



Aalto University
School of Electrical
Engineering

Coverage Path Planning

Wide Area Coverage!!

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Motivation

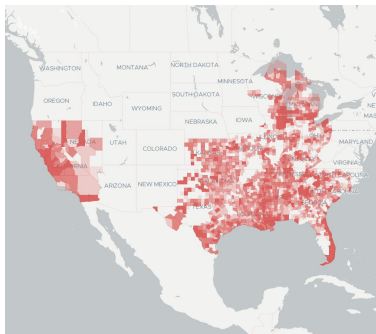
- ▶ Definition of a robot ✓
- ▶ Robot positioning (Localization) ✓
- ▶ Path planning
 - ▷ Graph-based ✓
 - ▷ Information-based ✓
 - ▷ Area-Coverage ...

Applications:

- ▶ Area surveillance
 - ▷ Forest, disaster site, *etc.*
- ▶ Patrolling
 - ▷ Event crowd, enemy territory, *etc.*

Let's get to business!!!

Intuition



- ▶ AT&T Internet Availability Map.¹
- ▶ To be a monopoly, tap maximal regions asap.
- ▶ Higher Coverage → lower competition.

Intuition (cont.)

In a robotic setting:

- ▶ Operation environment \rightarrow unknown.
- ▶ Unknown \propto Risk.
- ▶ Minimize risk by acquiring maximal observations until mission termination.

¹Image taken from <https://broadbandnow.com/ATT>

Coverage Path Planning (CPP)-Travelling Salesman

Mission:

- ▶ Maximize Sales → visit *all* locations.
- ▶ *Shortest* possible route.

Coverage Path Planning (CPP)-Travelling Salesman (cont.)



Figure: 8 cities across USA² for selling a product. Salesman has 5040 possible ways of covering these cities.

Coverage Path Planning (CPP)-Travelling Salesman (cont.)

Possible route selection strategies:

▶ **Greedy:**

- ▶ Choose next closest city.
- ▶ Produces sub-optimal routes.

Coverage Path Planning (CPP)-Travelling Salesman (cont.)

▶ 2 Opt Swap:

- ▶ Prevents route cross-overs
- ▶ Select 2 edges and reconnect to form new paths

Methods for selecting edges for swapping:

Coverage Path Planning (CPP)-Travelling Salesman (cont.)

◇ *Local Search:*

- Start with a random route.
- Select arbitrary pair of edges.
- If swapping reduces path length, retain and repeat.

Coverage Path Planning (CPP)-Travelling Salesman (cont.)

- Suffers from local minima

Coverage Path Planning (CPP)-Travelling Salesman (cont.)

- ◇ *Simulated Annealing:*
 - Probabilistically accept worse solutions early on.
 - Define temperature \propto affinity for “bad” solution.
 - ▶ Hot \rightarrow Accept Bad Solutions
 - ▶ Cold \rightarrow Reject
 - ▶ Start with Hot

²Image from <https://www.youtube.com/watch?v=SC5CX8drAtU>

Coverage Path Planning (CPP)-Lawnmower

Mission:



- ▶ Lawn with 2 static stones³.
- ▶ Mow *whole* lawn.
- ▶ Avoid *static* obstacles.

Coverage Path Planning (CPP)-Lawnmower (cont.)

Figure: Showcasing the progress of Lawn Mower algorithm. **N.B.:** Notice the exhaustive nature of this approach.

³Taken from https://www.youtube.com/watch?v=c_8d5sY455o

Coverage Path Planning (CPP)-Piano Mover

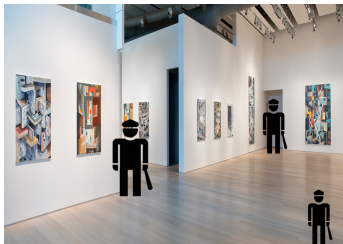
Mission:



- ▶ Move piano from shop to buyer's house
- ▶ Find *shortest* path through city

Coverage Path Planning (CPP)-Art Gallery

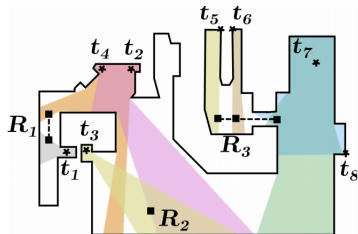
Mission:



