

$$\bar{\mathbf{D}} = \bar{\mathbf{E}} + \left( \bar{\boldsymbol{\zeta}} + \frac{\bar{\mathbf{k}} \times \bar{\mathbf{I}}}{\omega} \right) \cdot \bar{\boldsymbol{\mu}}^{-1} \cdot \left( \frac{\bar{\mathbf{k}} \times \bar{\mathbf{I}}}{\omega} - \bar{\mathbf{J}} \right)$$

$$\bar{\mathbf{E}} = \bar{\epsilon}_r \epsilon_0, \quad \bar{\boldsymbol{\mu}} = \mu_0 \bar{\mathbf{I}}, \quad \bar{\boldsymbol{\zeta}} = 0, \quad \bar{\mathbf{J}} = 0$$

$$\bar{\mathbf{D}} = \epsilon_0 \bar{\boldsymbol{\epsilon}}_r + \frac{1}{\omega^2 \mu_0} \bar{\mathbf{k}} \times (\bar{\mathbf{k}} \times \bar{\mathbf{I}})$$

$$= \epsilon_0 \underbrace{(\bar{\boldsymbol{\epsilon}}_r + n^2 \bar{\mathbf{v}} \times (\bar{\mathbf{v}} \times \bar{\mathbf{I}}))}_{\bar{\mathbf{B}}}$$

$$\bar{\mathbf{k}} = k_0 n \bar{\mathbf{v}} \quad \left[ \bar{\mathbf{v}} \cdot \bar{\mathbf{v}} = 1 \right]$$

$$k_0 = \omega \sqrt{\mu_0 \epsilon_0}$$

$$\bar{\mathbf{B}} = \underbrace{\epsilon_{\perp} \bar{\mathbf{I}}_t + \epsilon_{\parallel} \bar{\mathbf{u}} \bar{\mathbf{u}}}_{\bar{\boldsymbol{\epsilon}}_r} + n^2 (\bar{\mathbf{v}} \bar{\mathbf{v}} - \bar{\mathbf{I}}) \quad \leftarrow \bar{\mathbf{I}}_t + \bar{\mathbf{u}} \bar{\mathbf{u}}$$

$$\bar{\mathbf{u}} \uparrow \theta \bar{\mathbf{v}}$$

$$= (\epsilon_{\perp} - n^2) \bar{\mathbf{I}}_t + (\epsilon_{\parallel} - n^2) \bar{\mathbf{u}} \bar{\mathbf{u}} + n^2 \bar{\mathbf{v}} \bar{\mathbf{v}}$$

$$\det \bar{\mathbf{B}} = \frac{1}{6} \bar{\mathbf{B}} \times \bar{\mathbf{B}} \cdot \bar{\mathbf{B}} \quad \Rightarrow 27 \text{ terms!}$$

$$\bar{\mathbf{I}}_t \times \bar{\mathbf{I}}_t \cdot \bar{\mathbf{I}}_t = 0$$

$$\bar{\mathbf{I}}_t \times \bar{\mathbf{I}}_t \cdot \bar{\mathbf{u}} \bar{\mathbf{u}} = 2$$

$$\bar{\mathbf{I}}_t \times \bar{\mathbf{I}}_t \cdot \bar{\mathbf{v}} \bar{\mathbf{v}} = 2 \cos^2 \theta$$

$$\bar{\mathbf{I}}_t \times \bar{\mathbf{v}} \bar{\mathbf{v}} \cdot \bar{\mathbf{v}} \bar{\mathbf{v}} = 0$$

$$\bar{\mathbf{I}}_t \times \bar{\mathbf{u}} \bar{\mathbf{u}} \cdot \bar{\mathbf{u}} \bar{\mathbf{u}} = 0$$

$$\bar{\mathbf{I}}_t \times \bar{\mathbf{u}} \bar{\mathbf{u}} \cdot \bar{\mathbf{v}} \bar{\mathbf{v}} = \sin^2 \theta$$

$$\bar{\mathbf{u}} \bar{\mathbf{u}} \times \bar{\mathbf{v}} \bar{\mathbf{v}} \cdot \bar{\mathbf{v}} \bar{\mathbf{v}} = 0$$

$$\bar{\mathbf{u}} \bar{\mathbf{u}} \times \bar{\mathbf{u}} \bar{\mathbf{u}} \cdot \bar{\mathbf{v}} \bar{\mathbf{v}} = 0$$

$$\bar{\mathbf{u}} \bar{\mathbf{u}} \times \bar{\mathbf{u}} \bar{\mathbf{u}} \cdot \bar{\mathbf{u}} \bar{\mathbf{u}} = 0$$

$$\bar{\mathbf{v}} \bar{\mathbf{v}} \times \bar{\mathbf{v}} \bar{\mathbf{v}} \cdot \bar{\mathbf{v}} \bar{\mathbf{v}} = 0$$

$$(\bar{\mathbf{I}}_t \cdot \underbrace{\bar{\mathbf{v}} \bar{\mathbf{v}} \times \bar{\mathbf{v}} \bar{\mathbf{v}}}) = 0$$

$$\det \bar{\mathbf{B}} = (\epsilon_{\perp} - n^2)^2 (\epsilon_{\parallel} - n^2) + \cos^2 \theta (\epsilon_{\perp} - n^2)^2 n^2 + \sin^2 \theta (\epsilon_{\perp} - n^2) (\epsilon_{\parallel} - n^2) n^2$$

$$\det \bar{B} = (\epsilon_{\perp} - n^2)(\epsilon_{\parallel} - n^2) + \cos \theta (\epsilon_{\perp} - n^2) n^2 \sin^2 \theta + \sin^2 \theta (\epsilon_{\perp} - n^2) n^2 \cos^2 \theta$$

$$= (\epsilon_{\perp} - n^2) (\epsilon_{\perp} \epsilon_{\parallel} - n^2 \epsilon_{\perp} \sin^2 \theta - n^2 \epsilon_{\parallel} \cos^2 \theta)$$

$$\Rightarrow n_o^2 = \epsilon_{\perp} \quad (\text{ORDINARY WAVE})$$

$$n_x^2 = \frac{\epsilon_{\perp} \epsilon_{\parallel}}{\epsilon_{\perp} \sin^2 \theta + \epsilon_{\parallel} \cos^2 \theta} \quad (\text{EXTRAORDINARY WAVE})$$

REFRACTIVE INDEX IS THE SAME:  $n_o = n_x = \sqrt{\epsilon_{\perp}}$

FOR  $\theta = 0 \leftarrow$  PROPAGATION DIRECTION  
(OPTICAL AXIS)