	0.02552
52	2377.3	18.19	31.4	0.02545
54	2372.4	18.39	31.9	0.02536
56	2367.6	18.59	32.4	0.02526
58	2362.7	18.79	32.9	0.02514
60	2357.9	18.99	33.4	0.02501
62	2353.0	19.19	34.0	0.02487
64	2348.1	19.38	34.5	0.02471
66	2343.1	19.57	35.1	0.02455
68	2338.2	19.76	35.7	0.02437
70	2333.3	19.94	36.3	0.02418
72	2328.3	20.10	36.9	0.02399
74	2323.3	20.28	37.6	0.02379
76	2318.3	20.44	38.3	0.02360
78	2313.3	20.58	39.0	0.02341
80	2308.3	20.71	39.8	0.02323
82	2303.2	20.81	40.7	0.02307
84	2298.1	20.90	41.5	0.02294
86	2293.0	20.96	42.5	0.02285
88	2287.9	20.99	43.6	0.02281
90	2282.8	20.99	44.7	0.02283
92	2277.6	20.94	46.0	0.02295
94	2272.4	20.84	47.4	0.02318
96	2267.1	20.69	49.0	0.02355
98	2261.9	20.47	50.8	0.02409
100	2256.7	20.08	52.8	0.02486

Table 1.2. Thermodynamic properties of dry air at 1 bar.

t °C	$\rho$ kg/m <sup>3</sup>	$\nu$ 10 <sup>-6</sup> m <sup>2</sup> /s	$c_p$ kJ/kgK	h kJ/kg	$\lambda$ 10 <sup>-3</sup> W/mK	Pr
-180	3.852	1.67	1.073	90.509	8.59	0.804
-160	3.126	2.51	1.037	111.53	10.41	0.782
-140	2.639	3.49	1.021	132.11	12.22	0.770
-120	2.287	4.58	1.014	152.42	14.00	0.759
-100	2.019	5.80	1.011	172.68	15.77	0.751
-80	1.807	7.13	1.009	192.87	17.50	0.743
-60	1.636	6.57	1.008	213.02	19.20	0.564
-40	1.495	10.11	1.007	233.14	20.89	0.729
-20	1.377	11.73	1.006	253.27	22.50	0.722
0	1.275	13.45	1.006	273.41	24.08	0.716
20	1.188	15.27	1.006	293.54	25.61	0.713
40	1.112	17.15	1.007	313.68	27.08	0.709
60	1.045	19.13	1.009	333.84	28.48	0.708
80	0.9859	21.18	1.010	354.02	29.91	0.705
100	0.9329	23.29	1.012	374.23	31.26	0.703
120	0.8854	25.50	1.014	394.48	32.59	0.702
140	0.8425	27.76	1.017	414.78	33.92	0.701
160	0.8035	30.09	1.020	435.14	35.24	0.700
180	0.7681	32.51	1.023	455.55	36.53	0.699
200	0.7356	34.94	1.026	476.03	37.82	0.697
220	0.7058	37.46	1.029	496.58	39.07	0.696
240	0.6783	40.06	1.033	517.2	40.34	0.696
260	0.6528	42.74	1.037	537.9	41.57	0.696
280	0.6292	45.44	1.041	558.69	42.79	0.696
300	0.6072	48.22	1.046	579.56	43.99	0.696
350	0.5585	55.4	1.057	632.13	46.92	0.697
400	0.517	62.9	1.059	685.28	49.83	0.691
450	0.4813	70.7	1.081	739.04	52.50	0.701
500	0.4502	78.8	1.093	793.39	55.45	0.699
550	0.4228	87.2	1.105	848.33	58.20	0.700
600	0.3906	96.0	1.116	903.83	60.93	0.687
650	0.377	105.0		959.88	63.59	
700	0.3577	114.3	1.137	1016.4	65.95	0.705
750	0.3396	124.0		1073.5	68.24	
800	0.3243	133.6	1.155	1131.0	70.5	0.710
850	0.3099	143.6		1188.9	72.7	
900	0.2967	153.7	1.171	1247.3	74.6	0.716
950	0.2846	164.4		1305.9	76.8	
1000	0.2734	175.1	1.185	1355.0	78.7	0.721
1050	0.2631	186.1		1424.4	80.6	
1100	0.2535	197.3	1.198	1484.0	82.5	0.726
1150	0.2446	209		1543.9	84.3	
1200	0.2363	220	1.209	1604.1	86.1	0.730
1250	0.2285	232	-	1664.5	-	-