- ▶ Art gallery with expensive exhibits
- ▶ Hire security personnel to monitor gallery at all times
- ▶ *How many guards are enough to patrol a gallery with n walls?*

Coverage Path Planning (CPP)-Watchman Route

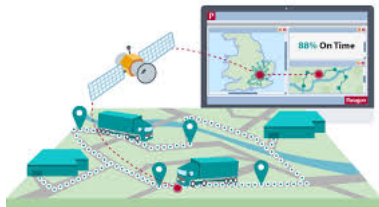
Mission:



- ▶ Consider a set of target points (denoted by \star) in a polygonal environment as shown.
- ▶ The objective of the watchmen denoted by R_1, \dots, R_3 is to find paths (denoted by $- -$) such that each target (\star) is seen from at least one viewpoint (\blacksquare).
- ▶ In this setup, watchman R_1 can observe t_1 and t_2 , R_2 can monitor t_3 and t_4 while R_3 can see $t_5 - t_8$.

Coverage Path Planning (CPP)-Orienteering

Mission:



- ▶ Given a start, goal and set of intermediate nodes like a truck with depots⁴.
- ▶ Find a subset of nodes:
 - ▷ Maximize net reward
 - ▷ Remain within time budget
 - ◇ *E.g.*, imagine delivering dairy products which perish as time passes
- ▶ Well known for vehicle routing problems

⁴Image from <http://tinyurl.com/yxhn9o53>

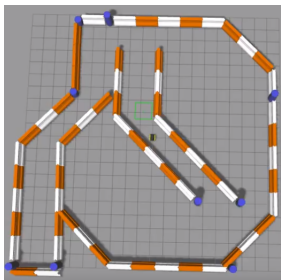
Coverage Path Planning (CPP)-Random Exploration

Mission:

- ▶ Pick a direction as per whim
- ▶ Rinse-and-repeat

Coverage Path Planning (CPP)-Frontier-based Exploration

Mission:



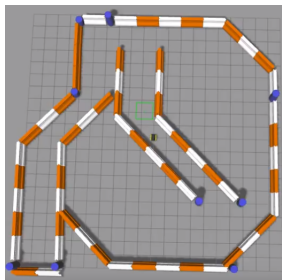
- ▶ Identify the frontier
 - ▷ Barrier between *known* and *unknown*
 - ▷ Function of sensing range
- ▶ Move to a candidate on frontier
- ▶ Rinse-and-repeat until all area is observed.

Coverage Path Planning (CPP)-Frontier-based Exploration (cont.)



Figure: Illustration of frontier-based expansion of civilization in a strategy game⁵.

Coverage Path Planning (CPP)-Frontier-based Exploration (cont.)



- ▶ *Grey*: Unobserved region; *White*: Observed region; *Blue*: Frontier
- ▶ Expansion using laser scanning

⁵Image from

<http://www.indieretronews.com/2015/03/freeciv-open-source-inspired.html>

Coverage Path Planning (CPP)-Adaptive Voronoi Exploration

Primer on Voronoi Tesselation:

- ▶ Encodes proximity information between object pairs
 - ▷ Each object is called a *site*
 - ▷ Set of pts. in ND that are closer to each site than to any other site form a *Voronoi Cell*
 - ▷ Convex hull of all cells gives a *Voronoi Diagram*.

Coverage Path Planning (CPP)-Adaptive Voronoi Exploration (cont.)

Mission:

- ▶ Generate Voronoi tessellation
- ▶ adapt Voronoi cells to faulty hardware⁶
 - ▷ Robot 1 has a faulty actuator. Note how its voronoi cell shrinks.

⁶Presented in <https://www.youtube.com/watch?v=qyYt3frZ7aw>

Coverage Path Planning (CPP)-Challenges

- ▶ These methods are exhaustive in nature
- ▶ Computationally challenging as size of area increases
- ▶ Hard to define an optimal termination condition
 - ▷ Robot resources vs exhaustivity

Summary

Over the span of last 2 days:

- ▶ Presented Graph-based path planning
 - ▷ Best-first search
 - ▷ Sampling-based search
- ▶ Brief intro to Informative path planning
- ▶ Per request, presented Coverage path planning
- ▶ All these 3 classes cover vast majority of well-known planners

You have a path, can you execute it?

"Book" — 2019/2/26 — 18:59 — page i — #1

Multi-Robot Exploration For Environmental Monitoring

The Resource Constrained
Perspective

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1st Edition

Thank You!!