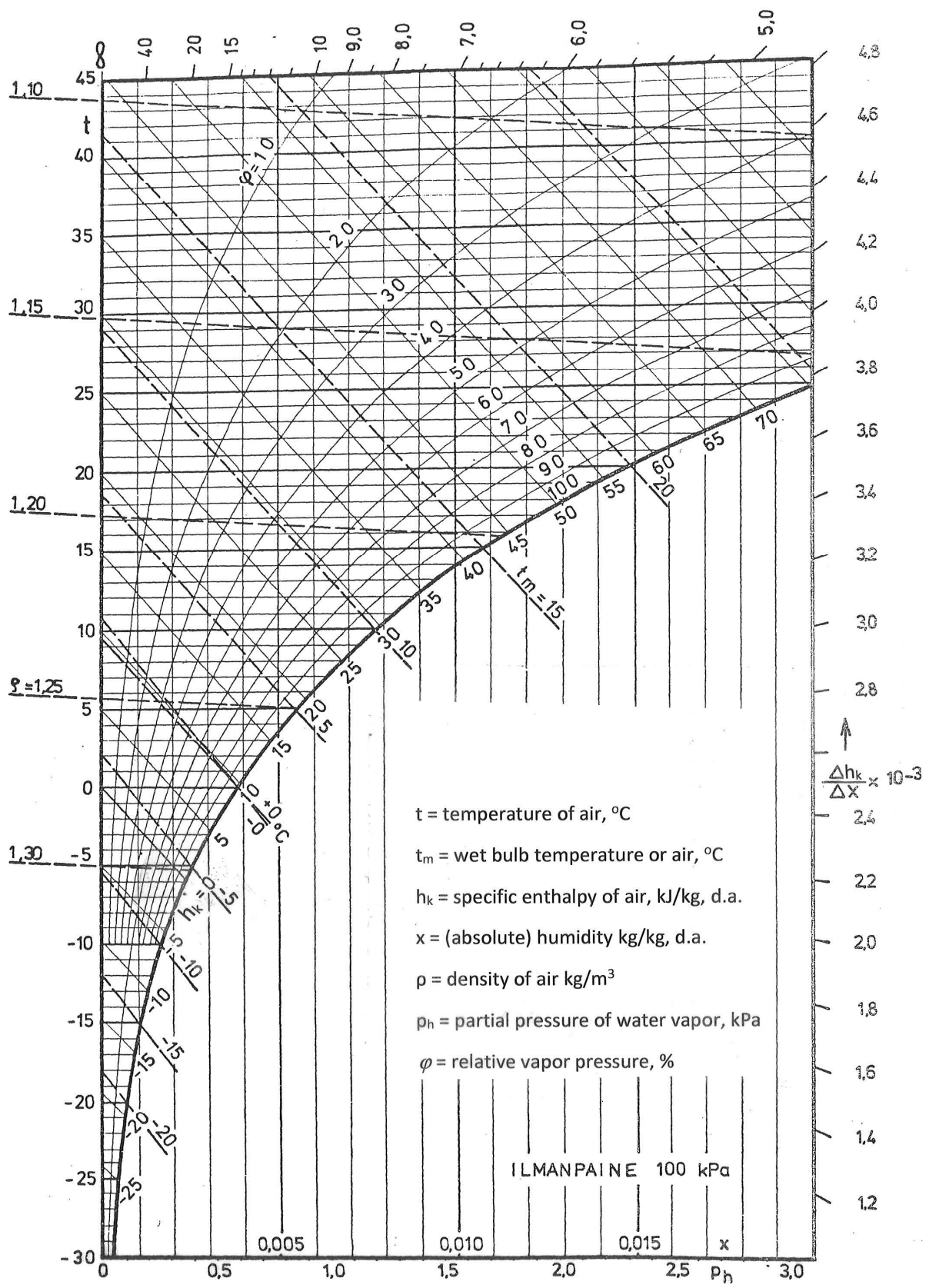


Figure 1.1. Mollier-diagram for humid air at total pressure 100 kPa.

Table 1.3. Properties of water at 1 atm.

T	$\rho$	$\eta$	$\lambda$	$c_p$	$c_v$	Pr
°C	kg/m <sup>3</sup>	10 <sup>-3</sup> kg/(ms)	W/(mK)	kJ/(kgK)	kJ/(kgK)	
0	999.868	1.7921	0.5535	4.2169	4.21	13.65
1	999.927	1.7311	0.5560	4.2133		13.12
2	999.968	1.6736	0.5584	4.2099		12.62
3	999.992	1.6192	0.5608	4.2069		12.15
4	1 000.000	1.5677	0.5631	4.2040		11.70
5	999.992	1.5188	0.5655	4.2014	4.20	11.28
6	999.968	1.4723	0.5678	4.1991		10.89
7	999.930	1.4281	0.5701	4.1969		10.51
8	999.876	1.3860	0.5723	4.1949		10.16
9	999.809	1.3459	0.5745	4.1931		9.82
10	999.728	1.3077	0.5767	4.1914	4.19	9.50
11	999.633	1.2712	0.5789	4.1899		9.20
12	999.525	1.2362	0.5810	4.1885		8.91
13	999.404	1.2029	0.5831	4.1872		8.64
14	999.271	1.1709	0.5852	4.1861		8.38
15	999.127	1.1403	0.5873	4.1850	4.17	8.13
16	998.971	1.1109	0.5893	4.1841		7.89
17	998.803	1.0828	0.5913	4.1832		7.66
18	998.624	1.0558	0.5933	4.1823		7.44
19	998.435	1.0298	0.5952	4.1817		7.24
20	998.234	1.0049	0.5971	4.1811	4.15	7.04
21	998.023	0.9809	0.5990	4.1805		6.85
22	997.802	0.9578	0.6009	4.1800		6.66
23	997.570	0.9356	0.6027	4.1796		6.49
24	997.329	0.9142	0.6046	4.1792		6.32
25	997.077	0.8935	0.6063	4.1788	4.14	6.16
26	996.816	0.8736	0.6081	4.1785		6.00
27	996.545	0.8544	0.6099	4.1782		5.85
28	996.265	0.8359	0.6116	4.1780		5.71
29	995.976	0.8180	0.6133	4.1778		5.57
30	995.678	0.8007	0.6149	4.1777	4.11	5.44
31	995.371	0.7840	0.6166	4.1776		5.31
32	995.056	0.7679	0.6182	4.1775		5.19
33	994.732	0.7523	0.6198	4.1775		5.07
34	994.401	0.7372	0.6210	4.1774		4.96
35	994.061	0.7225	0.6229	4.1774	4.09	4.85
36	993.714	0.7084	0.6244	4.1775		4.74
37	993.359	0.6946	0.6259	4.1775		4.64
38	992.996	0.6813	0.6274	4.1776		4.54
39	992.626	0.6685	0.6288	4.1777		4.44
40	992.250	0.6560	0.6303	4.1778	4.07	4.35
41	991.866	0.6438	0.6317	4.1779		4.26
42	991.468	0.6321	0.6330	4.1781		4.17
43	991.071	0.6207	0.6344	4.1783		4.09
44	990.662	0.6096	0.6357	4.1784		4.01
45	990.251	0.5988	0.6371	4.1787		3.93
46	989.820	0.5884	0.6384	4.1789		3.85
47	989.397	0.5782	0.6396	4.1791		3.78
48	988.964	0.5683	0.6409	4.1794		3.71
49	988.516	0.5587	0.6421	4.1796		3.64
50	988.068	0.5494	0.6433	4.1800	4.03	3.57
55	985.729	0.5064	0.6490	4.1816		3.26



Table 4.1. Critical Rayleigh numbers  $Ra_{cr}$ . If  $Ra_{cr} = \infty$ , free convection cannot occur. If  $Ra_{cr} = 0$ , free convection always occur.

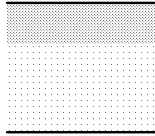
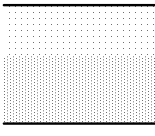
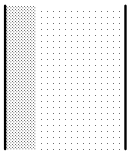
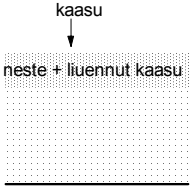
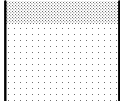
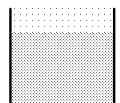
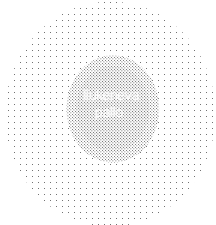
		Critical Rayleigh numbers ( $Ra_{cr}$ )	
Two parallel plates, denser fluid above		$\frac{L^4 g}{\eta D_{AB}} \frac{d\rho}{dz} = 1708$	$L =$ distance between plates
Two parallel plates, denser fluid below		$\frac{L^4 g}{\eta D_{AB}} \frac{d\rho}{dz} = \infty$	$L =$ distance between plates
Two vertical plates, denser fluid on the other side		$\frac{L^4 g}{\eta D_{AB}} \frac{d\rho}{dz} = 0$	$L =$ distance between plates
Gas absorbing into a horizontal layer of solvent producing a dense solution		$\frac{L^4 g}{\eta D_{AB}} \frac{d\rho}{dz} = 110$	$L =$ thickness of the liquid layer
Vertical tube, denser fluid above		$\frac{r_0^4 g}{\eta D_{AB}} \frac{d\rho}{dz} = 67.94$	$r_0 =$ tube radius
Vertical tube, denser fluid below		$\frac{r_0^4 g}{\eta D_{AB}} \frac{d\rho}{dz} = \infty$	$r_0 =$ tube radius
Dissolving sphere		$\frac{r_0^4 g}{\eta D_{AB}} \frac{d\rho}{dr} = 0$	$r_0 =$ sphere radius

Table 5.2. Experimental values for gas diffusion coefficients at 1 atm..

Gas mixture	Temperature (K)	Diffusion coefficient ( $10^{-5} \text{ m}^2/\text{s}$ )
Air - CH <sub>4</sub>	282	1.96
Air - H <sub>2</sub>	282	7.1
Air - D <sub>2</sub>	296.8	5.65
Air - He	282	6.58
Air - H <sub>2</sub> O	298.2	2.6
Air - CO <sub>2</sub>	282	1.48
Air- ethanol	273.0	1.02
Air - n-hexane	294	0.80
Air - n-heptane	294	0.71
Air – benzene	298.2	0.96
Air – toluene	299.1	0.86
Air - 2-propanol	299.1	0.99
Air – butanol	299.1	0.87
Air - 2-butanol	299.1	0.89
CH <sub>4</sub> - H <sub>2</sub>	298.0	7.26
CH <sub>4</sub> - H <sub>2</sub> O	307.7	2.92
CO <sub>2</sub> - O <sub>2</sub>	296	1.56
CO <sub>2</sub> - SO <sub>2</sub>	263	0.64
H <sub>2</sub> – He	317	17.06
H <sub>2</sub> - D <sub>2</sub>	288.2	12.4
H <sub>2</sub> – acetone	296	4.24
H <sub>2</sub> - n-butane	287.9	3.61
H <sub>2</sub> – benzene	311.3	4.04
N <sub>2</sub> - H <sub>2</sub> O	298.2	2.93
N <sub>2</sub> - O <sub>2</sub>	316	2.3
N <sub>2</sub> - SO <sub>2</sub>	263	1.04
O <sub>2</sub> – benzene	311.3	1.01
O <sub>2</sub> – cyclohexane	288.6	0.75
O <sub>2</sub> - n-hexane	288.6	0.75
O <sub>2</sub> - n-octane	303.1	0.71
Freon 12 – benzene	298.2	0.39
Freon 12 - ethanol	298.2	4.75

*Table 5.3. Diffusion coefficients at infinite dilution in water at 25 °C. Note! concentration  $c_1$  is in unit mol/liter.*

Solute	Diffusion coefficient ( $10^{-9}$ m <sup>2</sup> /s)	Solute	Diffusion coefficient ( $10^{-9}$ m <sup>2</sup> /s)
Argon	2.00	Benzene	1.02
Air	2.00	Sulphur acid	1.73
CO <sub>2</sub>	1.92	Nitric acid	2.60
CO	2.03	Acetylene	0.88
Ethane	1.2	Methanol	0.84
Ethylene	1.87	Ethanol	0.84
Helium	6.28	Formic acid	1.50
Hydrogen	4.5	Acetic acid	1.21
Methane	1.49	Benzoic acid	1.00
N <sub>2</sub>	1.88	Acetone	1.16
O <sub>2</sub>	2.10	Urea	$(1380 - 78.2c_1 + 4.64c_1^2)/1000$
Chlorine	1.25	Sucrose	$(0.5228 - 0.265c_1)$
Propane	0.97	Hemoglobin	0.069

*Table 6.1. Dimensionless variables.*

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$$\text{Sherwoodi number } Sh = \frac{kl}{D_{AB}}$$

$$\text{Schmidt number } Sc = \frac{\nu}{D_{AB}}$$

$$\text{Prandtl number } Pr = \frac{\eta c_p}{\lambda}$$

$$\text{Lewis number } Le = \frac{D_{AB} \rho c_p}{\lambda} = \frac{Pr}{Sc}$$

$$\text{Reynolds number } Re = \frac{ul}{\nu}$$

$$\text{Grashof number } Gr = \frac{l^3 g \Delta \rho}{\rho \nu^2}$$

$$\text{Rayleigh number } Ra = \frac{l^4 g}{\eta D_{AB}} \frac{d\rho}{dz}$$

$$\text{Nusselt number } Nu = \frac{\alpha l}{\lambda}$$

$$\text{Péclet number } Pe = \frac{ul}{D_{AB}}$$

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$c_p$  = specifiv heat at constant prssure,  $D_{AB}$  = diffusion coefficient,  $g$  = acceleration due to gravity =9.807m/s<sup>2</sup>,  $k$  = mass transfer coefficient,  $l$  = characteristic lenght,  $u$  = flow velocity,  $z$  = coordinate in direction to the flow,  $\alpha$  = convection heat transfer coefficient,  $\lambda$  = thermal conductivity,  $\nu$  = kinematic viscosity,  $\eta$  = dynamic viscosity,  $\rho$  = density.

Table 7.1. Mass transfer correlations.

Case	Correlation equation	Notice!
Large liquid drops rising in stirred solution	$Sh = 0.13 \left( \frac{(P/V) l^4}{\rho \nu^3} \right)^{1/4} Sc^{1/3}$	$l=d$ = bubble diameter $P/V$ = stirrer power per volume
Pure gas bubbles in an unstirred liquid	$Sh = 0.31 Gr^{1/3} Sc^{1/3}$	For small swarms of bubbles rising in liquid $l$ = drop diameter $\Delta\rho$ = density difference between drops and surrounding fluid
Large liquid drops rising in unstirred solution.	$Sh = 0.42 Gr^{1/3} Sc^{1/2}$	$l$ = drop diameter $\geq 3$ mm $\Delta\rho$ = density difference between drops and surrounding fluid
Small liquid drops rising in unstirred solution	$Sh = 1.13 (Re Sc)^{4/5}$	$l$ = drop diameter $u$ = drop velocity
Falling films	$Sh_z = 0.69 (Re_z Sc)^{1/2}$	$l = z$ = position along film measured from the top of the film $u$ = average film velocity
Turbulent flow through circular tube.	$Sh = 0.026 Re^{4/5} Sc^{1/3}$	$l$ = tube diameter
Free convection around a solid sphere.	$Sh = 2 + 0.6 Gr^{1/4} Sc^{1/3}$	$l$ = sphere diameter
Spinning disc	$Sh = 0.62 Re_\omega^{1/2} Sc^{1/3}$	Valid: $100 \leq Re_\omega \leq 20\,000$ $Re_\omega = \frac{l^2 \omega}{\nu}$ , $l$ = disc diameter disc rotation (rad/s)

$$Re = \frac{ul}{\nu}, Sh = \frac{kl}{D}, Sc = \frac{\nu}{D}, Gr = \frac{l^3 g \Delta\rho / \rho}{\nu^2}$$

$l$  = characteristic size,  $D$  = diffusion coefficient,  $g$  = acceleration due gravity,  $u$  = velocity,  $\nu$  = kinematic viscosity,  $\rho$  = density

Table 9.1. Thermal diffusion factors ( $\alpha_T$ ) for mixtures.

Mixture <sup>1</sup>	Temperature range K	$\alpha_T$
<b>Gases</b>		
(A) 50% D <sub>2</sub> - (B) 50% H <sub>2</sub>	290-370	+0.17
(A) 50% He - (B) 50% H <sub>2</sub>	273-700	+0.15
(A) 50% CH <sub>4</sub> - (B) 50% H <sub>2</sub>	300-500	+0.29
(A) 50% O <sub>2</sub> - (B) 50% N <sub>2</sub>	293	+0.02
(A) 50% CO <sub>2</sub> - (B) 50% N <sub>2</sub>	290-400	+0.05
<b>Liquids</b>		
(A) 80% CCl <sub>4</sub> - (B) 20% cyclohexane	313	+1.3
(A) 50% CCl <sub>4</sub> - (B) 50% cyclohexane	313	+1.3
(A) 20% CCl <sub>4</sub> - (B) 80% cyclohexane	313	+1.3
(A) 80% benzene - (B) 20% cyclohexane	313	-0.1
(A) 50% benzene - (B) 50% cyclohexane	313	-0.4
(A) 20% benzene - (B) 80% cyclohexane	313	-0.6
(A) 75% ethanol - (B) 25% water	298	-0.9
(A) 40% ethanol - (B) 60% water	298	-1.5
(A) 10% ethanol - (B) 90% water	298	+0.3
(A) water - (B) 0.01-M KCl	303	-0.6
(A) water - (B) 0.01-M NaCl	303	-0.9

<sup>1</sup>All in molar fractions except KCl and NaCl solutions.

Table 10. Collision diameters of molecules  $\sigma_{ii}$ .  $1 \text{ pm} = 10^{-12} \text{ m}$ .

	$\sigma_{ii}$ (pm)		$\sigma_{ii}$ (pm)
H2	289	N2	364
He	260	CO	376
CH4	380	CO2	330
H2O	265		

Table 10.2. Surface tension ( $\gamma$ ) of water.

T/K	$\gamma$ (J/m <sup>2</sup> )	$T \frac{\partial \gamma}{\partial T}$ (J/m <sup>2</sup> )
273	$75.5 \cdot 10^{-3}$	$-67.6 \cdot 10^{-3}$
323	$63.1 \cdot 10^{-3}$	$-77.8 \cdot 10^{-3}$
373	$51.5 \cdot 10^{-3}$	$-86.8 \cdot 10^{-3}$